# Molecular Electrostatics for Probing Hydrogen Bonds, Halogen Bonds and Lone Pair- $\pi$ Interactions and Design of Receptors for Lone Pair Bearing Molecules

Thesis submitted to Cochin University of Science and Technology for the award of Degree of

**Doctor of Philosophy** in Chemistry under the Faculty of Science

By

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### DECLARATION

I hereby declare that the matter embodied in the Ph.D. thesis entitled "Molecular Electrostatics for Probing Hydrogen Bonds, Halogen Bonds and Lone Pair- $\pi$ Interactions and Design of Receptors for Lone Pair Bearing Molecules" is the result of investigations carried out by me at the Inorganic and Theoretical Chemistry Section, Chemical Sciences and Technology Division, CSIR-National Institute for Interdisciplinary Science and Technology (CSIR-NIIST), Trivandrum, under the supervision of Dr. C. H. Suresh and the same has not been submitted elsewhere for a degree, diploma or title.

In keeping with the general practice of reporting scientific observations, due acknowledgement has been made wherever the work described is based on the findings of other investigators.

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March 3, 2014

### CERTIFICATE

This is to certify that the work embodied in the thesis entitled "Molecular Electrostatics for Probing Hydrogen Bonds, Halogen Bonds and Lone Pair- $\pi$  Interactions and Design of Receptors for Lone Pair Bearing Molecules" has been carried out by Ms. Neetha Mohan under my supervision and guidance at the Inorganic and Theoretical Chemistry Section, Chemical Sciences and Technology Division, CSIR-National Institute for Interdisciplinary Science and Technology (CSIR-NIIST), Trivandrum and the same has not been submitted elsewhere for a degree. All the relevant corrections, modifications and recommendations suggested by the audience and the doctoral committee members during the pre-synopsis seminar of Ms. Neetha Mohan have been incorporated in the thesis.

(C. H. Suresh) Thesis Supervisor

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"For each new morning with its light, For rest and shelter of the night, For health and food, for love and friends, For everything Thy goodness sends."

Ralph Waldo Emerson

Neetha Mohan

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AIM	: Atoms in Molecules	
BCP	: Bond Critical Point	
BSSE	: Basis Set Superposition Error	
CAHB	: Charge-Assisted Hydrogen Bonds	
CC	: Coupled Cluster	
ССР	: Cage Critical Point	
CCSD	: Coupled Cluster Single and Double	
CI	: Configuration Interaction	
CSD	: Cambridge Structural Database	
DFT	: Density Functional Theory	
DNA	: Deoxyribonucleic Acid	
DZ	: Double Zeta	
ECHBM	: Electrostatic-Covalent Hydrogen Bond Model	
G09	: Gaussian 09	
GGA	: Generalized Gradient Approximation	
GTO	: Gaussian-Type Orbitals	
HF	: Hartree-Fock	
НК	: Hohenberg-Kohn	
IPCM	: Isodensity Polarizable Continuum Model	
IUPAC	: International Union for Pure and Applied Chemistry	
LCAO	: Linear Combination of Atomic Orbital	
LDA	: Local-Density Approximation	
LSDA	: Local Spin Density Approximation	
MBPT	: Many Body Perturbation Theory	

MC	: Monte Carlo		
MED	: Molecular Electron Density		
MIPp	: Molecular Interaction Potential with Polarization		
MD	: Molecular Dynamics		
MESP	: Molecular Electrostatic Potential		
MM	: Molecular Mechanics		
МО	: Molecular Orbital		
MP	: Møller-Plesset Perturbation Theory		
ONIOM	: Our N-layered Integrated Molecular Orbital + Molecular Mechanics		
PCM	: Polarizable Continuum Model		
PES	: Potential Energy Surface		
QM	: Quantum Mechanics		
QSAR	: Quantitative Structure Activity Relationship		
RCP	: Ring Critical Point		
RAHB	: Resonance-Assisted Hydrogen Bonds		
RNA	: Ribonucleic Acid		
SCF	: Self Consistent Field		
SAPT	: Symmetry Adapted Perturbation Theory		
STO	: Slater-Type Orbitals		
UFF	: Universal Force Field		
XC	: Exchange Correlation		

## Preface

Noncovalent interactions, such as hydrogen bonds, halogen bonds and lone pair- $\pi$  interactions are central to many areas of chemistry, molecular biology and materials science. A clear understanding of the nature and relative magnitude of noncovalent interactions is indispensable for the rational design of new molecules. Despite the overwhelming importance of noncovalent interactions, their quantification has been remained as a challenging task. Molecular electrostatic potential (MESP), a property amenable to experimental observation as well as theoretical calculation, has emerged as an efficient tool to understand, interpret and quantify weak interactions. The focus of this thesis is to develop MESP based approaches to probe hydrogen bonds, halogen bonds and lone pair/anion- $\pi$  interactions. Further, these insights are utilized to design molecular receptors for neutral and anionic molecules of chemical, biological and environmental relevance. The thesis is divided into four chapters.

The first part of Chapter 1 gives an overview of various noncovalent interactions and reviews the major concepts and principles that have emerged from this area. Computational chemistry is an exciting and fast-emerging field that has become crucial for most advances made in chemistry today. A brief account of various computational methods and their theoretical basis is presented in the second part of Chapter 1.

In Chapter 2, an electrostatics-based approach is proposed for probing the weak interactions between lone pair containing molecules and electron deficient  $\pi$ -systems. For electron-rich molecules, the negative minima in molecular electrostatic potential (MESP) topography give the location of electron localization and the MESP value at the minimum ( $V_{min}$ ) quantifies the electron rich character of that region. Interactive behavior of lone pair bearing molecules with electron deficient  $\pi$ -systems explored within DFT brings out good correlation of the lone pair- $\pi$  interaction energy with the  $V_{min}$  value of

the electron rich system. On the basis of the precise location of MESP minimum, a prediction on the orientation of a lone pair bearing molecule with an electron deficient  $\pi$ -system is possible.

The quantification and characterization of hydrogen bonds, halogen bonds and dihydrogen bonds using accurate *ab initio* and MESP approaches is presented in Chapter 3. The competence of M06L, MP2, MP4//M06L and MP4//MP2 methods for modeling accurate binding energies of noncovalent complexes featuring hydrogen bonds, halogen bonds and dihydrogen bonds is assessed. It is shown that unambiguous evidence for bond formation in hydrogen bonds, halogen bonds and dihydrogen bonds, halogen bonds and dihydrogen bonds. Compared to the electron density ( $\rho$ ) at the bond critical point-based analysis, the MESP data obtained at the bonded nuclei ( $V_n$ ) as well as the MESP minimum ( $V_{min}$ ) observed on the constituents of the bonded complexes are found to be effective for predicting the strength of all kinds of hydrogen bonds, halogen bonds and dihydrogen bonds. A good linear correlation obtained between a parameter based on  $V_n$  and bond strength strongly suggests that all such bonds arise from electron donor-acceptor (eDA) interactions.

Chapter 4 presents the rational design of bidentate ( $\mathbf{R}_{I}$ ), tridentate ( $\mathbf{R}_{II}$ ) and tetradentate ( $\mathbf{R}_{III}$ ) receptors capable of binding neutral molecules and anions predominantly through lone pair- $\pi$  and anion- $\pi$  interactions. The receptors are modeled in a stepwise manner by substituting the electron deficient core of hexafluorobenzene at 1, 3, and 5 positions with pentafluorobenzyl ( $C_6F_5CH_2$ -) groups. The tripodal platform of  $\mathbf{R}_{III}$  is used for the construction of a cage receptor ( $\mathbf{R}_{IV}$ ) which can form stable endohedral van der Waal's complexes with noble gas atoms and molecular hydrogen.

# Introduction

# Part A – Noncovalent Interactions & Part B – Computational Chemistry

# Part A – Noncovalent Interactions

# **1.1 An Overview of Noncovalent Interactions**

Atoms and molecules can interact together leading to the formation of either new molecules or molecular assemblies. The former which result from the partial overlap between hybrid atomic orbitals is termed covalent [Lewis 1923] while the latter which neither involves the formation or breaking of chemical bond is termed noncovalent interactions. Noncovalent interactions were first recognized in the last century by J. D. van der Waals who realized that the discrepancies between the state function of a real gas and ideal gas could be accounted for by the attractive forces existing between gas molecules [Müller-Dethlefs and Hobza 2000]. Liquefaction of helium by Kamerlingh Onnes [Onnes 1909] provided a most decisive argument about the existence of attractive intermolecular forces even between rare gas atoms such as helium which do not possess any charge or permanent electric multipole moment. Later in 1930, Frtiz London made fundamental step in understanding and interpreting these interactions using the principles of quantum mechanics [London 1930a]. Noncovalent interactions exist at much greater distances compared to covalent bonds; sometimes at more than 10 Å or even 100 Å in the case of some biomacromolecules [Hobza and Müller-Dethlefs 2010].

Noncovalent interactions are the main source of stability of many molecular complexes in chemistry, nanoscience and biology. The three dimensional structure and functions of biomacromolecules like DNA, RNA and proteins result from a delicate balance between various noncovalent interactions acting between biomolecular building blocks as well as between these molecules and their surrounding environment. Although weak relative to covalent interactions, it is the large number of these interactions that occur in biomolecules and supramolecular structures that make them functionally significant. To quote Nobel laureate Jean-Marie Lehn [Lehn 1995], "Noncovalent interactions define the inter-component bond, the action and reaction, in brief, the behavior of molecular individuals and populations". Despite the enormous progress made in experimental and theoretical techniques, an unambiguous description of noncovalent interactions is far from reality [Müller-Dethlefs and Hobza 2000].

The term "noncovalent" encompasses an enormous range of attractive and repulsive forces which range from coordinative bonds with a strength of several hundreds of kJ/mol to weak van der Waals interactions worth only a few kJ/mol. In the very broadest sense, noncovalent interactions include electrostatic interactions occurring between permanent multipoles such as charge-charge, charge-dipole, charge-multipole, multipole-multipole interactions, induction or polarization interactions between permanent and induced multipoles and dispersion interactions between instantaneous and induced multipoles. Charge-transfer, ionic and metallic interactions, hydrogen bonds, halogen bonds, dihydrogen bonds and lithium bonds are also subsumed under noncovalent interactions.  $\pi$ -systems also participate in noncovalent interactions and can interact favorably with cations, anions or other  $\pi$ -systems leading to cation- $\pi$ , anion  $\pi$  or  $\pi$ - $\pi$  stacking interactions. Hydrophobic interactions represent the tendency of nonpolar groups to associate in aqueous solutions and occur in low molecular weight organic molecules and biological macromolecules. Strongest among noncovalent interactions are ion-ion interactions (bond energies ranging from 100 - 350 kJ/mol) and the strength of these interactions depend on the distance between the charges and the extent of delocalization. Interactions between ions and dipoles (ion-dipole interactions) are weaker with bond energies in the range of 20 - 200 kJ/mol. Even weaker are dipole-dipole interactions with bond energies lying between 5 - 50 kJ/mol. Hydrogen bonds are highly directional noncovalent interactions with bond strength ranging from very weak (< 12 kJ/mol) to moderate (16 – 60 kJ/mol) and strong (60 – 120 kJ/mol) [Desiraju and Steiner

#### Chapter 1

2001]. The classification and strength ranges of accepted intermolecular noncovalent interactions are summarized in Table 1.1.

Interaction	Strength Range	Example
Ion-ion	100 - 350 kJ/mol	NaCl
Ion-dipole	20 - 200 kJ/mol	Coordination Bonds
Dipole-dipole	5 - 50 kJ/mol	$SO_2 + SO_2$
Hydrogen Bonding	4 - 120 kJ/mol	Water
Halogen Bonding	10 - 200 kJ/mol	Bromine 1,4-dioxanate
Cation- $\pi$ Interaction	5 - 80 kJ/mol	Na <sup>+</sup> channels
Anion- $\pi$ Interaction	4 - 120 kJ/mol	Hexafluorobenzene-F <sup>-</sup> complex
$\pi$ - $\pi$ stacking	0 - 50 kJ/mol	Benzene crystal structure
van der Waals	< 5 kJ/mol	Crystal close packing/charge balance
Hydrophobic Effects	No measurement	Oil and water

**Table 1.1** Important classes of noncovalent interactions and their strength ranges.

The thesis mainly focuses on hydrogen bonds, halogen bonds and anion- $\pi$  interactions which will be described in detail in the forthcoming sections.

## **1.1.1 Components of Noncovalent Interaction Energy**

Various intermolecular noncovalent forces can be broadly classified as shortrange forces that decrease exponentially with distance and long-range forces that vary as the inverse powers of distance. The total intermolecular interaction ( $E_{int}$ ) energy of noncovalent complexes is partitioned into five different energy contributions on the basis of perturbation theory *viz*. electrostatic, polarization, dispersion, charge-transfer and exchange-repulsion terms.

$$E_{int} = E_{ES} + E_{POL} + E_{EX} + E_{DIS} + E_{CT}$$
(Eq. 1.1)

where  $E_{ES}$ ,  $E_{POL}$ ,  $E_{EX}$ ,  $E_{DIS}$  and  $E_{CT}$  represent electrostatic, polarization, exchangerepulsion, dispersion and charge-transfer energies respectively. The relative contributions of each of these components vary for specific kinds of noncovalent interactions.

Electrostatic forces arise from the classical Coulombic interactions between the static charge distributions of two molecules. These forces can be either attractive or repulsive and includes the interactions of all permanent charges and multipoles such as charge-charge, charge-dipole, dipole-dipole, dipole-quadrupole, etc. The electrostatic force of interaction, F between two point charges  $q_1$  and  $q_2$  separated by a distance r can be described by Coulomb's Law as,

$$F = \frac{q_1 q_2}{4\pi \epsilon r^2}$$
 (Eq. 1.2)

where  $\varepsilon$  is the dielectric constant of the medium. The central multipole expansion [Hirschfelder *et al.* 1964] calculates the electrostatic potential, *V*(r) at point P at a distance r from the center of mass of any two point charges q<sub>1</sub> and q<sub>2</sub> as the sum of a finite series of charge-charge, charge-dipole, dipole-dipole, charge-quadrupole, dipolequadrupole, quadrupole-quadrupole interactions.

$$V(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \left( \frac{q}{r} + \frac{\mu_z \cos\theta}{r^2} + \frac{Q_{zz}(3\cos^2\theta - 1)}{2r^3} + \dots \right)$$
(Eq. 1.3)

where  $\mu_z$  is the dipole moment,  $Q_{zz}$  is the quadrupole moment and  $\theta$  is the angle which the point charge makes with the center of mass and the point P. Electrostatic interaction is directional and of long range diminishing slowly as r<sup>-1</sup> for charge-charge interactions, r<sup>-2</sup> for charge-dipole interactions, r<sup>-3</sup> for dipole-dipole and so on.

Polarization forces are highly non-additive, attractive forces arising from the deformation of the charge distribution of a nonpolar molecule by the external electric field generated by neighboring molecules possessing permanent dipole moment [Debye 1929]. The polarization component includes the interactions between all permanent

charges or multipoles and induced multipoles, such as dipole-induced dipole, quadrupole-induced dipole, etc. Polarization term is of long range and decrease faster with distance ( $r^{-4}$ ). The induced dipole moment  $\mu$  is given by

$$\mu = \alpha E \tag{Eq. 1.4}$$

where  $\alpha$  is the static polarizability and E is the electric field. The energy of interaction (E<sub>POL</sub>) between a dipole  $\mu$  and an electric field E is given by

$$E_{POL} = -\int_{0}^{E} \mu dE = -\frac{1}{2} \alpha E^{2}$$
 (Eq. 1.5)

Exchange interactions are short-range repulsive interactions of quantum chemical nature which originate from charge overlap and exchange effects. This interaction can be understood in terms of the Pauli principle which prohibits any two electrons in a system from having the same set of quantum numbers. The overlap of electron density distribution of the two interacting molecules causes a fall in electron density in the intermolecular region leading to repulsion between the incompletely shielded nuclei. Unlike for the covalent bond, where the electron density between subsystems having unpaired electrons increases in the bonding region, here the electron density increases in an antibonding region, which results in mutual repulsion. Exchange potential,  $E_{EX}$  is proportional to the square of the overlap integral,  $S_{ij}$  between orbitals of two molecules.

$$E_{EX} \propto S_{ij}^2$$
 (Eq. 1.6)

Dispersion interactions [Eisenschitz and London 1930; London 1930a; London 1930b] are less directionally specific, have a long-range character and are of vital importance in stacking interactions existing in biomacromolecules. The dispersion energy has its origin in quantum mechanics, and comes from the continuous fluctuation of charge distribution of molecules due to electron movement. The dispersion energy is proportional to the product of the polarizabilities of the subsystems and a sixth (or higher) power of reciprocal distance. Dispersion and exchange-repulsion terms are often

combined into "van der Waal's" contribution that can be approximately described by Lennard-Jones potential ( $E_{vdw} \sim Ar^{-12} - Br^{-12}$ ). Dispersion term has a distance dependence which decreases as  $r^{-6}$  while exchange-repulsion term increases sharply with reducing distance as  $r^{-12}$ . Charge-transfer interaction is caused by the charge transfer from the occupied molecular orbitals (MO) of monomer A to the vacant MO's of monomer B and from the occupied MO's of B to vacant MO's of A and the higher order coupled interactions. Charge-transfer term decreases faster, with an approximate distance dependence of  $e^{-r}$ .

## **1.1.2 Experimental Determination of Noncovalent Interactions**

Major efforts have been carried out to devise and employ experimental techniques to study the structure and dynamics of noncovalent clusters and to quantify noncovalent interactions. Scattering experiments, spectroscopic measurements, and Xray diffraction are some of the experimental techniques that are widely used to gather information about noncovalent interactions. Molecular structure, though not directly observable, can be determined by measuring the rotational constants. Microwave spectroscopy, a method of very high resolution optical spectroscopy, yield the three rotational constants and consequently the moment of inertia and the most probable structure of molecular clusters [Canagaratna et al. 1998; Townes and Schawlow 1975]. It is extensively employed for the study of noncovalent clusters including those bound by electrostatic and dispersion interactions. However, rotational constants cannot provide an unambiguous answer regarding the structure and geometry of noncovalently bound complexes. Far-infrared vibration rotation tunneling or FIR-VRT spectroscopy [Blake et al. 1991] is widely used in the study of transitions between vibration-rotation-tunneling states in molecular clusters with a resolution comparable to that of microwave spectroscopy. Pugliano and Saykally carried out the first detailed experimental study of water trimer using FIR-VRT spectroscopy and showed that water trimer exhibits a cyclic triangular structure [Pugliano and Saykally 1992]. Vibrational frequencies are directly

observable characteristics of noncovalent complexes and hence vibrational spectroscopy methods based on infrared absorption or Raman effect can provide information on the structure and strength of noncovalent complexes. Zero-electron kinetic energy (ZEKE) [Müller-Dethlefs et al. 1984a; Müller-Dethlefs et al. 1984b] photoelectron spectroscopy provides high accurate information of stabilization energies of noncovalent complexes. ZEKE spectroscopy has greatly contributed to improving the knowledge on (ro)vibronic structure of cationic molecular complexes, van der Waal's complexes like Benzene...Ar complexes and hydrogen bonded complexes of the type Phenol...H<sub>2</sub>O [Hobza and Müller-Dethlefs 2010]. Resonance-enhanced multiphoton ionization (REMPI) spectroscopy provides spectroscopic information on the excited states of neutral systems and is frequently applied to understand the structure and dynamics of molecular clusters. Zwier et al. [Dian et al. 2002a; Dian et al. 2002b], Mikami et al. [Patwari et al. 2001] and Kleinermanns et al. [Nir et al. 2001; Nir et al. 2002] have extensively employed IR-UV hole burning studies to understand the noncovalent interactions in molecules of biological interest in the gas phase. Molecular torsion balance experiments [Carroll et al. 2008] and chemical double mutant complex cycles [Cockroft and Hunter 2007] are of particular importance in the determination of the magnitude of  $\pi$ - $\pi$  interactions. Atomic force microscopy (AFM) has become a method of choice for obtaining actual images of molecules and the forces that hold them together. Very recently by Zhang and coworkers [Zhang et al. 2013] reported a realspace visualization of the formation of hydrogen bonding in 8-hydroxyquiline molecular assemblies on a Cu(III) substrate revealing weak O-H...O, C-H...O and C-H...N bonds using noncontact atomic force microscopy (NC-AFM). Accurate experimental determination of structure and energetics of noncovalent interactions still remains a challenge. The progress in the understanding of noncovalent interactions can be achieved only by close cooperation between experiment and theoretical methods.

## 1.1.3 Hydrogen Bonds

"The discovery of the Hydrogen Bond could have won someone the Nobel Prize, but it didn't" George A. Jeffrey, Wolfram Saenger, 1991.

## **1.1.3.1** Historical Background

The hydrogen bond is the most important of all directional intermolecular interactions operative in determining structure, dynamics and function of a vast number of chemical and biological systems. The hydrogen bond X-H...Y-Z is an attractive interaction in which the electropositive H atom intercedes between two electronegative species X and Y and brings them closer [Desiraju 2011]. The weak interactions between molecules containing hydroxyl groups were noted by Nernst in 1892 [Nernst 1892]. However, the first proper description of hydrogen bonding came only ten years later with the concept of "Nebenvalenz" (minor valence) and "innerekomplexsalzbildung" developed by Werner [Werner 1902] and Hantzsch [Hantzsch 1910] to describe interand intra- molecular hydrogen bonding. Alfred Werner proposed that ammonium salt has a configuration where a proton lies between the ammonia molecule and the ion. Intramolecular hydrogen bonds were suggested by Oddo and Puxeddu (with the name mesohydric form) in 1906 to explain the properties of some o-hydroxyazo derivatives of eugenol [Oddo and Puxeddu 1906]. Several years later Pfeiffer made a similar proposal of an intramolecular hydrogen bond or "inner Komplexsdzbindung" between hydroxyl and carbonyl functional groups in 1-hydroxyanthraquinone [Pfeiffer et al. 1913]. Moore and Winmill concurred with Werner and proposed a hydrogen bonded structure of undissociated trimethyl ammonium hydroxide, thus accounting for its slight dissociation compared to tetramethyl ammonium hydroxide [Moore and Winmill 1912]. In 1920 W. M. Latimer and W, H. Rodebush, recognized that the unusual properties of water and ice owe their existence to hydrogen bonds between water molecules [Latimer and Rodebush 1920]. They proposed that "[A] free pair of electrons on one water molecule might be able to exert sufficient force on a hydrogen held by a pair of electrons on another water molecule to bind the two molecules together.... Such an explanation amounts to saying that the hydrogen nucleus held between 2 octets constitutes a weak 'bond'." This description, based on the Lewis dot formalism, is the first to truly call this interaction a bond. Hydrogen bond was apparently quoted for the first time by Lewis in 1923 [Lewis 1923]. Pauling interpreted the structure of the [F:H:F]<sup>-</sup> ion and accounted for the residual entropy of ice using the concept of hydrogen bonding [Pauling 1931; Pauling 1935]. Since its discovery, hydrogen bonding interactions has continued to fascinate chemists and enormous theoretical and experimental efforts has been made to understand the phenomenon of hydrogen bonding. Huggins predicted the role and importance of hydrogen bond as early as in 1936: "... the most fruitful applications of hydrogen-bridge theory will be to a better understanding of the nature and behavior of complicated organic substances such as gels, proteins, starch, cellulose, sugars and other carbohydrates, chlorophyll, hemoglobin, and related substances, etc." [Huggins 1936]. The role of hydrogen bonding in the structure and function of biomolecules were brought out by the landmark papers of Pauling and Corey [Pauling and Corey 1950; Pauling et al. 1951] describing elements of protein structure viz. alpha helix and beta sheet and Watson and Crick [Watson and Crick 1953] discussing the structure of DNA double helix.

### **1.1.3.2** Definition of Hydrogen Bond

A number of definitions have been put forward for hydrogen bonds, the earlier one being the one proposed by Pauling in his book "The Nature of the Chemical Bond" according to which "[U]nder certain conditions an atom of hydrogen is attracted by rather strong forces to two atoms, instead of only one, so that it may be considered to be acting as a bond between them. This is called the hydrogen bond" [Pauling 1939]. Over the years, chemists have found a large variety of hydrogen bonding interactions that do not quite fit the classical definition by Pauling. A far-sighted early definition is that of Pimental and McClellan who in 1960, defined hydrogen bond as being "said to exist when 1) there is evidence of a bond, and 2) there is evidence that this bond specifically involves a hydrogen atom already bonded to another atom" [Pimentel and McClellan 1960]. As noted by Hobza and Havlas [Hobza and Havlas 2000], "the published definitions of the H-bond are not unambiguous and many exist." A task group of International Union for Pure and Applied Chemistry (IUPAC) has reviewed this topic in depth based on theoretical and experimental knowledge acquired over the past century and proposed a short modern definition for it [Arunan et al. 2011a; Arunan et al. 2011b]. According to the definition "The hydrogen bond is an attractive interaction between a hydrogen atom from a molecule or a molecular fragment X-H in which X is more electronegative than H, and an atom or a group of atoms in the same or a different molecule, in which there is evidence of bond formation".

The IUPAC task committee recommends some criteria useful as evidence and some typical characteristics for defining a particular weak interaction as a hydrogen bond. The six criteria proposed by the committee for a hydrogen bond X–H...Y–Z are:

- a) The forces involved in the formation of a hydrogen bond are those originating from electrostatics, charge-transfer and dispersion.
- b) The X–H covalent bond is polarized and the H...Y bond strength increase with the increase in electronegativity of X.
- c) Closer the X–H...Y angle to 180°, stronger is the hydrogen bond and shorter is the H...Y distance.

- d) Hydrogen bond formation usually leads to an increase in the length of the X–H bond leading to a red shift in the infrared X–H stretching frequency and an increase in the infrared absorption cross-section for the X–H stretching vibration. The greater the lengthening of the X–H bond in X–H…Y, the stronger is the H…Y bond. Simultaneously, new vibrational modes associated with the formation of the H…Y bond are generated.
- e) Hydrogen bond formation leads to characteristic NMR signatures that typically include pronounced proton deshielding for H in X–H, through hydrogen bond spin-spin couplings between X and Y, and nuclear Overhauser enhancements.
- f) For a hydrogen bond to be detected experimentally, the Gibbs energy of formation for the hydrogen bond should be greater than the thermal energy of the system.

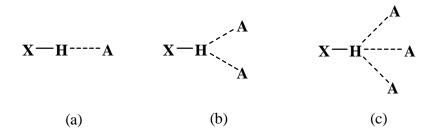
The typical characteristics of hydrogen bonds listed by the IUPAC committee are:

- (a) The  $pK_a$  of X–H and  $pK_b$  of Y–Z correlate strongly with the energy of the hydrogen bond formed between them.
- (b) Hydrogen bonds are considered as the partially activated precursors in protontransfer reactions (X−H...Y → X...H−Y).
- (c) Hydrogen bonding networks show cooperativity, leading to deviations from pair wise additivity in hydrogen bond properties.
- (d) Hydrogen bonds show directional preferences and influence packing modes in crystal structures.
- (e) Interaction energy of hydrogen bond correlates well with the extent of charge transfer between the donor and the acceptor.

(f) Analysis of the electron-density topology of hydrogen bonded systems usually shows a bond path connecting H and Y and a (3, -1) bond critical point between H and Y.

# **1.1.3.3** Types of Hydrogen Bonds

The term hydrogen bond includes a broad spectrum of interactions and the term "hydrogen bridge" [Desiraju 2002] is meaningfully used in literature to represent the different types of hydrogen bonds. In a normal hydrogen bond, the donor atom interacts with a single acceptor. A donor can interact with two or three acceptors simultaneously resulting in bifurcated (three-center) and trifurcated hydrogen (four-center) bonds respectively, as illustrated in Figure 1.1.



**Figure 1.1** (a) Normal hydrogen bond with one acceptor, (b) bifurcated hydrogen bond and (c) trifurcated hydrogen bond.

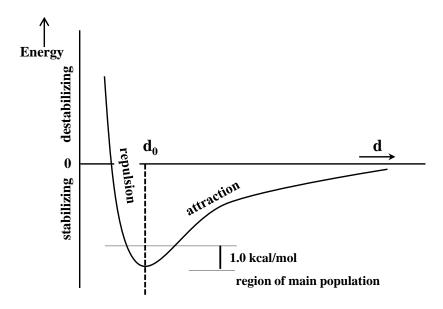
More than one hydrogen bond can be formed at once resulting in multiple hydrogen bonding interactions. For example Adenine-Thymine base pair in DNA exhibits two intermolecular hydrogen bonds whereas Guanine-Cytosine base pair is characterized by three hydrogen bonds. The hydrogen bond donor and hydrogen bond acceptor can belong to the same molecule or different molecules; the former is termed intramolecular hydrogen bond and the latter is intermolecular hydrogen bond. Intramolecular hydrogen bonds are necessarily bent whereas intermolecular hydrogen bonds are linear or nearly linear. Hydrogen bonds can also be classified based on the nature of donor and acceptor molecules as conventional and unconventional hydrogen bonds. Conventional hydrogen bonds have electronegative atoms O, N and Cl as proton acceptors and hence O-H...O, N-H...N, N-H...O, N-H...Cl and other similar systems are considered to be conventional hydrogen bonds. Carbon atoms or  $\pi$ -electrons can form hydrogen bonds and such bonds C–H...Y and X–H... $\pi$  are unconventional. Hydrogen bonds can be red-shifting or blue-shifting depending on the X-H stretching frequencies of the proton donor groups. The formation of a hydrogen bond X–H...Y–Z, according to the conventional definition, is accompanied by the weakening of the covalent X–H bond with a concomitant red-shift or decrease in the X–H stretching frequency. Such hydrogen bonds are red-shifting hydrogen bonds. The red-shift of the X-H stretch vibration is regarded as the "signature of hydrogen bonding" [Allerhand and Schlever 1963] and is the basis for several structural, spectroscopic and thermodynamic techniques for the detection of hydrogen bonding. Hobza and Špirko established the existence of a new type of hydrogen bond called improper blue-shifting hydrogen bonds in benzene dimers and other benzene complexes characterized by the strengthening of the X-H covalent bond and blue-shift in the X-H stretching frequency [Hobza et al. 1998]. Alabugin and coworkers showed that the structural reorganization of X-H bond in red-shift and blueshift hydrogen bonds arise from a balance of hyperconjugative bond weakening and rehybridization bond strengthening [Alabugin et al. 2003]. Jemmis et al. suggested that the nature of the electron density distribution resulting from the electron affinity of atoms involved in the hydrogen bond donor predetermines it toward proper or improper hydrogen bonds [Joseph and Jemmis 2007]. Gilli et al. proposed the three types of strong hydrogen bonds where the hydrogen bond strength is enhanced by adding an electron, withdrawing an electron, or by resonance [Gilli and Gilli 2000; Gilli and Gilli 2009a; Gilli et al. 2009b]. These are charge-assisted hydrogen bonds, (+) CAHB and (-) CAHB and resonance-assisted hydrogen bonds (RAHB) respectively. CAHBs involve ionic groups and are more strong compared to those found in neutral systems. In RAHBs, the enhancement of hydrogen bond strength is the result of  $\pi$ -electron delocalization.

Crabtree and coworkers introduced the concept of dihydrogen bonds to explain the unconventional hydrogen bonds established between metal hydrides and proton donor like O–H or N–H [Crabtree *et al.* 1996]. A dihydrogen bond is represented as M–H...H– Y where M is a metal which is less electronegative than H (usually Boron or transition metals) and Y is an electronegative element. Mikami and coworkers first reported dihydrogen bonding in the gas phase [Patwari *et al.* 2002]. The presence of one electron hydrogen bond has been revealed from both experimental [Merritt *et al.* 2006] and theoretical calculations [Alkorta *et al.* 1998] where the C atom in CH<sub>3</sub> radical acts as the acceptor. Very recently, Mani and Arunan [Mani and Arunan 2013] proposed 'carbon bond' (C...Y) analogous to hydrogen and halogen bonds wherein the tetrahedral face of CH<sub>3</sub> interacts with the negative centers of molecules like H<sub>2</sub>O, H<sub>2</sub>S and NH<sub>3</sub>.

## **1.1.3.4** Strength and Nature of Hydrogen Bonds

Hydrogen bonds exhibit a continuum of strengths depending on the nature of the donor and acceptor groups; weakest hydrogen bonds are hardly distinguishable from van der Waals interaction and strongest ones are stronger than the weakest covalent bonds [Desiraju and Steiner 2001]. The energy of hydrogen bonds lies in the range of 0.5 to 40 kcal/mol. Hydrogen bonding interactions in solid, liquid and gaseous states are classified as strong, moderate and weak based on the strength of the interactions and different geometrical and spectral criteria [Jeffrey 1997]. For weak hydrogen bonds, the strength falls in the range of < 1 to 4 kcal/mol. The strength of moderate and strong hydrogen bonds ranges between 4 to 15 kcal/mol and 15 to 40 kcal/mol respectively. The schematic representation of the hydrogen bond potential for any particular donor-acceptor combination is shown in Figure 1.2 [Desiraju and Steiner 1999]. The distance

profile of the potential energy indicates that the energy is lowest at the equilibrium distance  $d_0$  is negative for all distances  $d > d_0$  and is positive only for very short distances. The zero-energy line separates attractive (or stabilizing with energy E < 0) and repulsive (or destabilizing with energy E > 0) interactions. Every donor-acceptor combination of hydrogen bonds has its own potential energy curve with the minimum being deeper and shifted to shorter distances for stronger combinations. Figure 1.2 shows that a stabilizing interaction is associated with a repulsive force if it is shorter than the equilibrium distance.



**Figure 1.2** Schematic representation of typical hydrogen bond potential.  $d_0$  is the equilibrium distance and d is the hydrogen bond length. Negative and positive bond energies are indicated by the terms stabilizing and destabilizing respectively. Figure adapted from [Desiraju and Steiner 1999].

Hydrogen bond is a complex interaction that has contributions from electrostatic (acid/base) interactions, polarization (hard/soft) effects, van der Waals (dispersion/repulsion and electron correlation) interactions and covalency (charge transfer) terms. The contributions from each term vary depending on particular donor-acceptor combination and the geometry of the hydrogen bonded complex. Different

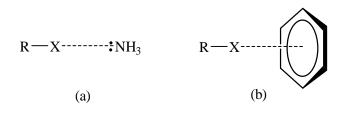
energy decomposition schemes are employed for decomposing the hydrogen bond energy into the constituent energy terms. One of the first decomposition schemes was proposed by Kollman and Allen [Kollman and Allen 1970; Kollman and Allen 1972]. Most popular partitioning modes follow the Morokuma and Kitara decomposition scheme where the interaction energy is calculated within the Hartree-Fock one-electron approximation [Kitaura and Morokuma 1976; Morokuma 1977]. Umeyama and Morokuma analyzed different hydrogen bonded systems and proposed that the energy components of hydrogen bonds are totally distance dependent [Umeyama and Morokuma 1977]. For any hydrogen bonded complex, the long-range electrostatic term dominates over the short range charge-transfer and polarization terms at larger distances whereas the attractive electrostatic, charge-transfer and polarization terms compete with large repulsive exchange-repulsion term at relatively small distances [Desiraju 2002; Steiner 2002]. Although electrostatic contribution is the dominant factor responsible for classical hydrogen bonding, pronounced covalent character is observed in strong hydrogen bonds and the dominance of dispersive interactions is found in weak hydrogen bonds. Gilli et al. proposed an electrostatic-covalent hydrogen bond model (ECHBM) based on the systematic analysis of structural and spectroscopic data of a large number of O-H...O-H bonds [Gilli and Gilli 2000]. According to this model weak hydrogen bonds are electrostatic in nature. As the strength of the interaction increases, the covalent character of the bond also increases, and very strong hydrogen bonds are actually three-center fourelectron covalent bonds. Desiraju claimed that the stronger hydrogen bonds are characterized by significant charge transfer from the acceptor to proton donating bond whereas weaker hydrogen bonds are mostly electrostatic in nature [Desiraju 2002]. Grabowski et al. characterized the covalent nature of interactions within various hydrogen bonded molecular aggregates and pointed out that the delocalization and

electrostatic interaction energy are the most important attractive terms for hydrogen bond

interactions [Grabowski 2011; Grabowski *et al.* 2006]. As the interaction becomes stronger, the ratio between the delocalization and electrostatic interaction energy terms increases.

# **1.1.4 Halogen Bonds**

A halogen bond, R–X...Y–Z is a highly directional, electrostatically-driven noncovalent interaction between a covalently bonded halogen atom X in one molecule and a negative site Y in another molecule [Politzer *et al.* 2010]. R–X is the halogen bond donor and Y–Z is the halogen bond acceptor; X is a halogen atom with an electrophilic region (chlorine, bromine, iodine and astatine) and the strength of the interaction increases in the order Cl < Br < I. R can be another halogen atom or a large organic or inorganic residue and Y is often an atom such as oxygen, nitrogen or sulfur, that has a lone pair or  $\pi$ -electron of an unsaturated system (Figure 1.3).



**Figure 1.3** Halogen bonding between R–X and (a) lone pair of NH<sub>3</sub> and (b)  $\pi$ -electrons of benzene.

The first reports of halogen acting as the Lewis acid came in the nineteenth century with the description of the complexes of  $Cl_2$ ,  $Br_2$  and  $I_2$  with Lewis bases such as ammonia and methylamines [Guthrie 1863; Prescott 1896; Remsen and Norris 1896]. More than 50 years later Benesi and Hildebrand reported the first cases of intermolecular donor acceptor complexes between iodine and aromatic hydrocarbons [Benesi and Hildebrand 1949]. The quantum mechanical theory of complex resonance that explained halogen bonding as a charge-transfer interaction was developed by Mulliken [Mulliken

1952] and Flurry [Flurry 1965; Flurry 1969]. Odd Hassel provided the detailed physical descriptions of the interactions in the mid-20<sup>th</sup> century from the crystal structures of molecular halogens in the complexes with organic bases and proposed that charge transfer from electron donors (Lewis bases) to electron acceptors (iodine or bromine) was responsible for these interactions [Hassel 1970; Hassel and Stromme 1958a; Hassel and Stromme 1958b]. The term "halogen bond" was first used by Dumas et al. in the context of experimental studies of complexes formed by CCl<sub>4</sub>, CBr<sub>4</sub>, SiCl<sub>4</sub> and SiBr<sub>4</sub> with tetrahydrofuran, tetrahydropyran, pyridine, anisole and di-n-butyl ether in organic solvents [Dumas et al. 1978]. The importance of halogen bonding in supramolecular selfassembly phenomena was stressed by Hassel [Hassel 1970] while the survey of Protein Data Bank (PDB) by Auffingeret al. in 2004 revealed the significance of such interactions in the crystal structures of biomolecular systems [Auffinger et al. 2004]. Extensive surveys of crystallographic data by Murray-Rust et al. to identify and characterize short intermolecular contact distances within the lattices of crystalline sulfides and halides revealed they show distinct patterns of attractive noncovalent interactions [Murray-Rust and Motherwell 1979; Murray-Rust et al. 1983]. Close contacts of halogens with electrophiles such as metal ions occur at angles 90° to 120° with the C-X bond whereas with nucleophiles such as oxygen and nitrogen, the angles were between 160° to 180° *i.e.*, along the extensions of the covalent bonds to the halogens (Figure 1.4). Such directed, near-linear interactions of halogens with nucleophiles came to be known as halogen bonds. The existence of halogen bonds initially appeared surprising and counterintuitive since both halogen atoms and halogen bond acceptors (Y) are electronegative and are typically viewed as being negatively charged.

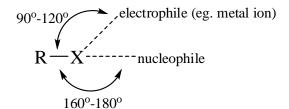
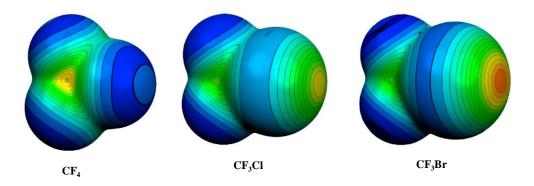


Figure 1.4 Directional tendencies of close contacts in crystalline halides.

Politzer and coworkers [Clark et al. 2007; Murray et al. 1994; Politzer et al. 2013] provided an advanced explanation of halogen bonding based on the concept of  $\sigma$ hole. Molecular electrostatic potential studies by Brinck et al. showed that in H<sub>3</sub>C-Br, CBr<sub>4</sub> and CCl<sub>4</sub>, the halogen atom have areas of positive electrostatic potential on the outer portion of their surfaces while the lateral sides of the halogen have negative potential [Brinck et al. 1992; Brinck et al. 1993]. This is because the half-filled p<sub>z</sub> orbital of halogen participates in the covalent R-X bond and this depletes the electron density in the outer lobe of the  $p_z$  orbital. The four  $p_x$  and  $p_y$  electrons create a belt of negative potential around the sides of the halogens thus permitting the interactions with electrophiles. Politzer *et al.* suggested the term ' $\sigma$ -hole' to denote this positive halogen surface region and suggested that halogen bond is an electrostatically-driven attractive interaction between a positive  $\sigma$ -hole on a covalently-bonded halogen atom and a negative site. The presence and magnitude of  $\sigma$ -hole depends on the halogen and the electron-withdrawing power of the remainder of the molecule. More electronegative halogens, F and Cl, attract enough electronic charge from the R portion of R-X molecule and hence their  $\sigma$ -holes have a negative potential although less negative than the lateral sides of the halogen. Thus the halogen surfaces are entirely negative for H<sub>3</sub>CF, H<sub>3</sub>CCl and CF<sub>4</sub>. Molecular electrostatic potential plots of CF<sub>4</sub>, CF<sub>3</sub>Cl and CF<sub>3</sub>Br are shown in Figure 1.5 to demonstrate the concept of  $\sigma$ -hole. The fluorine hemispheres are negative for CF<sub>4</sub>. However when a chlorine or bromine is substituted,  $\sigma$ -hole develops on the outermost portion of its surface, around its intersection with the C-Cl axis. The  $\sigma$ -hole on the bromine is progressively larger and more positive than chlorine.



**Figure 1.5** Molecular electrostatic potential at 0.001 au isodensity surface of  $CF_4$ ,  $CF_3Cl$  and  $CF_3Br$  showing  $\sigma$ -hole. Color coding, **blue** -0.009 au to red 0.054 au. Figure adapted from [Clark *et al.* 2007].

It has been shown that covalently bonded atoms of Group IV, Group V and Group VI exhibit  $\sigma$ -hole interactions [Politzer *et al.* 2013]. Frontera and coworkers [Bauzá *et al.* 2013] used tetrel bonding to refer to noncovalent interactions between electron donors and the group 14 elements, silicon, germanium and tin. Tetrel bonds have comparable strength to hydrogen bonds and other  $\sigma$ -hole-based interactions, are highly directional, and are expected to be valuable in crystal engineering, supramolecular chemistry, and catalysis.

Various theoretical and experimental studies have pointed out the intriguing similarities between halogen bonds and hydrogen bonds. Metrangolo and coworkers demonstrated the striking parallelism between the spectroscopic, energetic and geometric features of hydrogen bonds and halogen bonds [Metrangolo *et al.* 2005]. Quite recently it has been demonstrated that halogen bonded systems can also exhibit blue shifts as well as red shifts similar to hydrogen bonded systems [Murray *et al.* 2008; Wang *et al.* 2004]. Legon discussed the parallelism in detail and pointed out that the hydrogen bond is more likely to be nonlinear [Legon 1999; Legon 2008; Legon 2010]. Halogen bonds are found

to be more sensitive to steric hindrance due to the larger size and polarizability of halogens compared to hydrogen. Di Paolo and Sandorfy found that the infra-red bands due to solute-solvent hydrogen bonds can be significantly reduced by the introduction of a co-solute that can halogen bond with the solvent [Di Paolo and Sandorfy 1974]. Some compounds capable of co-crystalizing with both halogen bond donors and hydrogen bond donors will do so preferentially with the former [Corradi *et al.* 2000].

IUPAC recommendations 2013 [Desiraju *et al.* 2013] has proposed a definition for halogen bond which stated that "A halogen bond R–X...Y–Z occurs when there is evidence of a net attractive interaction between an electrophilic region on a halogen atom X belonging to a molecule or a molecular fragment R–X (where R can be another atom, including X, or a group of atoms) and a nucleophilic region of a molecule, or molecular fragment, Y–Z." Some features useful as indications for the halogen bond, are also listed:

- a) The distance between the donor halogen atom X and the acceptor atom Y tends to be less than the sum of the van der Waals radii of X and Y.
- b) The angle R–X...Y tends to be linear (180°) and the halogen atom X tends to align with the direction of the axis of the *n*-lone pair on Y or the  $\pi$ -bond electron pair in Y–Z.
- c) Halogen bond formation is usually accompanied by an increase in the length of the R-X covalent bond.
- d) The strength of the halogen bond decreases with an increase in the electronegativity of X and/or decrease with the electron withdrawing ability of R.
- e) The forces involved in the formation of the halogen bond are primarily electrostatic (including polarization) and dispersion and the relative roles of the different forces may vary from one case to the other.
- f) The analysis of the electron density topology of halogen bond usually shows a bond critical point and a bond path connecting X and Y.

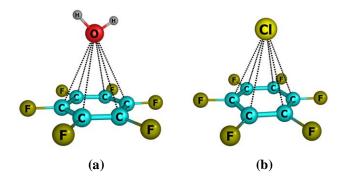
- g) Halogen bond formation is associated with the formation of new vibrational modes, changes in the IR, Raman absorptions and NMR signals of R-X and Y-Z and blue shifts in the UV visible spectrum of the halogen bond donor.
- h) The halogen atom X may participate in more than one halogen bond.
- The halogen bond may be involved in halogen transfer reactions or other reactive phenomena.

Different energy decomposition schemes have been employed to decompose the interaction energy of halogen bonds into their plausible components [Lommerse et al. 1996; Riley and Hobza 2008; Riley et al. 2009; Wang et al. 2007]. These studies have shown that there are five main energetic contributions to halogen bonding viz. electrostatic, polarization, dispersion, exchange-repulsion, and charge-transfer. The physical meaning of the contributions to the interaction energy is different for various schemes, with each scheme giving different weight for each component. Several studies have shown that electrostatic contribution is the major attractive contribution of halogen bonding interactions [Riley and Hobza 2008]. However, in a recent study Palusiak showed that the orbital interaction accounting for charge-transfer and the polarization are the most important factors responsible for the stability of halogen bonded complexes [Palusiak 2010]. Riley and Hobza pointed dispersion component has significant contribution to the total interaction energy of halogen bonds [Riley and Hobza 2008; Riley et al. 2013]. Politzer and coworkers provided strong evidence for the significance of electrostatic contribution from a detailed analysis of the nature of halogen bonds [Politzer et al. 2013]. They showed that the strength of halogen bond correlates with the positive potential of the halogen, for a given Lewis base involved in the halogen bond interaction. Using the natural energy decomposition analysis (NEDA) scheme of the interaction energy Grabowski showed that polarization is the most important attractive term in the interaction energy with significant contributions from electrostatic and charge transfer terms [Grabowski 2013].

There is mounting evidence of the significance of halogen bonds in biological systems in ligand binding, recognition, conformational stabilization, molecular folding and drug design [Auffinger et al. 2004]. Auffinger et al. reported several interesting cases of halogen bonding in a survey of halogenated proteins and nucleic acids in the Protein Data Bank, including a strong interaction involving 5-bromouracil that stabilized a Holliday junction [Auffinger et al., 2004]. Halogen bonds are found to direct ligandprotein binding, including the recognition of naturally iodinated thyroid hormones by their cognate proteins. Voth *et al.* reported that DNA junctions are stabilized more by halogen bonds than by hydrogen bonds [Carter et al. 2013; Voth et al. 2007]. Halogen bonding also finds potential applications in medicinal chemistry where halogen atoms are used as important inhibitors of proteins including those involved in carcinogenesis [Voth and Ho 2007]. The iodinated inhibitor designed to target the mitogen activated protein kinase (MEK) and a chlorinated inhibitor to the CDC2-like kinase isoform 1 (CDK1) reinforce the significance of halogen bonds in conferring specificity of inhibitors against protein kinases. Thus exploiting halogen bonding offers remarkable possibilities for the design and developments of new compounds and materials with probable applications in chemistry, biology and medicine [Politzer et al. 2010].

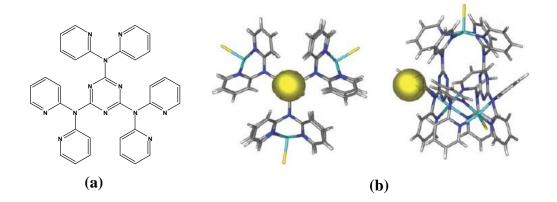
# **1.1.5** Lone Pair- $\pi$ and Anion- $\pi$ Interactions

Lone pair- $\pi$  and anion- $\pi$  interactions are two interaction types involving aromatic rings that have been added recently to the world of noncovalent interactions. Lone pair- $\pi$ or anion- $\pi$  interactions are defined as the favorable attractive interactions between the lone pairs of neutral molecules or anions and electron deficient  $\pi$ -electron systems of aromatic rings [Hernández-Trujillo and Vela 1996; Laidig 1991]. Schneider *et al.*  reported weak but attractive interactions between negative charges and polarizable aryl parts of host-guest systems in the early 1990s [Schnieder *et al.* 1993]. Pioneering theoretical investigations by Alkorta and coworkers in 1997 revealed the favorable nature of the interaction between  $\pi$ -cloud of hexafluorobenzene (C<sub>6</sub>F<sub>6</sub>) and several small electron-donor molecules (FH, HLi, :CH<sub>2</sub><sup>-</sup>, HCN, and HNC) on the basis of their electron density and molecular electrostatic potential maps [Alkorta *et al.* 1997]. Gallivan and Dougherty in 1999 demonstrated the significant binding interaction between water and hexafluorobenzene in a geometry where in the oxygen lone pairs points directly into the face of the  $\pi$ -system and suggested that these interactions mainly arise due to attractive electrostatic forces [Gallivan and Dougherty 1999]. This was followed by numerous theoretical reports on lone pair and anion- $\pi$  interactions [Alkorta *et al.* 2002; Mascal *et al.* 2002; Quiňonero *et al.* 2002a; Quiňonero *et al.* 2002b]. Figure 1.6 shows the lone pair- $\pi$  and anion- $\pi$  interactions in C<sub>6</sub>F<sub>6</sub>-H<sub>2</sub>O and C<sub>6</sub>F<sub>6</sub>-Cl<sup>-</sup> complexes.



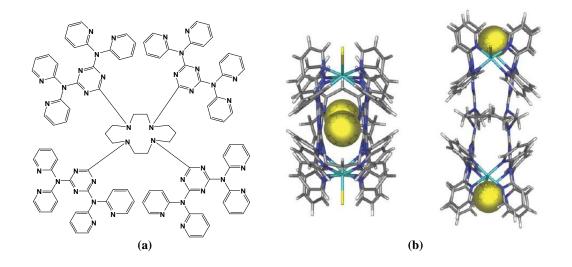
**Figure 1.6** Lone pair- $\pi$  and anion- $\pi$  interactions. (a) Lone pair- $\pi$  complex between hexafluorobenzene and water (b) Anion pair- $\pi$  complex between hexafluorobenzene and chloride ion.

The first experimental proof for lone pair/anion- $\pi$  interactions was provided independently in 2004 by Meyer *et al.* and Reedijk *et al.* [De Hoog *et al.* 2004; Demeshko *et al.* 2004]. Meyer *et al.* reported the attractive interaction between chloride ions and triazine in the large electron deficient ligand hexakis(pyridine-2-yl)-[1,3,5]- triazine-2-4-6-triamine (L1), complexed with Cu(II) chloride to afford  $[(L1)_2(CuCl)_3][CuCl_4][Cl]$ . One of the  $[Cl]^-$  counter ion establish an anion- $\pi$  interaction with a triazine ring of L1 (Figure 1.7). The contact distance and angle of the anion to the ring centroid (3.11 Å and 88° respectively) are close to the theoretically predicted values by Mascal *et al.* [Mascal *et al.* 2002] and Deya *et al.* [Quiňonero *et al.* 2002b].



**Figure 1.7** Anion- $\pi$  interaction reported by Meyer and coworkers. (a) Schematic drawing of hexakis(pyridine-2-yl)-[1,3,5]-triazine-2-4-6-triamine (L1); (b) Front view and side view of {[(L1)<sub>2</sub>(CuCl)<sub>3</sub>][Cl]}<sup>2+</sup>. Atom colors: C = grey, H = white, N = dark blue, Cu = light blue and Cl = yellow. Figure adapted from [Demeshko *et al.*, 2004].

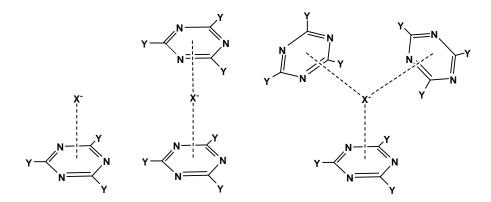
Reedijk and coworkers demonstrated the attractive interactions between Cl<sup>-</sup> and pyridine in a remarkable supramolecular system involving the dendritic octadentate ligand N,N',N",N"'-tetrakis{2,4-bis(di-2-pyridylamino)-1,3,5-triazinyl}-1,4,8,11tetraazacyclotetradecane (L2) coordinated to Cu(II) chloride to afford the ternuclear complex [Cu<sub>4</sub>(L2)Cl<sub>4</sub>][Cl]<sub>4</sub>(H<sub>2</sub>O)<sub>13</sub>(Figure 1.8). This complex has 16 pyridinyl rings of L2 coordinated to four different Cu(II) ions and two Cl<sup>-</sup> ions are encapsulated in two different cavities formed by pyridinyl rings through anion- $\pi$  interactions. This study prompted Reedijk *et al.* to design new triazine-based ligands and relevant systems with anion- $\pi$  interactions [De Hoog *et al.* 2004].



**Figure 1.8** Anion- $\pi$  interaction reported by Reedijk and coworkers. (a) Schematic drawing of N,N',N'',N'''-tetrakis{2,4-bis(di-2-pyridylamino)-1,3,5-triazinyl}-1,4,8,11-tetraazacyclotetradecane (L2), (b) Crystal structure of [Cu<sub>4</sub>(L2)Cl<sub>4</sub>][Cl]<sub>4</sub>(H<sub>2</sub>O)<sub>13</sub> from two different views. Atom colors: C = grey, H = white, N = dark blue, Cu = light blue and Cl = yellow. Figure adapted from [De Hoog *et al.*, 2004].

Reedijk and coworkers carried out a comprehensive examination of CSD and reported that an ion- $\pi$  contacts are quite common supramolecular bonding interactions in solid-state structures [Mooibroek et al. 2008]. Markedly different conclusions were drawn by Hay and Custelcean in 2009 after an exhaustive statistical analysis of anionarene contacts in the CSD and they concluded that genuine examples of anion- $\pi$ interactions with uncharged arenes are extremely rare in crystal structures [Hay and Bryantsev 2008]. CSD analyses [Hay and Custelcean 2009], spectroscopic studies [Chiavarino et al. 2009; Schneider et al. 2007] and several ab initio calculations [Berryman et al. 2007; Hay and Bryantsev 2008; Mascal et al. 2002] have revealed that in complexes of anions with neutral six-member aromatic rings the anion is likely to engage in any C-H hydrogen bonding interactions than an ion- $\pi$ interactions. Devà and coworkers studied anion- $\pi$ , anion- $\pi_2$  and anion- $\pi_3$  complexes of 1,3,5-triazine and trifluoro-1,3,5-triazine with Br and Cl ions using ab initio

calculations and demonstrated the additivity in both binding energies and geometries of anion- $\pi$  interactions (Figure 1.9) [Garau *et al.* 2005]. The synergetic effect of anion- $\pi$ , cation- $\pi$  and  $\pi$ - $\pi$  interactions has been demonstrated by Deyà and coworkers by means of high level *ab initio* calculations coupled with "atoms in molecules" theory and molecular interaction potential with polarization (MIPp) method [Garau *et al.* 2006].



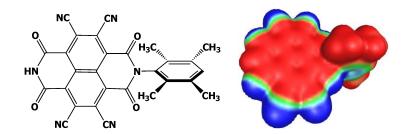
**Figure 1.9** Anion- $\pi$  complexes of 1,3,5-triazine and trifluoro-1,3,5-triazine with multiple anion- $\pi$  interactions per anion. (X = Br<sup>-</sup> or Cl<sup>-</sup> and Y = H or F).

Elegant studies by Deyà and coworkers revealed that anion- $\pi$  interactions are dominated by electrostatic and anion induced polarization contributions [Garau *et al.* 2003a; Quiňonero *et al.* 2002b]. Topological analysis of electron density in anion- $\pi$ interactions show that strong correlation exists between the permanent quadrupole moment,  $Q_{zz}$  of the electron deficient aromatic ring and the electrostatic component of the interaction energy [Garau *et al.* 2003a]. It has been shown that anion-induced polarization correlates with the molecular polarizability of the aromatic compound. Molecules with small magnitudes of  $Q_{zz}$  can exhibit a dual behavior by binding both cations and anions [Garau *et al.* 2004]. Garau *et al.* established that even non-electron deficient aromatic rings are capable of exhibiting anion- $\pi$  interactions if the ring is interacting simultaneously with a cation on the opposite face of the ring [Garau *et al.* 2003b]. Symmetry adapted perturbation theory (SAPT) studies by Kim and coworkers on anion- $\pi$  complexes revealed that the major attractive contributions to the total interaction energy are due to electrostatic and induction energies [Garau *et al.* 2004; Kim *et al.* 2004]. They also showed that total interaction energy has significant contributions from dispersion and exchange-repulsion energies.

Egli and coworkers provided crystallographic evidence for the stabilizing influence of sugar O4' lone pair- $\pi$  (nucleobase) intramolecular interactions in DNA [Berger and Egli 1997; Berger *et al.* 1996; Egli and Gessner 1995]. They also reported the role of attractive lone pair- $\pi$  interactions in the conformational stability of Z-DNA at high ionic strength despite poor base pair stacking. A high-resolution X-ray structure analysis showed the existence of lone pair- $\pi$  interactions between water molecules and functionally important unstacked residues in the 1.25 Å crystal structure of the ribosomal frameshifting RNA pseudoknot from beet western yellow virus [Sarkhel *et al.*, 2003]. Sankararamakrishnan and coworkers systematically analyzed 500 highresolution protein structures and identified 286 examples which show  $\pi$ ... $\pi$  and/or lonepair... $\pi$  interactions indicating that such interactions could stabilize secondary structures of proteins [Jain *et al.* 2007]. The presence of relevant anion– $\pi$  interactions in the active site of the urate oxidase enzyme has been reported by Deyà and coworkers [Estarellas *et al.* 2011].

Anion/lone pair- $\pi$  interactions holds great promise for the design of colorimetric sensors, selective anion receptors, hosts or scaffolds and catalysts of chemical and biological significance [Chifotides and Dunbar 2013]. Matile *et al.* reported synthesis and of an unprecedented synthetic ion channel based on  $\pi$ -acidic oligo-(para-phenylene)-N,N-naphthalenediimide (O-NDI) rods as transmembrane chloride  $\pi$ -slides and showed that the gradient of electron deficiency in these oligomers can be exploited to transfer anions through membranes [Matile and Mareda 2009]. The N,N-naphthalenediimide

(NDI) building unit exhibits an electron deficient character at the center of the molecule (Figure 1.10).



**Figure 1.10** N,N-naphthalenediimide unit and its DFT computed electrostatic potential map demonstrating the electron deficient character. Color coding, **blue** -0.02 au to red 0.02 au. Figure adapted from [Mohan *et al.* 2013].

Wang and coworkers demonstrated that the anion- $\pi$  interaction motifs can be used in the design of receptors for ion pair recognition by synthesizing oxacalix[2]arene[2]triazine azacrown based dipotic receptor molecules that binds to ion pairs through anion- $\pi$  interactions [Chen *et al.* 2011]. Experimental and theoretical calculations by Matile and coworkers showed that anion- $\pi$  interactions can contribute to catalysis [Zhao *et al.* 2014]. They showed that the stabilization of anionic transition states in Kemp elimination increases with the  $\pi$ -acidity of the catalysts.

With the development of experimental and theoretical techniques, the realm of weak noncovalent interactions is expanding continuously with many non-conventional interactions being reported and analyzed.

# Part B – Computational Chemistry

"Everything that living things do can be understood in terms of the jiggling and wiggling of atoms." Richard Feyman, 1963

# **1.2 An Overview of Computational Chemistry**

Computational chemistry or molecular modeling encompasses quantum mechanics, molecular mechanics, simulations, conformational analysis and other computer-based methods for understanding and predicting the behavior of molecular systems. Quantum chemistry is a branch of computational chemistry that attempts to explain the chemical phenomena through a computational solution of the basic equations of quantum mechanics. The theoretical basis for this field of chemistry embodies many of the important scientific discoveries made in the late 19<sup>th</sup> century and in the first part of the 20th century by Michael Faraday, Gustav Kirchoff, Ludwig Boltzman, Albert Einstein, Max Plank, Neils Bohr, Erwin Schrödinger and others [Cramer 2004]. Computational chemistry methods range from highly accurate ones feasible only for small systems to very approximate methods for larger systems. Depending on the formalism, these methods can be broadly classified into (a) Molecular mechanics (b) ab initio quantum chemical methods (c) semi-empirical quantum chemical methods (d) the density functional methods (e) molecular dynamics and Monte Carlo simulations and (f) hybrid quantum mechanics/molecular mechanics (QM/MM) methods. All these methods use different approximations to produce results of varying levels of accuracy. Except ab initio quantum chemical methods, all others rely on empirical information (parameters, energy levels etc.).

The molecular mechanics (MM) or force field methods [Bowen and Allinger 1991; Boyd and Lipkowitz 1982; Dinur and Hagler 1991; Weiner and Kollman 1981] use

the laws of classical physics and calculate the energy of a system as a function of the nuclear coordinates alone ignoring the electronic motions. MM calculations are based upon on a rather simple mathematical model of the system as a collection of balls (corresponding to the atoms) held together by springs (corresponding to the bonds). The energy of a molecule is expressed as a function of its resistance towards bond stretching, bond bending, and atom crowding and this energy equation is used to find the bond lengths, angles, and dihedrals corresponding to the minimum energy geometry. MM methods can invariably be used to perform calculations on systems containing significant number of atoms and, in some cases, provide answers that are as accurate as even the highest level quantum mechanical calculation in a fraction of the computer time, provided that the forcefield is carefully parameterized for the molecules studied. MM methods however, cannot throw light on electronic properties like charge distributions, nucleophilic and electrophilic behavior of molecules, electronic spectra etc.

Semi-empirical quantum mechanical methods [Pople and Beveridge 1970; Stewart 1990] are also based on Schrödinger equation and they represent a middle road between the mostly qualitative results from molecular mechanics and the highly computationally demanding quantitative results from *ab initio* methods. These methods are logically regarded as simplifications of the *ab initio* method since they use parameterizations and approximations from experimental data to provide input into mathematical models. Semi-empirical calculations are relatively inexpensive and much faster, often only with an inconsequential loss of accuracy and are generally applicable to very large molecular systems.

Computer simulations act as a bridge between microscopic length and time scales and the macroscopic world of the laboratory. Molecular dynamics (MD) and Monte Carlo (MC) methods are the two main families of simulation techniques widely employed in computational chemistry. MD methods use Newton's laws of motion to examine the time-dependent behavior of systems, including vibrations or Brownian motion, using a classical mechanical description [Rapaport 2004; Schlick 2002]. 'Monte Carlo' is almost always used to refer methods that use importance sampling, a technique that generates states of low energy. MC simulation generates configurations of a system by making random changes to the positions of the species present, together with their orientations and conformations where appropriate [Doll and Freeman 1994]. MD simulations are required if one wishes to calculate time-dependent quantities while, MC methods are often appropriate to investigate systems in certain ensembles.

The hybrid QM/MM approach combines the strength of both QM (accuracy) and MM (speed) calculations, are generally applicable for the calculation of ground and excited state properties like molecular energies and structures, energies and structures of transition states, atomic charges, reaction pathways etc. [Senn and Thiel 2009]. The basic idea of QM/MM methods is to partition the system into two (or more) parts. The region of chemical interest is treated using accurate QM methods while the rest of the system is treated using MM or less accurate QM methods such as semi-empirical methods or a combination of the two. *Ab initio* quantum chemical methods and density functional methods are discussed in detail in the forthcoming section.

# **1.2.1** Ab initio Molecular Orbital Theory

The electronic structure theory aims at solving the time-independent, nonrelativistic Schrödinger equation [Schrödinger 1926], which in its simplest form is

$$H\Psi = E\Psi$$
 (Eq. 1.7)

where H is the Hamiltonian operator,  $\Psi$  is the N-body wave function and E is the energy eigenvalue of the system. The Hamiltonian operator for a system of N electrons and M nuclei comprises of the nuclear and electronic kinetic energy operators and the potential energy operators corresponding to the nuclear-nuclear, nuclear-electron and electron-

electron interactions and may be written in atomic unit as:

$$\mathbf{H} = -\sum_{i=1}^{N} \frac{1}{2} \nabla_{i}^{2} - \sum_{A=1}^{M} \frac{1}{2M_{A}} \nabla_{A}^{2} - \sum_{i=1}^{N} \sum_{A=1}^{M} \frac{Z_{A}}{r_{iA}} + \sum_{i=1}^{N} \sum_{j>i}^{N} \frac{1}{r_{ij}} + \sum_{A=1}^{M} \sum_{B>A}^{M} \frac{Z_{A}Z_{B}}{R_{AB}} \quad (\text{Eq. 1.8})$$

where  $R_A$  and  $r_i$  are the position vectors of nuclei and electrons. The distance between the  $i^{th}$  electron and  $A^{th}$  nucleus is  $r_{iA}$ ; the distance between  $i^{th}$  and  $j^{th}$  electron is  $r_{ij}$  and the distance between the  $A^{th}$  nucleus and  $B^{th}$  nucleus is  $R_{AB}$ .  $M_A$  is the ratio of the mass of the nucleus A to the mass of an electron and  $Z_A$  is the atomic number of nucleus A.

The Schrödinger equation cannot be solved exactly for any molecular systems and hence some approximations are introduced for its practical applications. A common and very reasonable approximation used is the Born Oppenheimer (BO) approximation [Born and Oppenheimer 1927] which enables the electronic and nuclear motions to be separated. BO approximation is based on the concept that the nuclear and electronic motions take place at different time scales, the latter being much smaller than the former. Thus, an electron in motion sees relatively static nuclei, while a moving nucleus feels averaged electronic motion. The electronic wave function thus depends only on the positions of the nuclei and not on their momenta. Under the BO approximation the electronic Hamiltonian (Eq. 1.8) may be written as

$$\mathbf{H}_{\text{elec}} = -\sum_{i=1}^{N} \frac{1}{2} \nabla_{i}^{2} - \sum_{i=1}^{N} \sum_{A=1}^{M} \frac{Z_{A}}{r_{iA}} + \sum_{i=1}^{N} \sum_{j>i}^{N} \frac{1}{r_{ij}}$$
(Eq. 1.9)

The first term is the electronic kinetic energy operator summed over the number of electrons, N. The second term represents Coulombic attraction between N electrons and M nuclei, while  $Z_A$  are the nuclear charges. The last term attributes to the Coulombic repulsion between electrons. The eigenvalue equation involving the electronic Hamiltonian is then written as

$$\mathbf{H}_{\text{elec}} \Phi_{\text{elec}} \left( \{ \mathbf{r}_{i} \}; \{ \mathbf{R}_{A} \} \right) = \mathbf{E}_{\text{elec}} \Phi_{\text{elec}} \left( \{ \mathbf{r}_{i} \}; \{ \mathbf{R}_{A} \} \right)$$
(Eq. 1.10)

where  $\{\mathbf{r}_i\}$  and  $\{\mathbf{R}_A\}$  are the positions of electrons and nuclei, respectively. The solution to Eq. 1.10 gives the electronic wave function (Eq. 1.11) which describes the motion of electrons and depends explicitly on the electronic coordinates and parametrically on the nuclear coordinates.

$$\Phi(\{\mathbf{r}_{i}\};\{\mathbf{R}_{A}\}) = \Phi_{elec}(\{\mathbf{r}_{i}\};\{\mathbf{R}_{A}\}) \Phi_{nuc}(\{\mathbf{R}_{A}\})$$
(Eq. 1.11)

All properties can be calculated from the wave function, once the equations are solved as the expectation value of appropriate operator,  $\langle \Psi | \boldsymbol{O} | \Psi \rangle$ . An exact solution to the Schrödinger equation is not possible for any but the most trivial molecular systems and hence simplifying approximations are needed to get qualitatively correct solutions to the many body Schrödinger equation.

# **1.2.2 Hartree-Fock Theory**

Hartree-Fock (HF) theory (also known as independent particle model or a mean field theory) [Fock 1930; Hartree 1928; Slater 1930] is an approximate method for solving the Schrödinger equation which posits that each electron's motion can be described by a single-particle function (orbital) which does not depend explicitly on the instantaneous motions of other electrons. In the HF approach, the N-electron wave function for a given state is written as a Slater determinant, an anti-symmetrized product of spin orbitals.

$$\Psi(\mathbf{x}_{1}, \mathbf{x}_{2}, ..., \mathbf{x}_{N}) = \frac{1}{\sqrt{N!}} \begin{vmatrix} \chi_{i}(\mathbf{x}_{1}) & \chi_{j}(\mathbf{x}_{1}) \dots & \chi_{N}(\mathbf{x}_{1}) \\ \chi_{i}(\mathbf{x}_{2}) & \chi_{j}(\mathbf{x}_{2}) \dots & \chi_{N}(\mathbf{x}_{2}) \\ \vdots & \vdots & \ddots & \vdots \\ \chi_{i}(\mathbf{x}_{N}) & \chi_{j}(\mathbf{x}_{N}) \dots & \chi_{N}(\mathbf{x}_{N}) \end{vmatrix}$$
(Eq. 1.12)

The factor  $1/\sqrt{N!}$  is a normalization factor. The spin orbitals are denoted as  $\chi$ 's, while  $x_1$ ,  $x_2$ , etc. represent the combined spatial and spin coordinates of the respective electrons. An interesting consequence of this functional form is that the electrons are all

indistinguishable. The normalized Slater determinant can also be represented in a shorter notation as:

$$\Psi(\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_N) = \left| \chi_i \chi_j, \dots, \chi_k \right\rangle$$
 (Eq. 1.13)

In this notation it is presumed that electrons 1, 2, etc. sequentially occupy the spin orbitals.

In the HF method, the determinantal wave function is used to approximate the exact wave function and the energy is calculated as an expectation value of the Hamiltonian over this approximate wave function. The orbitals are found using the variational principle by minimization of the energy expectation value. Thus, the best approximate wave function can be obtained by varying all the wave function parameters, until the energy expectation value of the approximate wave function is minimized. The application of this minimizing procedure leads to the HF equations for the individual spin orbitals. HF equation is an eigenvalue equation of the form:

$$\mathbf{f}(i)\boldsymbol{\chi}(\mathbf{x}_{i}) = \boldsymbol{\varepsilon}\boldsymbol{\chi}(\mathbf{x}_{i}) \tag{Eq. 1.14}$$

where f(i) is an effective one-electron operator, called the Fock operator, of the form:

$$f(i) = -\frac{1}{2}\nabla_{i}^{2} - \sum_{A=1}^{M} \frac{Z_{A}}{r_{iA}} + V^{HF}(i)$$
 (Eq. 1.15)

where  $V^{\text{HF}}(i)$  is the HF potential which is the average potential experienced by the *i*<sup>th</sup> electron due to the presence of other electrons. Thus, the HF approximation replaces the complicated many-electron problem by a one-electron problem in which electron-electron repulsion is treated in an average way. The HF potential  $V^{\text{HF}}(i)$  depends on the spin orbitals of other electrons. The solution of HF eigenvalue problem yields a set  $\{\chi_k\}$  of orthonormal HF spin orbitals with orbital energies  $\{\varepsilon_k\}$ . The N spin orbitals with the lowest energies are called the occupied orbitals and the remaining members of the set

 $\{\chi_k\}$  are called virtual or unoccupied orbitals. The HF potential for the electron (1) is defined as:

$$\mathbf{V}^{\rm HF}(1) = \sum_{j}^{N} \left( \mathbf{J}_{j}(1) - \mathbf{K}_{j}(1) \right)$$
 (Eq. 1.16)

where  $J_j$  and  $K_j$  are the classical Coulomb and the exchange operators, respectively. The Coulomb operator takes into account the Coulombic repulsion between electrons, and the exchange operator represents the quantum correlation due to the Pauli exclusion principle.

Coulomb operator, 
$$J_{j}(1) = \int \chi_{j}(2) \frac{1}{r_{12}} \chi_{j}(2) d\mathbf{x}_{2}$$
 (Eq. 1.17)

The exchange operator can only be written through its effect when operating on a spin orbital  $\chi_i(1)$ ,

$$\mathbf{K}_{j}(1)\chi_{i}(1) = \left[\int \chi_{j}(2)\frac{1}{r_{12}}\chi_{i}(2)d\mathbf{x}_{2}\right]\chi_{j}(1)$$
 (Eq. 1.18)

Derivation of the HF equations for the closed shell systems was proposed by Roothaan and Hall [Hall 1951; Roothaan 1951]. The HF equation Eq. 1.14 may be rewritten by substituting Eq. 1.19, where the spin orbital is expressed as the linear combination of basis functions, leading to Eq. 1.20

$$\Psi_i = \sum_{\mu=1}^{K} C_{\mu i} \phi_{\mu} \qquad i = 1, 2, \dots, K$$
(Eq. 1.19)

where  $\phi_{\mu}$  are the basis functions corresponding to atomic orbitals,  $C_{\mu i}$  are the coefficients of  $\phi_{\mu}$  and K is the total number of basis functions. Roothaan Hall equation is written as a single matrix equation,

$$FC=SC\varepsilon$$
 (Eq. 1.20)

where  $\varepsilon$  are orbital energies, S is the overlap matrix and F is the Fock matrix. The Fock matrix F is the matrix representation of the Fock operator (Eq. 1.15) in the basis  $\phi_{\mu}$ . The Fock matrix must be diagonalized to find out the unknown molecular orbital coefficients in order to determine the eigenvalues from Roothaan Hall equation (Eq. 1.20).

The HF equation is non-linear and is solved iteratively using a procedure called self-consistent field (SCF) method in which a trial set of spin orbitals are guessed and used to construct the Fock operator. The new set of spin orbitals obtained from the solution is used to obtain a revised Fock operator, and this cycle of calculation and reformulation is repeated until the convergence criterion is satisfied. The one-electron nature of Fock operator results certain limitations to HF theory constructed using the Roothaan approach since all electron correlation is ignored other than exchange. The correlation energy is typically a small fraction of the total energy. However, it can be a very important contribution to many systems of physical and chemical interest. Further, the choice of basis set was challenging to early computational chemists. Even though the LCAO approach using hydrogenic orbitals remains attractive, this basis set requires numerical solution of the four index integrals appearing in the Fock matrix elements which is a tedious process. Since each index runs over the total number of basis functions, there are in principle  $N^4$  total integrals to be evaluated, and this quartic scaling behavior with respect to basis set size proves to be a bottleneck in HF theory applied to essentially any molecules.

# **1.2.3 Electron Correlation Methods**

Electron correlation methods or Post Hartee-Fock methods are a set of methods which go beyond SCF in attempting to add electron correlation in a more accurate way. Most of these methods require more flexible wave functions than that of a single determinant HF and usually it is obtained by means of excitations of electrons from occupied to virtual orbitals. The energy contribution resulting from the correlated motion of electrons is usually denoted as the correlation energy [Boys 1950] and is defined as the difference between the exact energy and the energy obtained by the HF method *i.e.*,

$$\mathbf{E}_{\rm corr} = \mathbf{\varepsilon}_0 - \mathbf{E}_0 \tag{Eq. 1.21}$$

where,  $\varepsilon_0$  is the exact eigenvalue of H<sub>elec</sub> and E<sub>0</sub> the "best" HF energy with the basis set extrapolated to completeness. The popular approaches that try to compute E<sub>corr</sub> are the configuration interaction (CI) [Foresman *et al.* 1992; Pople *et al.* 1976], coupled cluster (CC) [Cramer 2004; Kümmel 2002], and many body perturbation theory (MBPT) [Brillouin 1934; Kelly 1969] methods.

#### **1.2.3.1 Configuration Interaction**

The most simple and easiest method to incorporate electron correlation effect into an *ab initio* molecular orbital calculation is the configuration interaction (CI). In CI, the electronic state is described with excited states which are constructed by replacing one or more occupied orbitals with a virtual orbital within the HF determinant. In general, CI wave function can be written as:

$$\left|\Phi\right\rangle = c_{0}\left|\Psi_{0}\right\rangle + \sum_{ar} c_{a}^{r}\left|\Psi_{a}^{r}\right\rangle + \sum_{\substack{a < b \\ r < s}} c_{ab}^{rs}\left|\Psi_{ab}^{rs}\right\rangle + \sum_{\substack{a < b < c \\ r < s < t}} c_{abc}^{rst}\left|\Psi_{abc}^{rst}\right\rangle + \dots$$
(Eq. 1.22)

The first term in Eq. (1.22) represents the Slater determinant corresponding to the HF wave function and rest of the terms constitute singly, doubly, triply, ..., n-tuply excited determinants with appropriate expansion coefficients. The indices *a*, *b*, etc. signify the occupied orbitals and *r*, *s*, etc. signify the virtual orbitals involved in the electron excitations. The energy of the system is then minimized in order to determine the coefficients using linear variation approach. The number of excitations used to construct each determinant classifies the CI calculations. If only one electron has been moved from each determinant, it is called a configuration interaction single-excitation (CIS)

calculation. The CIS calculation gives an approximation to the excited states of a molecule, but do not change its ground-state energy. Single-and double excitation (CISD) calculations yield a ground-state energy that has been corrected for correlation. Triple-excitation (CISDT) and quadruple-excitation (CISDTQ) calculations are done only when very high accuracy results are desired. The configuration interaction calculation with all possible excitations is called a full CI. Full CI is important because it is the most complete possible estimation of electron correlation within the limitations imposed by the basis set. In the limit of a complete basis set full CI becomes complete CI, but is generally impractical. Truncated CI (CISD etc.) can be used as a simplification; however these methods are not size-consistent.

## **1.2.3.2 Coupled Cluster Methods**

The coupled cluster (CC) method [Čizek 1966] introduced by Čizek and Pauldus in the 1960's is among the most robust levels of theory that can describe dynamic electron correlation. It essentially takes the basic HF molecular orbital method and constructs multi-electron wave functions using the exponential cluster operator to account for electron correlation. The CC method assumes the full CI wave function,

$$\Psi_{\rm CC} = \mathbf{e}^{\rm T} \,\Psi_{\rm HF} \tag{Eq. 1.23}$$

 $\psi_{\text{HF}}$  is a Slater determinant constructed from HF molecular orbitals and

$$e^{T} = 1 + T + \frac{1}{2}T^{2} + \frac{1}{6}T^{3} + ... = \sum_{k=0}^{\infty} \frac{1}{k!}T^{k}$$
 (Eq. 1.24)

T is known as cluster operator which when acting on  $\psi_{HF}$  produces a linear combination of excited slater determinants and can be given as

$$T = T_1 + T_2 + T_3 + \dots + T_n$$
 (Eq. 1.25)

where n is the total number of electrons and various  $T_i$  operators generate all possible determinants having i<sup>th</sup> excitation from the reference.

$$T_{2} = \sum_{i < j}^{\text{occ.}} \sum_{a < b}^{\text{vir.}} t_{ij}^{ab} \psi_{ij}^{ab}$$
(Eq. 1.26)

where the amplitudes t are determined by the constraint that (Eq. 1.23) be satisfied. When considering the double excitation  $T = T_2$  and the Taylor expansion of the exponential function in (Eq. 1.23) gives

$$\Psi_{\rm CCD} = \left(1 + T_2 + \frac{1}{2!}T_2^2 + \frac{1}{3!}T_2^3 + \dots\right)\Psi_{\rm HF}$$
 (Eq. 1.27)

where CCD implies coupled cluster with only the double excitation operator. The first two terms in parenthesis  $(1 + T_2)$  defines the configuration double excitation method and the remaining terms involve the product of excitation operators. Solving for the unknown coefficients  $t_{ij}^{ab}$  is necessary for finding the approximate solution  $|\Psi_{CC}\rangle$ . The coupled cluster correlation energy is determined completely by the singles and doubles coefficients and the two electron MO integrals. The cost of including single excitations (T<sub>1</sub>) in addition to doubles defines CC singles-doubles (CCSD) model. Inclusion of connected triple excitations arising with their amplitudes from T<sub>3</sub> defines CCSDT and if the singles/triples coupling term is included then it is called CCSD(T). Coupled cluster calculations are size extensive but not variational. By including many excitation terms in the expansion, CC methods are computationally very expensive relative to HF calculations. Formally, CCSD scales as N<sup>6</sup>, CCSDT scales as N<sup>8</sup> and CCSD(T) scales as N<sup>7</sup>.

#### **1.2.3.3 Many-Body Perturbation Theory**

Møller and Plesset proposed an alternative way to tackle the problem of electron correlation based on Rayleigh-Schrödinger perturbation theory [Bartlett and Silver 1975; Krishnan and Pople 1978] in which the 'true' Hamiltonian operator H is expressed as the sum of a 'zeroth order' Hamiltonian  $H_0$  and a perturbation U:

$$H = H_0 + \lambda U \tag{Eq. 1.28}$$

The eigenfunctions of the 'true' Hamiltonian operator are  $\psi_i$ , with the corresponding energies  $E_i$ . The eigenfunctions of the zeroth-order Hamiltonian are written  $\psi_i^{(0)}$  with energies  $E_i^{(0)}$ . The ground-state wave function is thus  $\psi_0^{(0)}$  with energy  $E_0^{(0)}$ .  $\lambda$  is a parameter that can vary between 0 and 1; when  $\lambda$  is zero then H is equal to the zerothorder Hamiltonian but when  $\lambda$  is one then H equals its true value. The eigenfunctions  $\psi_i$ and eigenvalues  $E_i$  of H are then expressed in powers of  $\lambda$ :

$$\psi_{i} = \psi_{i}^{(0)} + \lambda \psi_{i}^{(1)} + \lambda^{2} \psi_{i}^{(2)} \dots = \sum_{n=0}^{\infty} \lambda^{n} \psi_{i}^{(n)}$$
(Eq. 1.29)

$$E_{i} = E_{i}^{(0)} + \lambda E_{i}^{(1)} + \lambda^{2} E_{i}^{(2)} + \dots = \sum_{n=0}^{\infty} \lambda^{n} E_{i}^{(n)}$$
(Eq. 1.30)

 $E_i^{(1)}$  is the first-order correction to the energy,  $E_i^{(2)}$  is the second-order correction and so on. These energies can be calculated from the eigenfunctions as follows:

$$E_{i}^{(0)} = \int \psi_{i}^{(0)} H_{0} \psi_{i}^{(0)} d\tau$$
 (Eq. 1.31)

$$E_{i}^{(1)} = \int \psi_{i}^{(0)} U \psi_{i}^{(0)} d\tau$$
 (Eq. 1.32)

$$E_{i}^{(2)} = \int \psi_{i}^{(0)} U \psi_{i}^{(1)} d\tau$$
 (Eq. 1.33)

$$E_{i}^{(3)} = \int \psi_{i}^{(0)} U \psi_{i}^{(2)} d\tau$$
 (Eq. 1.34)

To determine the corrections to the energy, it is necessary to determine the wave functions to a given order. In Møller-Plesset perturbation theory [Møller and Plesset 1934] the unperturbed Hamiltonian  $H_0$  is the sum of the one-electron Fock operator for the N electrons.

$$H_{0} = \sum_{i=1}^{N} f_{i} = \sum_{i=1}^{N} \left( H^{\text{core}} + \sum_{j=1}^{N} (J_{i} + K_{i}) \right)$$
(Eq. 1.35)

The zeroth-order energy is the sum of orbital energies for the occupied molecular orbitals.

$$\mathbf{E}_{0}^{(0)} = \sum_{i=1}^{\text{occupied}} \boldsymbol{\varepsilon}_{i}$$
(Eq. 1.36)

In order to calculate higher order wave functions, the form of the perturbation, U is established as the difference between the 'real' Hamiltonian, H and the zeroth-order Hamiltonian,  $H_0$ . The true Hamiltonian is equal to the sum of the nuclear attraction terms and electron repulsion terms:

$$H = \sum_{i=1}^{N} (H^{\text{core}}) + \sum_{i=1}^{N} \sum_{j=i+1}^{N} \frac{1}{r_{ij}}$$
(Eq. 1.37)

Hence the perturbation U is given by:

$$U = \sum_{i=1}^{N} \sum_{j=i+1}^{N} \frac{1}{r_{ij}} - \sum_{j=1}^{N} (J_j + K_j)$$
(Eq. 1.38)

The first-order energy  $E_0^{(1)}$  is given by:

$$E_0^{(1)} = -\frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \frac{1}{r_{ij}} [(ii \mid jj) - (ij \mid ij)]$$
(Eq. 1.39)

The sum of the zeroth-order and first-order energies corresponds to the HF energy,

$$E_0^{(0)} + E_0^{(1)} = \sum_{i=1}^{N} \varepsilon_i - \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} [(ii | jj) - (ij | ij)]$$
(Eq. 1.40)

To obtain an improvement on the HF energy it is necessary to use Møller-Plesset perturbation theory to at least second order. This level of theory is referred to as MP2 and involves the integral  $\int \psi_0^{(0)} U \psi_0^{(1)} d\tau$ 

The higher order wave function  $\psi_0^{(1)}$  is expressed as linear combinations of solutions to the zeroth-order Hamiltonian:

$$\psi_0^{(1)} = \sum_j c_j^{(1)} \psi_j^{(0)}$$
 (Eq. 1.41)

The  $\psi_j^{(0)}$  in Eq. 1.41 include single, double etc. excitations obtained by promoting electrons into virtual orbitals obtained from a HF calculation. The second order energy is given by:

$$E_{0}^{(2)} = \sum_{i}^{occupied} \sum_{j>i}^{virtual} \sum_{a}^{b>a} \frac{\iint d\tau_{1} d\tau_{2} \chi_{i}(1) \chi_{j}(2) \left(\frac{1}{r_{12}}\right) [\chi_{a}(1) \chi_{b}(2) - \chi_{b}(1) \chi_{a}(2)]}{\epsilon_{a} + \epsilon_{b} - \epsilon_{i} - \epsilon_{j}}$$
(Eq. 1.42)

These integrals will be non-zero only for double excitations, according to the Brillouin theorem [Brillouin 1934]. Third- and fourth-order Møller-Plesset calculations (MP3 and MP4) are also available. The advantage of many-body perturbation theory is that it is size-independent, unlike CI. However, Møller-Plesset perturbation theory is not variational and can sometimes give energies that are lower that the 'true' energy. Møller-Plesset calculations are computationally intensive, yet the most popular way to incorporate electron correlation in molecular quantum mechanical calculations.

# **1.2.4 Density Functional Theory**

The foundations of density functional theory (DFT) date from the 1920s with the work of Thomas and Fermi [Fermi 1927; Fermi 1928; Thomas 1927], but it was after the work of Hohenberg, Kohn, and Sham [Hohenberg and Kohn 1964; Kohn and Sham 1965] in the 1960s that the widespread application of DFT became a reality. In contrast to Hartree-Fock theory, DFT is based on electron density, rather than on wave functions. DFT is built around the premise that the energy of an electronic system can be defined in terms of its electron probability density,  $\rho(\mathbf{r})$ . An important advantage of using the  $\rho(\mathbf{r})$  over the wave function is the much reduced dimensionality. Regardless of how many electrons one has in the system, the density is always 3 dimensional whereas, the wave function for an N-electron system is a function of 3N spatial co-ordinates. This enables DFT to readily be applied to much larger systems with hundreds or even thousands of atoms. According to DFT formalism, the electronic energy, E is regarded as a functional

of the electron density,  $E[\rho(\mathbf{r})]$ , in the sense that the given function  $\rho(\mathbf{r})$  corresponds a single energy, *i.e.*, a one-to-one correspondence exists between the electron density of a system and its energy.

 $\rho(\mathbf{r})$  is defined as

$$\rho(\mathbf{r}) = N \int ... \int |\psi(x_1, x_2, ... x_N)|^2 d\sigma_1 d\sigma_2 ... dx_N$$
 (Eq. 1.43)

where  $\{x_i\}$  represents both spatial and spin coordinates.  $\rho(\mathbf{r})$  determines the probability of finding any of the N electrons within the volume  $\mathbf{r}$  but with arbitrary spin while the other N-1 electrons have arbitrary positions and spin in the state represented by  $\psi$ . This is a non-negative simple function of three variables, x, y, and z, integrating to the total number of electrons,

$$\mathbf{N} = \int \rho(\mathbf{r}) d\mathbf{r} \tag{Eq. 1.44}$$

#### **1.2.4.1 Thomas-Fermi Model**

The concept of density functional emerged for the first time in the late 1920's, in the early work of E. Fermi and L.H. Thomas, which introduced the idea of expressing the energy of a system as a function of the total electron density. In Thomas-Fermi model [Fermi 1927; Fermi 1928; Thomas 1927] the kinetic energy of the electrons is derived from the quantum statistical theory based on the uniform electron gas, but the electron-nucleus and electron-electron interactions are treated classically. Within this theory, the kinetic energy of the electron gas,  $T_{TF}[\rho(\mathbf{r})]$  is defined as,

$$T_{\rm TF}[\rho(\mathbf{r})] = \frac{3}{10} (3\pi^2)^{2/3} \int d\mathbf{r} \, \rho^{5/3}(\mathbf{r})$$
 (Eq. 1.45)

From the above equation, the approximation is made that the kinetic energy of the electrons depends exclusively on the electron density. By adding the interaction between electron-nucleus and electron-electron, a total energy in terms of electron density is obtained,

$$E[\rho(\mathbf{r})] = \frac{3}{10} (3\pi^2)^{2/3} \int d\mathbf{r} \, \rho^{5/3}(\mathbf{r}) - Z \int \frac{\rho(\mathbf{r})}{\mathbf{r}} d\mathbf{r} + \frac{1}{2} \iint \frac{\rho(\mathbf{r}_1)\rho(\mathbf{r}_2)}{|\mathbf{r}_1 - \mathbf{r}_2|} d\mathbf{r}_1 d\mathbf{r}_2 \qquad (\text{Eq. 1.46})$$

The second and third terms are the electron-nucleus and electron-electron interactions, respectively. The Thomas-Fermi kinetic energy functional is the only density functional that has an elegant mathematical derivation, but it is not accurate enough to be chemically useful. The significance of Thomas-Fermi model in the history of DFT is more as an illustration that the energy can be determined purely using the electron density. In1951, J.C. Slater [Slater 1951], applied the same basic idea into the development of the Hartee-Fock-Slater method, nowadays considered as a predecessor of the theory of DFT. However, a formal proof of this notion came with Hohenberg-Kohn Theorem.

#### 1.2.4.2 Hohenberg-Kohn Theorem

In 1964, Hohenberg and Kohn [Hohenberg and Kohn 1964] formulated and proved a theorem that put on solid mathematical grounds to the former ideas proposed by Thomas and Fermi. In their landmark paper Hohenberg and Kohn stated that (i) there exists a one-to-one correspondence between external potential and electron density and (ii) the ground state energy can be obtained variationally *i.e.*, the density that minimizes the total energy is the exact ground state density. A straightforward consequence of the first Hohenberg and Kohn theorem is that the ground state energy E is also uniquely determined by the ground-state charge density. The energy functional can be written as a sum of two terms:

$$E[\rho(\mathbf{r})] = \begin{bmatrix} V_{ext}(\mathbf{r})\rho(\mathbf{r})d\mathbf{r} + F[\rho(\mathbf{r})] & (Eq. 1.47) \end{bmatrix}$$

The first term arises from the interaction of the electrons with an external potential  $V_{ext}(\mathbf{r})$ , typically due to the Coulomb interaction with the nuclei.  $F[\rho(\mathbf{r})]$  is the sum of the kinetic energy of the electrons and the contribution from the interelectronic interactions.

The minimum value in the energy corresponds to the exact ground-state electron density, enabling a variational approach to be used. The DFT equivalent of the Schrödinger equation may be written as:

$$\left(\frac{\delta E[\rho(\mathbf{r})]}{\delta \rho(\mathbf{r})}\right)_{V_{ext}} = \mu$$
 (Eq. 1.48)

where  $\mu$  is a Lagrangian multiplier which can be identified with the chemical potential for the electron for its nuclei.

#### **1.2.4.3 The Kohn-Sham Equations**

Kohn and Sham [Kohn and Sham 1965] suggested a practical way to solve the Hohenberg-Kohn theorem for a set of interacting electrons. They showed that  $F[\rho(\mathbf{r})]$  should be approximated as the sum of three terms:

$$F[\rho(\mathbf{r})] = E_{KE}[\rho(\mathbf{r})] + E_{H}[\rho(\mathbf{r})] + E_{XC}[\rho(\mathbf{r})]$$
(Eq. 1.49)

where  $E_{KE}[\rho(\mathbf{r})]$  is the kinetic energy,  $E_{H}[\rho(\mathbf{r})]$  is the electron-electron Coulombic energy, and  $E_{XC}[\rho(\mathbf{r})]$  contains contributions from exchange and correlation. The first term,  $E_{KE}[\rho(\mathbf{r})]$ , is defined as the kinetic energy of a system of non-interacting electrons with the same density  $\rho(\mathbf{r})$  as the real system:

$$E_{\rm KE}[\rho(\mathbf{r})] = \sum_{i=1}^{N} \int \psi_i(\mathbf{r}) \left(-\frac{\nabla^2}{2}\right) \psi_i(\mathbf{r}) d\mathbf{r} \qquad (Eq. \ 1.50)$$

Hartree electrostatic energy,  $E_{\rm H}[\rho(\mathbf{r})] = \frac{1}{2} \iint \frac{\rho(\mathbf{r}_1)\rho(\mathbf{r}_2)}{|\mathbf{r}_1 - \mathbf{r}_2|} d\mathbf{r}_1 d\mathbf{r}_2$  (Eq. 1.51)

The full expression for the energy of an N-electron system within the Kohn-Sham scheme now becomes:

$$E[\rho(\mathbf{r})] = \sum_{i=1}^{N} \int \psi_{i}(\mathbf{r}) \left( -\frac{\nabla^{2}}{2} \right) \psi_{i}(\mathbf{r}) d\mathbf{r} + \frac{1}{2} \iint \frac{\rho(\mathbf{r}_{1})\rho(\mathbf{r}_{2})}{|\mathbf{r}_{1} - \mathbf{r}_{2}|} d\mathbf{r}_{1} d\mathbf{r}_{2} + E_{XC}[\rho(\mathbf{r})] - \sum_{A=1}^{M} \int \frac{Z_{A}}{\mathbf{r} - \mathbf{R}_{A}} \rho(\mathbf{r}) d\mathbf{r}_{2} d\mathbf{r}_{2} d\mathbf{r}_{2} d\mathbf{r}_{3} d\mathbf{r}_{4} d\mathbf{r}_{4} + E_{XC}[\rho(\mathbf{r})] - \sum_{A=1}^{M} \int \frac{Z_{A}}{\mathbf{r} - \mathbf{R}_{A}} \rho(\mathbf{r}) d\mathbf{r}_{4} d\mathbf{r}_{4} d\mathbf{r}_{4} d\mathbf{r}_{4} d\mathbf{r}_{4} d\mathbf{r}_{5} d$$

(Eq. 1.52)

This equation acts to define the exchange-correlation energy functional which thus contains not only the contributions due to exchange and correlation but also a contribution due to the difference between the true kinetic energy of the system and  $E_{KE}[\rho(\mathbf{r})]$ . Kohn and Sham wrote the density of the system as the sum of the square moduli of a set of one-electron orbitals:

$$\rho(\mathbf{r}) = \sum_{i=1}^{N} \left| \Psi_i(\mathbf{r}) \right|^2$$
(Eq. 1.53)

By introducing this expression for electron density and applying the appropriate variational condition, the one-electron Kohn-Sham equation takes the form:

$$\left\{-\frac{\nabla_1^2}{2} - \left(\sum_{A=1}^M \frac{Z_A}{r_{1A}}\right) + \int \frac{\rho(\mathbf{r}_2)}{r_{12}} d\mathbf{r}_2 + V_{\rm XC}[\mathbf{r}_1]\right\} \psi_i(\mathbf{r}_1) = \varepsilon_i \psi_i(\mathbf{r}_1) \qquad (\text{Eq. 1.54})$$

where  $\varepsilon_i$  are the orbital energies and  $V_{XC}$  is known as the exchange-correlation potential which is related to the exchange-correlation energy by:

$$V_{\rm XC}[\mathbf{r}] = \frac{\delta E_{\rm XC}[\rho(\mathbf{r})]}{\delta \rho(\mathbf{r})}$$
(Eq. 1.55)

To solve the Kohn-Sham equations a self-consistent approach is followed. An initial guess of the density is fed into Eq. 1.55 from which a set of orbitals can be derived, leading to an improved value of density, which is then used in the second iteration and so on until convergence is achieved. The exchange-correlation energy,  $E_{\rm XC}$  is generally divided into two terms, an exchange term  $E_{\rm X}$  (associated with the interaction of electrons of the same spin) and a correlation term  $E_{\rm C}$  (associated with the interaction of electrons of opposite spin). The corresponding functionals are exchange functional and correlation functional, respectively.

$$\mathbf{E}_{\mathrm{XC}}[\rho(\mathbf{r})] = \mathbf{E}_{\mathrm{X}}[\rho(\mathbf{r})] + \mathbf{E}_{\mathrm{C}}[\rho(\mathbf{r})]$$
(Eq. 1.56)

#### **1.2.4.4 Exchange-Correlation Functionals**

Kohn-Sham DFT is formally exact, but it does not lead to the exact form of exchange-correlation functional  $V_{XC}$ . The situation is well summarized by the quotation: "DFT is the method of choice for first principles quantum chemical calculations of the electronic structure and properties of many molecular and solid systems. With the exact exchange-correlation functional, DFT would take into full account all complex manybody effects at a computation cost characteristic of mean field approximations. Unfortunately, the exact exchange-correlation functional is unknown, making it essential to pursue the quest of finding more accurate and reliable functionals" [Xu and Goddard 2004]. For practical applications of DFT, several methods have been designed by modifying the exchange-correlation potential *viz*. (i) Local density approximation (LDA) (ii) Generalized gradient approximation (GGA) (iii) meta-GGA (iv) Hybrid functionals.

The local density approximation [Dirac 1930; Fermi 1927; Thomas 1927] represents the simplest approach to represent the exchange-correlation functional. LDA implicitly assumes that the exchange-correlation energy at any point in space is a function of the electron density at that point and can be given by the electron density of a homogenous electron gas of the same density. Within the LDA approach, the exchange function is given by:

$$E_{X}^{LDA}[\rho(\mathbf{r})] = -\frac{3}{4} \left(\frac{3}{\pi}\right)^{\frac{1}{3}} \int \rho^{\frac{4}{3}}(\mathbf{r}) d\mathbf{r}$$
 (Eq. 1.57)

The local spin density approximation (LSDA) proposed by J.C. Slater [Slater 1951], represents a more general application of LDA, which introduces spin densities into the functionals, thereby solving several conceptual problems of LDA. The exchange functional in LSDA approach is given by:

$$E_{X}^{LDA}[\rho(\mathbf{r})] = -2^{\frac{1}{3}} \left( -\frac{3}{4} \left( \frac{3}{\pi} \right)^{\frac{1}{3}} \right) \int \left( \rho_{\alpha}^{\frac{4}{3}}(\mathbf{r}) + \rho_{\beta}^{\frac{4}{3}}(\mathbf{r}) \right) d\mathbf{r}$$
 (Eq. 1.58)

 $\alpha$  and  $\beta$  represent spin up and down, respectively.

In LDA, the correlation energy  $E_C$  per particle is difficult to obtain separately from the exchange energy. Several different formulations for this functional have been developed by Vosko, L. Wilk and M. Nusair known as Vosko-Wilk-Nusair or VWN [Vosko *et al.* 1980] by incorporating Monte Carlo results.

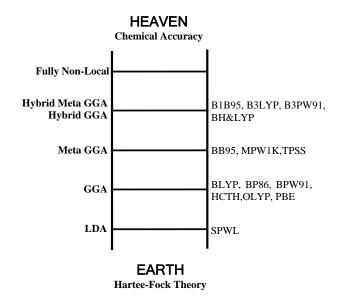
Generalized gradient approximation methods (GGAs) assume that the exchangecorrelation energies depend not only on the density but also on the gradient of the density,  $\nabla \rho(\mathbf{r})$ .

$$\mathbf{E}_{\mathrm{XC}}\left[\rho_{\alpha}(\mathbf{r}),\rho_{\beta}(\mathbf{r})\right] \equiv \int \varepsilon_{\mathrm{XC}}(\rho_{\alpha}(\mathbf{r}),\rho_{\beta}(\mathbf{r}),\vec{\nabla}\rho_{\alpha}(\mathbf{r}),\vec{\nabla}\rho_{\beta}(\mathbf{r}))\mathbf{d}^{3}\mathbf{r} \qquad (\mathrm{Eq.\ 1.59})$$

The development of GGA methods, follow two main lines; one based on numerical fitting procedures proposed by Becke [Becke 1988] and a more rational-based one advocated by Perdew [Perdew 1986; Perdew *et al.* 1992]. Meta-GGA functionals represent a significant improvement over GGA methods and depend explicitly on higher order density gradients which involve derivatives of the occupied Kohn-Sham orbitals.

Hybrid density functional (H-GGA) methods combine the exchange-correlation of a conventional GGA method with a percentage of HF exchange, with a certain degree of empiricism in optimizing the weight factor for each component and the functionals that are mixed. The exact amount of HF exchange is fitted semiempirically from experimental atomization energies, ionization potentials, proton affinities, total atomic energies, and other data, for a representative set of small molecules. Hybrid-meta GGA (HM-GGA) methods represent a new class of density functionals, based on a similar concept of M-GGAs, but start from M-GGAs instead of standard GGAs. These methods depend on HF exchange, the electron density and its gradient and the kinetic energy density.

J. Perdew presented the hierarchy of DFT approximations as Jacob's ladder (the famous allusion from the book of Genesis), containing five different rungs, comprising the five generations of density functionals *viz*. LDA, GGA, M-GGA, H-GGA and HM-HGA, and finally the fully nonlocal description [Perdew and Schmidt 2001]. Each rung adds something more to the design elements of the lower rungs and each rung has particular strength and weaknesses (Figure 1.11). Recently, Janesko added a new rung on the Jacob's ladder called "rung 3.5" which is an intermediate between the local and hybrid functionals [Janesko 2010; Janesko 2013].



**Figure 1.11** Jacob's ladder representing the five generations of density functional from the world of Hartree to the heaven of chemical accuracy, with examples from each class.

### **1.2.4.5 Minnesota Functionals**

Zhao and Truhlar presented and parameterized a new suite of functionals termed Minnesota functionals [Peverati and Truhlar 2011; Peverati and Truhlar 2012; Zhao *et al.* 2005a; Zhao *et al.* 2005b; Zhao and Truhlar 2006a; Zhao and Truhlar 2006b; Zhao and Truhlar 2008a; Zhao and Truhlar 2008b]. The Minnesota functional family includes one meta-GGA (M06-L), two meta-NGAs (M11-L and MN12-L), seven global-hybrid meta-GGAs (M05, M05-2X, M06-2X, M08-HX and M08-SO), one range-separated hybrid meta-GGA (M11) and one screened exchange hybrid meta-NGA (MN12-SX). The M06 family, the most popular among these, is composed of four functionals that have similar functional forms for the DFT part, but each has parameters optimized with a different percentage of HF exchange. The four functionals are (i) M06-L, a local functional (no HF exchange) (ii) M06, a global-hybrid meta-GGA with 27% of HF exchange, leading to a well-balanced functional for overall good performance for chemistry (iii) M06-2X, a global hybrid meta-GGA with 54% HF exchange, for top-level across-the-board performances in all areas of chemistry including thermochemistry and reaction kinetics, but excluding multi-reference systems such as those containing transition metals and (iv) M06-HF, a global-hybrid meta-GGA with 100% HF exchange, suitable for calculation of spectroscopic properties of charge-transfer transitions, where elimination of selfinteraction error is of prime importance. Although it was believed that one could not design a generally useful functional with 100% HF exchange, M06-HF disproved this by achieving overall performances for chemistry better than the popular B3LYP functional. The DFT calculations presented in this thesis have been carried out using M06-L functional. Being a non-hybrid meta GGA functional M06-L resides in the third rung of Jacob's ladder and can be applied for large systems with low costs.

### 1.2.5 Basis Sets

Basis set refers to the linear combinations of a pre-defined set of non-orthogonal one-electron wave functions used to build molecular orbitals, with the weights or coefficients to be determined. There are two main types of basis functions *viz*. Slater type orbitals (STOs) [Allen and Karo 1960] and Gaussian type orbitals (GTOs) [Boys 1950;

Feller and Davidson 1990]. The first basis sets used in molecular calculations were typically STOs, which correspond to a set of functions which decay exponentially with the distance from the nuclei. STOs have the exponential dependence:  $e^{-\zeta r}$  and are given by the mathematical expression:

$$\phi_{abc}^{STO}(\mathbf{x}, \mathbf{y}, \mathbf{z}) = \mathbf{N}\mathbf{x}^{a}\mathbf{y}^{b}\mathbf{z}^{c}\mathbf{e}^{-\zeta \mathbf{r}}$$
(Eq. 1.60)

where N is the Normalization constant, a, b, c control the angular momentum (L = a +b + c),  $\zeta$  determines the width or spread of the orbital and x, y, z represent the cartesian coordinates. STOs are not particularly amenable to implementation in molecular orbital calculations since some of the integrals in STOs are difficult to evaluate especially when the atomic orbitals are centered on different nuclei. Gaussian type orbitals have the exponential dependence  $e^{-\zeta r^2}$ . GTOs have the following mathematical expression:

$$\phi_{abc}^{STO}(x, y, z) = Nx^{a}y^{b}z^{c}e^{-\zeta r^{2}}$$
 (Eq. 1.61)

The computational advantage of GTOs over STOs is primarily due to the Gaussian product theorem, *viz.* the product of two GTOs is also a Gaussian function centered at the weighted midpoint of the two functions [Shavitt 1963]. In addition, the overlap and other integrals are easier to evaluate leading to huge computational savings. The Gaussian function described in Eq. 1.61 is generally known as primitive Gaussian (PGTO). It is a common practice [Stewart 1970] to bunch together a set of primitive Gaussian functions into one Gaussian function or a contracted Gaussian (CGTO),

$$\phi_{abc}^{CGTO}(\mathbf{x}, \mathbf{y}, \mathbf{z}) = N \sum_{i=1}^{n} c_{i} \mathbf{x}^{a} \mathbf{y}^{b} \mathbf{z}^{c} e^{-\zeta_{i} r^{2}}$$
(Eq. 1.62)

where n represent the number of Gaussian's to mimic the STO and  $c_i$  represent coefficients. By contracting several primitive Gaussians into one, the computational effort can be reduced through the optimization of several coefficients in one go. The degree of complexity, and thus precision, of a basis set is defined by the number of contracted functions employed to represent each atomic orbital, the minimum being one contracted function to describe a basis function (minimal basis set). For example the STO-3G basis set [Hehre *et al.* 1969] (where G indicates a combination of contracted Gaussian functions) is formed by a linear combination of three contracted functions for each basis function so as to resemble an STO.

For more precision and better description of the system, two or more functions can be used to describe each type of orbital, usually double-zeta (DZ) and triple-zeta (TZ) basis sets [Davidson and Feller 1986]. Pople and coworkers designed the split valence basis sets of type 'k-nlmG' where 'k' indicates how many PGTOs are used for representing the core orbitals and 'nlm' indicates both how many functions the valence orbitals are split into and how many PGTOs are used for their representation [Ditchfield et al. 1971]. 3-21G and 6-31G basis sets are examples of split valence basis sets [Binkley et al. 1980; Hehre et al. 1972]. Further improvements can be achieved by adding polarization or diffuse functions. Although a free isolated atom will have spherical symmetry, the atoms in a molecule or some other chemical environment will exhibit some distortions in their electron density. To take account of this effect, functions of higher angular momentum than the occupied atomic orbitals known as polarization functions are added to the basis sets. This is usually denoted as \* or \*\* (or (d) or (d, p)) after the G in the notation of the basis sets describing the use of an extra set of d-orbitals on heavy atoms and p-orbitals on hydrogens. Similarly, diffuse functions are sometimes included in the basis set to improve the description at large distances from the nuclei and are denoted by + or ++ signs. This is especially important for anions as the additional electrons are loosely bound to nuclei.

The basis sets employed for the calculations in the thesis are (a) Pople's split valence basis set, 6-311++G(d,p) with d polarization functions for non-hydrogen atoms and p polarization function for hydrogen atom as well as diffuse functions for non-

hydrogen and hydrogen atom [Hehre *et al.* 1986], (ii) Dunning's augmented correlation consistent polarized valence triple zeta basis function, aug-cc-pvtz [Dunning 1989] and iii) double-zeta valence plus polarization basis set (equivalent to the one used in DGauss software [Godbout *et al.* 1992]), DGDZVP.

### **1.2.6 Basis Set Superposition Error**

Basis set superposition error (BSSE) refers to the artificial shortening of intermolecular distances and concomitant strengthening of intermolecular interactions in weakly bound clusters while using smaller basis sets. When two fragments A and B approach each other to form a new species, their basis functions overlap. Each fragment "borrows" basis functions from the nearby components, effectively increasing its basis set and improving the calculation of derived properties such as energy. The energy of the system falls not only because of the favourable intermolecular interactions but also because the basis functions on each molecule provide a better description of the electronic structure around the other molecule. One widely used method to assess the BSSE is the counterpoise correction scheme of Boys and Bernardi [Boys and Bernardi 1970] in which the entire basis set is included in all calculations. To illustrate this, consider the binding energy of the dimer (AB) *viz*.  $A+B \rightarrow AB$ . The binding energy ( $\Delta E$ ) can be expressed as,

$$\Delta \mathbf{E} = \mathbf{E}(\mathbf{AB})_{ab} - [\mathbf{E}(\mathbf{A})_a + \mathbf{E}(\mathbf{B})_b]$$
(Eq. 1.63)

where  $E(AB)_{ab}$ ,  $E(A)_a$  and  $E(B)_b$  represent the energy of AB, monomer A and monomer B, respectively. Subscripts indicate the corresponding basis sets for AB, A and B. In counterpoise method, the calculation of the energy of the individual species A is performed in the presence of 'ghost' orbitals of B, without the nuclei or electrons of B. A similar calculation is performed for B using the 'ghost' orbitals on A. Using counterpoise method, BSSE can be evaluated with:

$$\Delta E_{BSSE} = E(\widetilde{A})_{ab} + E(\widetilde{B})_{ab} - E(\widetilde{A})_a - E(\widetilde{B}_b)$$
(Eq. 1.64)

where  $E(\tilde{A})_{ab}$  and  $E(\tilde{B})_{ab}$ , respectively represents the energy of monomer A and B in the structure it adopts in the dimer (AB) and with the full basis set of the dimer available.  $E(\tilde{A})_a$  and  $E(\tilde{B})_b$  are the energies of A and B, respectively, with only their own basis functions but again in the structure they adopt in the dimer. The correction to the binding energy can be calculated as,  $\Delta E - \Delta E_{BSSE}$ .

### **1.2.7 Atoms in Molecules**

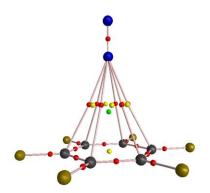
Richard Bader [Bader 1985; Bader 1991] pioneered the topographical investigation of molecular electron density (MED), one of the fundamental scalar functions that describe the probabilistic charge distribution of a molecule and developed a method called quantum theory of atoms in molecules (QTAIM). Topology of electron density  $\rho(\mathbf{r})$  provides an accurate mapping of the molecule and is effectively described by a set of critical points (CPs). MED attains maximum at the nuclear positions and each atom may be described by its boundaries dependent on the balance of forces of the considered system. A critical point (CP) is a point in the electron density surface where the gradient of electron density vanishes (Eq.1.65).

$$\nabla \rho(\mathbf{r}) = i \frac{d\rho(\mathbf{r})}{dx} + j \frac{d\rho(\mathbf{r})}{dy} + k \frac{d\rho(\mathbf{r})}{dz} \longrightarrow \begin{cases} = 0 \text{ (at critical points at } \infty) \\ \# 0 \text{ (at any other point)} \end{cases}$$
(Eq.1.65)

The critical points may correspond to maxima, saddle points or to the local minima. The various CPs are distinguished by considering the signs of the second derivatives of electron density. The Hessian matrix is formed from the nine possible second derivatives of electron density. The Laplacian is expressed as the sum of the eigenvalues of the Hessian matrix (Eq. 1.66).

$$\nabla^2 \rho(\mathbf{r}) = \nabla \cdot \nabla \rho(\mathbf{r}) = i \frac{\partial^2 \rho(\mathbf{r})}{\partial x^2} + j \frac{\partial^2 \rho(\mathbf{r})}{\partial y^2} + \frac{\partial^2 \rho(\mathbf{r})}{\partial z^2}$$
(Eq. 1.66)

Critical points are designated as ordered pair (r, $\omega$ ) where r is the rank of the CP and  $\omega$  the signature. The rank is the number of non-zero eigenvalues of the electron density at the CP and signature is the algebraic sum of the signs of eigenvalues. If one or more eigenvalue is/are zero, then the corresponding CP is termed degenerate *i.e.*, a degenerate CP has  $\omega < 3$ . A non-degenerate CP has all three eigenvalues non zero. There are four types of CPs of rank three: (3, -3), (3, -1), (3, +1) and (3, -3). (3, -3) CP corresponds to the local maximum, the nuclear attractor; (3, -1) is the bond critical point (BCP); (3, +1) is the ring critical point (RCP); and (3, -3) is the local maximum, called the cage critical point (CCP). Bond path (BP) is the line of maximum electron density connecting two interacting atoms or bond critical point is the minimum of electron density on the bond path. A collection of bond paths linking the nuclei of bonded atoms in equilibrium geometry with the associated critical points is known as the molecular graph. Figure 1.12 represents the molecular graph showing the bond paths and BCPs of hexafluorobenzene-nitrogen lone pair- $\pi$  complex.



**Figure 1.12** Molecular graph of hexafluorobenzene-nitrogen complex (M06L/6-311++G(d,p) level) showing the bond paths (lines) and different critical points (red for (3, -1) or bond CP, yellow for (3, +1) or ring CP, and green for (3, +3) or cage CP). Color-code by element: C = black, F = grey and N=blue.

Analysis of BCP provides information about the nature of various interatomic interactions [Bader and Essén 1984]. The Laplacian of electron density is negative for shared interactions like covalent and polarized bonds due to the concentration of electron density in the atom-atom region. Laplacian is positive for interactions like van der Waals, ionic and hydrogen bonds where there is depletion of electron charge in the atom-atom region. Pioneering works of Boyd and Choi showed that AIM theory can be applied for the analysis of hydrogen bonds [Boyd and Choi 1985; Boyd and Choi 1986]. The values of  $\rho(\mathbf{r})$  and  $\nabla^2 \rho(\mathbf{r})$  are important quantities to characterize hydrogen bonding in respect with strength and nature. Koch and Polpelier generalized a set of eight different criteria for a hydrogen bonds based on AIM analysis [Koch and Popelier 1995; Popelier 1998; Popelier and Logothetis 1998]. The eight criteria are: (i) the presence of (3, -1) BCP and bond path linking the CP with the bonded atoms, (ii) the values of  $\rho(\mathbf{r})$  at the (3, -1) BCP should lie in the range of 0.002 to 0.035 au (iii) the values of  $\nabla^2(\rho(\mathbf{r})$  should lie in the range of 0.024 to 0.139 au (iv) mutual penetration of hydrogen and acceptor atoms (v) increase in the positive charge on the hydrogen atom (vi) increase in the energy of the hydrogen atom (vii) decrease in the polarization of hydrogen atom and (viii) decrease in hydrogen atom volume. Grabowski proposed a new measure of hydrogen bond strength  $(\Delta_{com})$  using the properties of proton donating bond on the basis of detailed AIM analysis of a heterogeneous sample of hydrogen bonds, viz. O-H...O, O-H...N, C-H...O, C-H... $\pi$  and dihydrogen bonds [Grabowski 2001]. Quantitative values of  $\rho(\mathbf{r})$  and  $\nabla^2(\rho(\mathbf{r}))$ are good indicators of the character and strength of halogen bonds and anion- $\pi$ interactions also. Anion- $\pi$  interactions are characterized by the presence of cage critical point, located along the line connecting the ion with the center of the aromatic ring and the value of electron density at the CCP is a measure of the strength of the interaction [Garau et al. 2003a; Garau et al. 2004].

### **1.2.8 Molecular Electrostatic Potential**

Any distribution of electric charge, such as nuclei or electrons creates an electrical potential  $V(\mathbf{r})$  in the surrounding space. Molecular electrostatic potential or MESP [Pullman 1990; Scrocco and Tomasi 1978] can be regarded as the potential of a molecule to interact with an electric charge located at a point  $\mathbf{r}$ . Thus a positive charge is attracted to those regions in which  $V(\mathbf{r})$  is negative and is repelled from regions of positive potential. An important feature of MESP is that it is a real physical property and can be determined experimentally by X-ray diffraction techniques. MESP [Gadre and Shirsat 2000] can be rigorously and unambiguously calculated from the electron density function,  $\rho(\mathbf{r})$  using the equation:

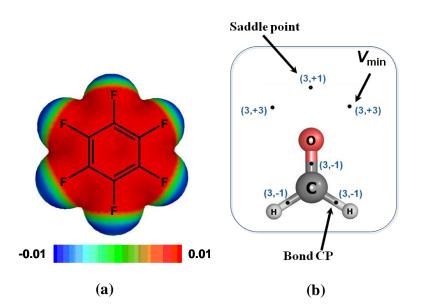
$$V(\mathbf{r}) = \sum_{A}^{N} \frac{Z_{A}}{|\mathbf{r} - \mathbf{R}_{A}|} - \int \frac{\rho(\mathbf{r}') d^{3} r'}{|\mathbf{r} - \mathbf{r}'|}$$
(Eq. 1.67)

where  $Z_A$  is the charge on nucleus A located at  $R_A$  and  $\mathbf{r}'$  is a dummy integration variable. The two terms refer to the bare nuclear potential and the electronic contributions, respectively. Effective localization of electron-rich regions in the molecular system thus emerges through a balance of these two terms. The above equation shows that the electrostatic potential is certainly specific to a given molecular geometry, and the value of  $V(\mathbf{r})$  in any particular region depends on whether the effect of nuclei or electrons is dominant there. Thus MESP is positive in the region close to nuclei and negative in the electron-rich region. The MESP can attain positive, zero or negative values, in contrast to the behavior of electron densities in position, which can attain only non-negative values. The ESP at nuclear sites shows a discontinuity and negative value since the nuclear contribution from the corresponding atom is dropped out. The MESP at a nuclei,  $V_{0,A}$  can be obtained by dropping nuclear contribution due to  $Z_A$  and can be give as:

$$V_{0,\mathrm{A}} = \sum_{\mathrm{B}\neq\mathrm{A}} \frac{Z_{\mathrm{B}}}{|\mathbf{R}_{\mathrm{B}} - \mathbf{R}_{\mathrm{A}}|} - \int \frac{\rho(\mathbf{r}')d^{3}\mathbf{r}'}{|\mathbf{r} - \mathbf{r}'|}$$
(Eq. 1.68)

Since MESP is a one electron property, its accurate quantification is possible within a variety of theoretical methods implemented in standard *ab initio* packages. Topographical features of MESP as well as the pictorial representation of MESP in the form of contours and isosurfaces are extremely useful for exploring the structure and reactivity of molecules, intermolecular interactions, molecular recognition and a variety of chemical phenomena [Gadre et al. 1996; Luque et al. 1994; Politzer and Truhlar 1981]. Figure 1.13 (a) depicts the MESP contour plot of hexafluorobenzene molecule textured on to a 0.003 au electron density surface with the electron rich region in blue and electron deficient regions in red. In MESP topography analysis the electronic distribution of molecules is understood in terms of critical points (CPs) i.e., the points at which the partial derivatives of MESP vanish. The signs of eigenvalues of the corresponding Hessian matrix indicate the nature of the CP. A CP, usually denoted as an ordered pair (R, S) of rank R and signature S, is classified according to the nature of the eigenvalues of the corresponding Hessian matrix. Rank is the number of non-zero eigenvalues of the Hessian matrix and the signature is defined as the algebraic sum of the signs of these eigenvalues. A CP possessing at least one zero eigenvalue is termed as degenerate while a non-degenerate CP has all the three eigenvalues nonzero. Four types of non-degenerate critical points for MESP exist with rank 3, viz. (3, -3), (3, -1), (3, +1)and (3, +3). A CP with (3, +3) character is referred to as local minimum while (3, -1)and (3,+1) are saddle points and (3, -3) is a local maximum. Figure 1.12 (b) shows the nature and location of MESP CPs of formaldehyde. MESP brings out electron rich regions like lone-pairs of electrons and  $\pi$ -bonds in the form of a negative valued (3, +3) minima. The most negative value of the MESP ( $V_{min}$ ) corresponds to a point at which electrostatic potential due to the electron density term dominates maximally over the bare nuclear term, the location of it indicates the electron-dense region of a molecule [Gadre and Pathak 1990b; Gadre and Shirsat 2000; Pathak and Gadre 1990; Shirsat *et al.* 1992].

Any bonding (covalent/weak) interaction between atoms is featured by the presence of a positive valued (3, -1) CP (BCP) and a positive valued (3, +1) CP is the manifestation of a ring [Gadre and Shirsat 2000]. The absence of non-nuclear maxima is a main feature of MESP topography over other scalar fields in the interpretation of electronic mechanisms. Similar to the molecular electron density (MED) topography, BCPs bring out the strain in bonds by deviating from the line joining the corresponding atoms. The significance of the negative-valued MESP and their critical points in molecules and their anionic species have been widely addressed in the literature [Gadre *et al.* 1992; Gadre and Pathak 1990a; Gadre and Shrivastava 1993; Luque *et al.* 1994; Politzer and Truhlar 1981].



**Figure 1.13** (a) MESP contour plot of hexafluorobenzene molecule textured on to a 0.003 au electron density surface,(b) nature and location of MESP CPs of formaldehyde.

In this thesis MESP is used as a predictive tool for analysing and quantifying intermolecular noncovalent interactions as well as predicting the reactive behaviour of molecules.

### **1.2.9 Solvation Models**

Even though gas phase predictions are appropriate for many purposes, some properties such as geometry, total energy, vibrational frequency and electronic spectra are considerably affected by the surrounding environment, such as solvent. Methods for evaluating solvent effect can be broadly classified into two types; those that treat the solvent as a continuous medium (continuum solvation) and those describing the individual solvent molecules (explicit solvation) [Cramer and Truhlar 1999]. Explicit solvation models represent the most rigorously correct way of modeling chemistry in solution but are computationally expensive. Continuum models include solvent as a uniform polarizable medium with a dielectric constant  $\varepsilon$  and the solute **M** is placed in a suitably shaped cavity in the medium [Foresman et al. 1996]. Dispersion interactions between the solvent and solute add stabilization while the creation of a hole in the medium costs energy, i.e. destabilization. The electric charge distribution of M will polarize the medium, which in turn acts back on the molecule, thereby producing an electrostatic stabilization. Thus the free energy of solvation,  $\Delta G_{sol}$  is expressed as the sum of three terms viz. the electrostatic ( $\Delta G_{elec}$ ) and dispersion-repulsion ( $\Delta G_{disp}$ ) contributions to free energy, and the cavitation energy ( $\Delta G_{cav}$ ).

$$\Delta G_{sol} = \Delta G_{elec} + \Delta G_{disp} + \Delta G_{cav} \qquad (Eq. 1.69)$$

SCRF (Self-Consistent Reaction Field) is a method of accounting for the effect of a polarizable solvent on the quantum system [Tomasi and Persico 1994]. The SCRF algorithm calculates the reaction field through solutions to the Poisson or Poisson---Boltzmann equation, and iteratively obtains self-consistency between the reaction field and charge distribution of the quantum system. SCRF methods vary with how they define the cavity and the reaction field. Polarizable continuum model (PCM) by Tomasi and coworkers is one of the most frequently used SCRF methods where the cavity is defined as the union of a series of interlocking atomic spheres [Cossi *et al.* 1996]. This technique uses a numerical integration over the solute charge density and generally gives good results.

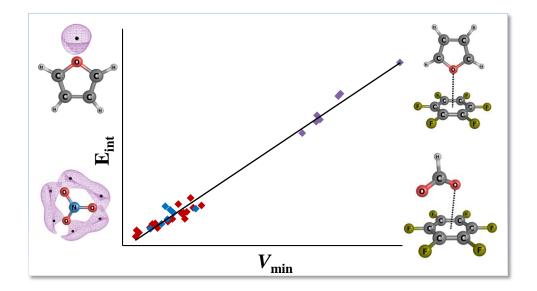
The isodensity PCM (IPCM) model defines the cavity as an isodensity surface of the molecule determined by an iterative procedure in which an SCF cycle is performed and converged using the current isodensity cavity [Foresman *et al.* 1996]. The resultant wavefunction is used to compute an updated isodensity surface, and the cycle is repeated until convergence is reached. An isodensity surface is a very natural, intuitive shape for the cavity since it corresponds to the reactive shape of the molecule possible. Selfconsistent isodensity PCM (SCI-PCM) embed the cavity calculation in the SCF procedure to account for coupling between the cavity and the electron density and includes coupling terms that IPCM neglects.

## **1.3 Conclusions**

Noncovalent interactions are of utmost importance in various fields of chemistry and biology. The first part of Chapter 1 gives an overview of various noncovalent interactions with special emphasis to hydrogen bonds, halogen bonds and anion/lone pair- $\pi$  interactions. Insights into the nature and strength of these interactions and the details of the various energetic contributions to their total interaction energy are also presented. An account of the experimental and theoretical studies that has contributed to the modern day understanding of hydrogen bonds, halogen bonds and anion/lone pair- $\pi$ interactions is also discussed.

Computational chemistry methods have become crucial for many developments in chemistry today and have contributed immensely towards understanding the noncovalent interactions at the molecular level. Computational chemistry uses the laws and equations that govern the subatomic world to calculate and predict molecular structure and properties. The second part of Chapter 1 deals with the theoretical background of the methods which are commonly used in computational chemistry calculations. A detailed account of the *ab initio* and density functional theory methods used in the calculations discussed in the thesis is presented in this section. The principles and applications of atoms in molecules and molecular electrostatic potential analysis employed for the quantification and characterization of weak interactions are also outlined.

# Molecular Electrostatics for Probing Lone Pairs and Lone Pair-π Interactions



# 2.1 ABSTRACT

Lone pairs are ubiquitous in chemistry to describe molecular interactions, yet their experimental characterization has never been achieved. Using a large variety of neutral, anionic and radical systems, it is shown that molecular electrostatic potential (MESP), a property amenable to experimental observation as well as theoretical calculation can reveal lone pairs. For electron-rich molecules, the negative minima in MESP topography give the location of electron localization and the MESP value at the minimum  $(V_{min})$  quantifies the electronrich character of that region. Calculations at M06L/6-311++G(d,p) DFT show that among neutral molecules,  $N_2$  exhibits the most shallow  $V_{min}$  (-11.4 kcal/mol) and imidazole possesses the deepest  $V_{min}$  (-68.4 kcal/mol).  $V_{min}$  at lone pairs of free radicals lie in the range -24.2 to -63.5 kcal/mol while anions exhibit large negative  $V_{min}$  (-155.7 to -240.3 kcal/mol). The eigenvalues of the Hessian at  $V_{min}$ and the orientation and distance of  $V_{min}$  from the lone pair bearing atom provide further characterization of a lone pair. Further, an electrostatics-based approach is proposed for probing the weak interactions between lone pair containing molecules and  $\pi$ -deficient molecular systems. Interactive behavior of lone pair bearing molecules with electron-deficient  $\pi$ -systems, viz., hexafluorobenzene, 1,3,5-trinitrobenzene, 2,4,6-trifluoro-1,3,5-triazine and 1,2,4,5-tetracyanobenzene are explored which show that good prediction on the lone pair- $\pi$  interaction energy  $(E_{int})$  can be achieved with  $V_{min}$  as it correlates linearly with  $E_{int}$ . On the basis of the precise location of MESP minimum, a prediction on the orientation of a lone pair bearing molecule with an electron-deficient  $\pi$ -system is possible in

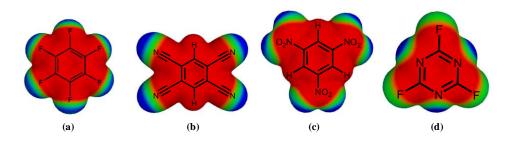
majority of the cases studied. Thus,  $V_{min}$  emerges as a powerful descriptor for lone pairs and also provides good predictions on the structure of intermolecular complexes and their interaction energy.

# **2.2 Introduction**

Lone pairs are known to play a vital role in describing the chemical and biological reactivity of molecules. Classically, a lone pair is defined as valence electron pair, bound to a nucleus, not utilized in chemical bonding. The concept of localized lone pairs originates from the classical Lewis-Langumir theory of bonding which explain covalent bonding in molecules based on the sharing of electrons in the valence shell [Langmuir 1919a; Langmuir 1919b; Lewis 1916]. Lewis dot representation of lone pairs is well-known and widely used formalism for representing covalent bonding in molecules. The role of lone pairs in determining the shape of molecules was examined by N. V. Sidgwick and H. E. Powell [Sidgwick and Powell 1940] and later by R. J. Gillespie and R. S. Nyholm [Gillespie 1963; Gillespie and Nyholm 1957] in a popular theoretical approach known as valence shell electron pair repulsion (VSEPR) model. VSEPR model is a natural extension of the electron pair model of Lewis and delineates the importance of varying electronic repulsions among shared pair and lone pair of electrons in valence shell orbitals. The concept of hybridization was introduced by Pauling in 1931 which is an essential tool useful for suggesting the presence and probable location of lone pair orbitals [Pauling 1931]. Molecular orbital (MO) theory, a popular bonding theory, in its purest form, is based on maximum amount of delocalization of MO's. Nevertheless, localization methods need to be invoked for describing a lone pair as an electron pair localized in a non-bonded valence MO [Chesnut 2003]. However, orbitals are not observables [Humphreys 1999; Scerri 2000; Zuo et al. 1999]. Experiments can only provide information about observables e.g. the electron density distribution and the entities derivable from it. Thus, characterization of lone pairs in terms of physical observables, such as the molecular electron density (MED) and molecular electrostatic potential (MESP) is more realistic and appropriate. The topological features of MED remain silent in the regime of non-bonded electrons and do not provide critical points (CPs) for lone pair regions though it yields a reliable depiction of bonding between atoms in molecules. Laplacian of the electron density,  $\nabla^2 \rho(\mathbf{r})$ , provide the physical basis for the Lewis and VSEPR models however, locating chemically significant CPs from the Laplacian distribution [Bader 1990] is difficult. Though the scalar field of electron localization function (ELF) is suggested for the study of lone pairs, [Becke and Edgecombe 1990; Chesnut 2003] it cannot provide a quantified value for the lone pair strength. Natural bond orbital (NBO) methods [Glendening et al. 2002; Reed et al. 1988; Weinhold 1998], generally regarded as a "chemist's basis set", are strongly orbital based and provides localized hybrid bond and lone pair orbitals instead of delocalized description of electrons. NBO analysis makes good predictions about the number of lone pairs and the percentage participation of s and p orbitals in a particular lone pair, generally in agreement with the classical hybridization concepts, but fails to predict the geometrical location of the lone pairs. Rather, it shows the occupancy in localized and delocalized MO and cannot provide a quantitative measure of lone pair strength.

The scalar field of MESP and its topographical features [Deshmukh *et al.* 2008; Gadre and Pathak 1990; Gadre and Shirsat 2000; Mathew and Suresh 2010] are the basis of the work presented in this chapter. MESP [Murray *et al.* 1994; Politzer *et al.* 1985; Pullman 1990; Sen and Politzer 1989; Sjoberg and Politzer 1990] is a well-established analytical tool for interpreting and predicting the reactive behavior of a variety of chemical systems. Tomasi *et al.* [Tomasi *et al.* 1990; Tomasi *et al.* 1996a; Tomasi *et al.*  1996b] pioneered the applications of MESP for understanding intermolecular interactions in the early 70's. Politzer and coworkers popularized MESP as an important tool to describe various chemical properties [Politzer et al. 1985; Politzer and Murray 2002; Politzer et al. 2001] such as bonding, chemical reactivity, inductive effect and resonance. In the methods developed by Politzer and coworkers, the positive and negative regions, generated by texturing the MESP on molecular surface have been used for identifying the sites of nucleophilic and electrophilic attack respectively. In a number of studies, Gadre and coworkers [Balanarayan et al. 2007; Deshmukh et al. 2008; Sundararajan et al. 2002; Yeole and Gadre 2011] have shown that by studying the topographical features of MESP, quantitative information about electron-rich regions corresponding to lone pairs or  $\pi$ -bonds in molecules can be obtained. The most negative value of the MESP ( $V_{\min}$ ) in the lone pair region or  $\pi$ -electron region is used as a measure of the electron-rich character of the corresponding region [Gadre et al. 1992; Mathew et al. 2007; Politzer and Murray 2002; Politzer et al. 2001; Suresh 2006; Suresh et al. 2008]. On the basis of electrostatic properties of the interacting molecules, Gadre and coworkers developed the electrostatic potential for intermolecular complexation (EPIC) model [Gadre et al. 1996; Gadre and Pundlik 1997; Pundlik and Gadre 1997] for predicting the orientation and interaction energies of weak molecular complexes. MESP analysis is also utilized in several other studies for identifying lone pair regions as well as to study molecular interactions [Gadre et al. 1992; Politzer and Murray 2002; Politzer et al. 2001]. MESP is calculated rigorously by using Eq. 1.67 presented in Chapter 1.

Electron-deficient aromatic rings often with halo-, nitro- and cyano- substituents have an inherent tendency to interact with lone pairs of neutral molecules and anions giving rise to lone pair- $\pi$  or anion- $\pi$  interactions [Hernández-Trujillo and Vela 1996; Laidig 1991]. A thorough understanding of the energetic and geometric features of lone pair- $\pi$  interactions is of prime importance in the design and development of hosts that exhibit anion and lone pair recognition property. MESP has been extensively applied for obtaining quantitative description of cation- $\pi$  interactions. [Ma and Dougherty 1997; Mecozzi et al. 1996a; Mecozzi et al. 1996b; Sayyed and Suresh 2011] However, the utility of this property in the study of lone pair- $\pi/anion-\pi$  interactions in general yet remains to be explored. The main aim of this work is to characterize and quantify lone pairs of molecules using MESP and then show that a great deal of information regarding the structure and interaction energy of lone pair bearing molecules with electrondeficient  $\pi$ -systems can be understood in terms of MESP topographical features. To do this study in a systematic way, the lone pair regions of a large variety of neutral, radical and anionic systems need to be investigated on the basis of  $V_{\min}$ . Further, a  $V_{\min}$  based approach is proposed for quantifying the lone pair- $\pi$ /anion- $\pi$  interaction energy. This approach is validated by modeling interactions of lone pair bearing molecules with electron-deficient aromatic host molecules, viz. hexafluorobenzene (HFB), 1,3,5trinitrobenzene (TNB), 2,4,6-trifluoro-1,3,5-triazine or cyanuric fluoride (CNF) and 1,2,4,5-tetracyanobenzene (TCB). Figure 2.1 presents the MESP textured on the 0.003 au electron density surface of HFB, TNB, CNF and TCB demonstrating their electrondeficient nature.



**Figure 2.1** MESP textured on the 0.003 au electron density surface for (a) HFB, (b) TCB, (c) TNB and (d) CNF demonstrating the electron deficient nature of the aromatic rings. Color coding, **blue** -0.01 au to red 0.01 au.

## **2.3 Computational Methods**

Geometries of the monomers and lone pair- $\pi$  complexes are fully optimized at M06-L [Zhao and Truhlar 2006] DFT functional employing 6-311++G(d,p) basis set without any symmetry constraints. Frequency calculations are performed to ensure that all the structures correspond to true energy minima containing only positive frequencies. Interaction energies of the complexes are calculated by using the supermolecule approach which gives the difference between the total energy of the complex and the sum of the isolated monomers. The computed interaction energies are corrected for basis set superposition error (BSSE) by using the counterpoise technique [Boys and Bernardi 1970]. Gaussian09 suite of programs [Frisch *et al.* 2010] is employed for all the calculations. Topological properties of molecular electron density (MED) at the bond critical points (BCP) are obtained by AIM methodology as implemented in AIM2000 program [Biegler-König and Schönbohm 2002; Biegler-König *et al.* 2001]. MESP topographical analysis of the monomers are carried out using the wave function obtained at M06L/6-311++G(d,p) level.

The location and characterization of the MESP CP is carried out using the Rapid topography mapping Fortran code developed recently by Gadre *et al.* [Yeole *et al.* 2012]. The hierarchy of their scalar field, *viz.* bare nuclear potential (BNP), molecular electron density (MED) and MESP is used for building the topography. The critical points of BNP, obtained by optimization of BNP grid points, serve as guess points for generating MED CPs. These MED CPs along with points generated inside a cube around each nuclei serve as guess points for generating MESP CPs. Guess points are optimized using L-BFGS code [Morales and Nocedal 2011]. The topography of MESP is much richer than that of BNP and MED scalar fields in terms of chemically significant CPs. The deformed atoms in molecules (DAM) procedure proposed by Rico and López *et* 

*al.* [Lòpez *et al.* 2009; Rico *et al.* 2005; Rico *et al.* 2004] is implemented for evaluating MED and MESP and corresponding gradients at guess point during optimization. The DAM method, based on partitioning of scalar field into atomic contributions, provides a rapid and sufficiently accurate function and gradient calculation.

Topographical analysis of MESP has been carried out for locating the MESP minima for a set of 34 molecules comprising of neutral species (H<sub>2</sub>O, N<sub>2</sub>, CO<sub>2</sub>, H<sub>2</sub>CO, H<sub>2</sub>S, HCN, NCCH<sub>3</sub>, HF, HCl, CH<sub>3</sub>OH, PH<sub>3</sub>, O(CH<sub>3</sub>)<sub>2</sub>, N(CH<sub>3</sub>)<sub>3</sub>, NH<sub>2</sub>COH, N<sub>3</sub>H, pyrimidine, pyridine, furan, imidazole and pyrazine), anions (Cl<sup>-</sup>, H<sub>2</sub>PO<sub>4</sub><sup>-</sup>, Br<sup>-</sup>, NO<sub>3</sub><sup>-</sup>, F<sup>-</sup>, CH<sub>3</sub>CO<sub>2</sub><sup>-</sup> and HCO<sub>2</sub><sup>-</sup>) and free radicals (OH<sup>•</sup>, CH<sub>3</sub>O<sup>•</sup>, CH<sub>3</sub>OO<sup>•</sup>, HCO<sup>•</sup>, CH<sub>3</sub>CO<sup>•</sup>, CH<sub>3</sub>NH<sup>•</sup> and HOO<sup>•</sup>). By mapping the MESP topography, the electronic distribution of molecules is understood through the critical points (CPs), *viz.* those points in space at which all the partial derivatives of MESP vanish. There are four types of non-degenerate critical points for MESP with rank 3, *viz.* (3, -3), (3, -1), (3, +1) and (3, +3). Herein (3, +3) is referred to as local minimum (*V*<sub>min</sub>) while (3, -1) and (3, +1) are saddle points and (3, -3) is a local maximum. More details of MESP CP's are given in Chapter 1.

# **2.4 Results and Discussion**

## 2.4.1 MESP Topography to Quantify Lone Pairs

MESP isosurfaces and minima of some representative systems are presented in Figure 2.2. The MESP topography features of neutral molecules are summarized in Table 2.1. Those of radicals and anions are reported in Table 2.2. Since the MESP minimum corresponds to a point at which electrostatic potential due to the electron density term dominates maximally over the bare nuclear term, the location of it indicates the electrondense region of a molecule.

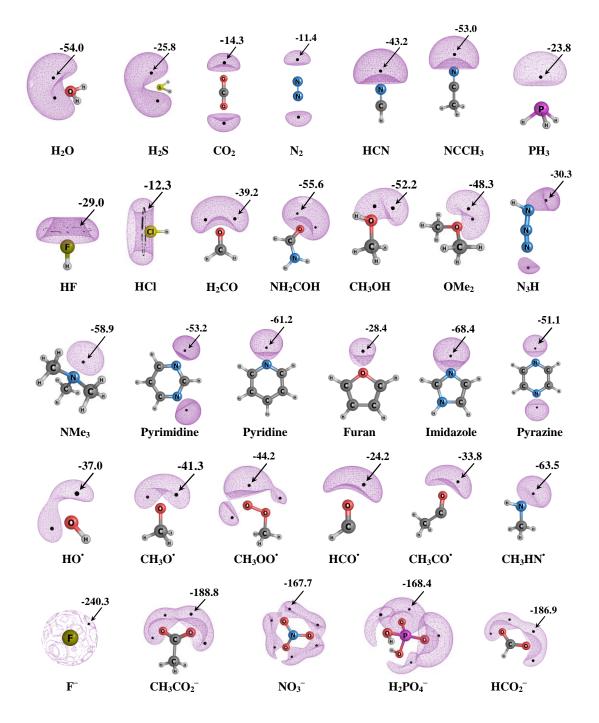


Figure 2.2 Representation of molecular electrostatic potential (MESP) isosurfaces for a representative set of lone pair species. The MESP minima are marked as black dots and the corresponding  $V_{\min}$  values are given in kcal/mol.

For the molecules given in Figure 2.2, MESP minima appear in the lone pair region.  $H_2O$  and  $H_2S$  are characterized by two such minima, one above and one below the plane of these molecules. For water,  $V_{min}$  is -54.0 kcal/mol, which is 28.2 kcal/mol

more negative than that of  $H_2S$ . This indicates that oxygen lone pairs of water are highly electron-rich compared to those of  $H_2S$ . Although lone pair regions of HCN, pyridine, furan, imidazole, pyrazine etc. are easily recognized in the MESP topography, cases such as HCl and HF exhibit a degenerate ring of negative potential at the halogen end [Gadre *et al.* 1992; Gadre and Shirsat 2000; Murray and Sen 1996] suggesting a delocalized distribution of lone pair electrons around the halogen atom (Figure 2.2). MESP topography of F<sup>-</sup>, Br<sup>-</sup> and Cl<sup>-</sup> reveals a sphere of negative potential around the ions.

Among all the systems discussed here, fluoride anion (F<sup>-</sup>) exhibits the deepest  $V_{\text{min}}$  (-240.3 kcal/mol) while the least negative  $V_{\text{min}}$  (-11.4 kcal/mol) is observed for N<sub>2</sub>. Imidazole has the most negative  $V_{\text{min}}$  value (-68.4 kcal/mol) among the aromatic heterocyclic molecules while furan has the least (-28.4 kcal/mol). Similarly CH<sub>3</sub>NH<sup>•</sup> and HCO<sup>•</sup> display the most (-63.5 kcal/mol) and the least (-24.2 kcal/mol) negative  $V_{\text{min}}$  among free radicals, respectively. It may be noted that MESP topography reveals (3, +3) CPs in the  $\pi$ -electron regions of molecules as well in addition to the CPs corresponding to the lone pair regions. For instance, furan and imidazole possess one CP each above and below the C=C bond.

For all the (3, +3) CPs of MESP one of the three eigenvalues is significantly more positive compared to the other two. For instance, in the case of H<sub>2</sub>O, among the three eigenvalues of the Hessian matrix (0.0064, 0.0327, 0.1304), the last one, *viz*. 0.1304 au is considerably more positive than the other two. The eigenvalues of NO<sub>3</sub><sup>-</sup> (0.1769, 0.0330, 0.0148) at the deepest minimum of MESP also show a similar character with one value being considerably larger. It is noticed that for the above systems, generally one of the eigenvalues of the Hessian is at least 5 times larger than the other two. It is also seen that the eigenvalues become more positive when  $V_{min}$  becomes more negative. Figure 2.3 depicts a linear relationship between  $V_{min}$  and the largest eigenvalue (LE) at the minimum. Good linear correlations for anions and neutral molecules with approximate correlation coefficient values of 0.93 and 0.94 respectively, are observed. The largest eigenvalue and corresponding eigenvector of the Hessian at the minima are shown to distinguish lone pair regions from the other types of electron localization (such as  $\pi$ -bonds). It has been shown that magnitude of eigenvalue at the CP that corresponds to lone pair, is numerically greater than 0.025 au and the eigenvector associated to it nearly points in the direction (angle  $\leq 5^{\circ}$ ) of the atom on which it is localized [Kumar *et al.* 2014].

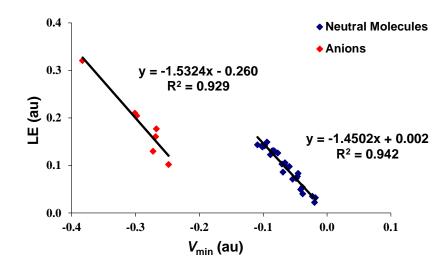


Figure 2.3 Correlation between MESP minimum  $(V_{\min})$  and the largest eigenvalue (LE).

MESP analysis shows that the position of negative-valued minimum is useful for characterizing the region of non-bonded electrons in the molecule. Since  $V_{min}$  value indicates the interaction energy of the molecule with a test positive charge at that location and an increase in the negative character of  $V_{min}$  value suggests higher electron concentration at that region,  $V_{min}$  value would qualify as a good parameter for quantifying the strength of a lone pair. This hypothesis is tested by studying the interactive behavior of all the lone pair bearing molecules with electron-deficient aromatic  $\pi$ -systems.

System	СР	No .of CPs	Distance of CP from lone pair atom (Å)		V <sub>min</sub> (kcal/mol)	Largest eigenvalue , LE (au)
H <sub>2</sub> O	(3,+3)	2	1.24	One above and one below the plane of the molecule forming a tetrahedral structure.	-54.0	0.1304
$N_2$	(3,+3)	2	1.54	Along the internuclear axis close to N atom.	-11.4	0.0320
$CO_2$	(3,+3)	2	1.48	Along the internuclear axis close to O atom.	-14.3	0.0350
H <sub>2</sub> CO	(3,+3)	2	1.29	Two on each side of the C2 axis close to the O atom.	-39.2	0.0960
$H_2S$	(3,+3)	2	1.78	One above and one below the plane of the molecule.	-25.8	0.0491
HCN	(3,+3)	1	1.37	Along the internuclear axis near the N atom.	-43.2	0.0858
NCCH <sub>3</sub>	(3,+3)	1	1.34	Along the internuclear axis near the N atom.	-53.0	0.1429
HF	Degenerate ring	-	1.30	Degenerate ring 1.30 Å away from the F end	-29.0	0.0769
HCl	Degenerate ring	-	1.90	Degenerate ring 1.90 Å away from the Cl end	-12.3	0.0219
CH <sub>3</sub> OH	(3,+3)	2	1.24	Two CPs equidistant from the O atom forming 117.5° with the OH bond.	-52.2	0.1310
PH <sub>3</sub>	(3,+3)	1	1.88	Along the C3 axis near the P atom	-23.8	0.0403
O(CH <sub>3</sub> ) <sub>2</sub>	(3,+3)	1	1.24	One above and one below the plane of the molecule near the O atom.	-48.3	0.1260

**Table 2.1** MESP topography features of neutral molecules.

Table 2.1 continued						
N(CH <sub>3</sub> ) <sub>3</sub>	(3,+3)	1	1.26	Along the C3 axis close to the N atom.	-58.9	0.1491
NH <sub>2</sub> COH	(3,+3)	4	1.25	Two CPs in the plane of the molecule near the O atom, two CPs above and below the plane at 1.60 Å from the N atom.	-55.6	0.1223
Pyrimidine	(3,+3)	2	1.29	One CP corresponding to each N atom lying in the plane of the molecule.	-53.2	0.1309
Pyridine	(3,+3)	1	1.28	One CP in the molecular plane at close to the N atom.	-61.2	0.1411
Furan	(3,+3)	5	1.31	One CP on the C2 axis near the O atom, one CP each above and below each C=C bond.	-28.4	0.0832
Imidazole	(3,+3)	3	1.28	One CP on the C2 near the N atom, one CP each above and below the C=C bond.	-68.4	0.1433
Pyrazine	(3,+3)	2	1.29	On the C2 axis at 1.29 Å from each N atom	-51.1	0.1291
N <sub>3</sub> H	(3,+3)	2	1.41	One CP for each terminal N atom at 1.41 Å and 1.50 Å respectively.	-30.3	0.0725

System	СР	No .of CPs	Distance of CP from lone pair atom (Å)		V <sub>min</sub> (kcal/mol)	Largest eigenvalue, LE (au)
НО∙	(3,+3)	2	1.29	One above and one below the plane of the molecule near the O atom.	-37.0	0.0975
CH <sub>3</sub> O <sup>●</sup>	(3,+3)	2	1.28	One above and one below the C2 axis near the O atom.	-41.3	0.1056
CH <sub>3</sub> OO•	(3,+3)	3	1.28	Two CPs in the molecular plane at 1.28 Å from the radical O and one CP on the adjacent O atom.	-44.2	0.1029
НСО•	(3,+3)	2	1.40	One CP in the molecular plane at 1.40 Å from the O atom and one CP on the adjacent C atom.	-24.2	0.0541
CH <sub>3</sub> CO•	(3,+3)	2	1.35	One CP in the molecular plane at 1.35 Å from the O atom and one CP on the C atom.	-33.8	0.0711
CH₃NH•	(3,+3)	1	1.29	One CP above the C-N plane at 1.29 Å from the N atom and 123.6° with the NH bond.	-63.5	0.1387
HOO•	(3,+3)	3	1.29	Two CPs in the plane of the molecule near the radical O atom and one CP 1.40 Å from the adjacent O atom.	-38.9	0.0186
$F^-$	Degenerate surface	-	1.08	Degenerate surface at 1.08 Å from F atom.	-240.3	0.3205
CH <sub>3</sub> CO <sub>2</sub> <sup>-</sup>	(3,+3)	4	1.15	Two CPs each on both sides of each O atom.	-188.8	0.2099

<b>Table 2.2</b> MESP topography features of radicals and anions.
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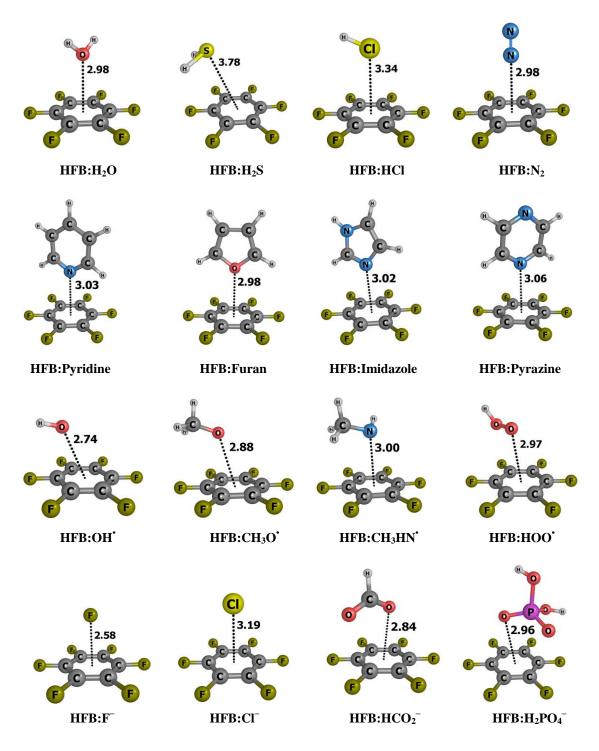
Table 2	.2 continued					
HCO <sub>2</sub> <sup>-</sup>	(3,+3)	4	1.16	Two CPs each on both sides of each O atom.	-186.9	0.2045
$NO_3^-$	(3,+3)	6	1.20	Two CPs each on both sides of each O atom.	-167.7	0.1769
Cl⁻	Degenerate surface	-	1.57	Degenerate surface at 1.57 Å from Cl atom.	-171.0	0.1298
Br <sup>-</sup>	Degenerate surface	-	1.74	Degenerate surface at 1.74 Å from Br atom.	-155.7	0.1019
$H_2PO_4^-$	(3,+3)	4	1.19	One CP corresponding to each O atom.	-168.4	0.1606

### **2.4.2 Lone Pair-** $\pi$ Complexes

Hexafluorobenzene (HFB) is employed as a model of an electron-deficient arene system to study lone pair- $\pi$  complexes. HFB is widely utilized in the literature for the study of lone pair- $\pi$  interactions and is an important binding motif used in the design of lone pair/anion sensors and receptors [Alkorta *et al.* 2002; Amicangelo *et al.* 2012; Danten 1999; Gallivan and Dougherty 1999; Kim *et al.* 2004; Quiňonero *et al.* 2002b]. The optimized geometries of a representative set of HFB-lone pair complexes are shown in Figure 2.4. Further, the interaction energy (E<sub>int</sub>), equilibrium distance between the molecule and the ring centroid (R<sub>hfb</sub>) and the equilibrium distance between the molecule and the nearest ring carbon atom (R<sub>c</sub>) are reported in Table 2.3 for all the HFB:lone pair complexes.

In lone pair- $\pi$  interactions, the lone pair should get electrostatically attracted towards the electron-deficient region of the  $\pi$ -system. The ring centroid of HFB is deficient of electrons due to electron withdrawing property of fluorine. Hence lone pair of guest molecules is expected to orient towards the ring centroid of HFB. However, in certain cases, slightly different orientations may be expected owing to the repulsive interactions of the atoms of the electron-rich guest molecules with the atoms of the HFB ring. Previous studies have shown that HFB offers two binding motifs for noncovalent interaction of lone pairs; one above the centroid of the ring and the second closer to the periphery of the ring [Hay and Bryantsev 2008]. The orientation of the interacting molecules with respect to the HFB ring in the lone pair- $\pi$  complexes can be explained on the basis of the topographical information of the binding molecule *i.e.*, from the location of their CPs.

Lone pair- $\pi$  complexes formed by molecules with two lone pairs, *viz*. H<sub>2</sub>S, OMe<sub>2</sub> and OH<sup>•</sup> exhibit off-center geometry with only one of the two lone pairs oriented towards the ring center. In molecules such as N<sub>2</sub>, CO<sub>2</sub>, HCN, N(CH<sub>3</sub>)<sub>3</sub>, NCCH<sub>3</sub>, PH<sub>3</sub> and in all heterocyclic compounds, the lone pair is located exactly above the ring centroid. Similarly HF, HCl and the F<sup>-</sup>, Br<sup>-</sup> and Cl<sup>-</sup> anions also lie exactly above the ring centroid of HFB since their lone pairs are symmetrically distributed as degenerate rings/spheres. The remaining anions (H<sub>2</sub>PO<sub>4</sub><sup>-</sup>, NO<sub>3</sub><sup>-</sup>, CH<sub>3</sub>CO<sub>2</sub><sup>-</sup> and HCO<sub>2</sub><sup>-</sup>) have more than four lone pairs and they form off-center complexes with HFB so as to generate maximum lone pair- $\pi$  interaction energy. The lone pairs present on O in HCO<sup>•</sup> and O in CH<sub>3</sub>CO<sup>•</sup> interact directly above the ring centroid of HFB. Thus the directionality of the lone pair- $\pi$  interaction is determined by the strength as well as the location of the lone pairs as revealed in the MESP topography.



**Figure 2.4** Optimized geometries of HFB-lone pair complexes at M06-L/6-311++G(d,p) level along with the interaction distances in Å.

	E <sub>int</sub>	R <sub>hfb</sub>	R <sub>c</sub>	θ	θ'	Δθ
System	(kcal/mol)	(Å)	(Å)	(deg)	(deg)	(deg)
H <sub>2</sub> O	-3.1	2.98	3.28	119.8	124.3	4.5
$N_2$	-1.0	2.98	3.28	180.0	179.8	-0.3
$CO_2$	-1.5	3.15	3.29	180.0	173.0	-7.0
H <sub>2</sub> CO	-2.7	2.97	3.27	131.3	174.0	42.7
$H_2S$	-2.5	3.78	3.50	102.5	85.8	-16.7
HCN	-3.1	3.02	3.28	180.0	164.5	-15.5
NCCH <sub>3</sub>	-3.8	2.97	3.25	180.0	175.4	-4.6
HF	-2.3	3.08	3.37	_ <sup>a</sup>	-	-
HCl	-1.7	3.34	3.61	_ <sup>a</sup>	-	-
CH <sub>3</sub> OH	-3.6	2.99	3.17	117.6	125.4	7.8
PH <sub>3</sub>	-2.1	3.47	3.73	123.3	123.9	0.6
O(CH <sub>3</sub> ) <sub>2</sub>	-4.8	2.96	3.24	121.3	104.9	-16.3
N(CH <sub>3</sub> ) <sub>3</sub>	-5.5	2.94	3.24	107.9	107.7	-0.2
NH <sub>2</sub> COH	-3.9	2.89	3.09	138.2	169.8	31.6
Pyrimidine	-3.7	3.06	3.35	121.6	122.1	0.5
Pyridine	-4.3	3.03	3.32	121.6	121.5	-0.1
Furan	-2.5	2.98	3.28	126.6	126.5	-0.2
Imidazole	-4.6	3.02	3.23	127.8	137.6	9.8
Pyrazine	-3.7	3.06	3.35	122.2	120.8	-1.4
N <sub>3</sub> H	-2.0	2.97	3.27	179.7	176.1	-3.6
HO●	-4.5	2.74	2.51	118.7	121.5	2.8
$CH_3O^{\bullet}$	-4.1	3.01	3.11	124.2	125.1	1.0
CH <sub>3</sub> OO <sup>●</sup>	-5.1	3.01	3.30	107.6	96.4	-11.2
HCO●	-1.9	2.97	3.25	141.3	175.2	34.0

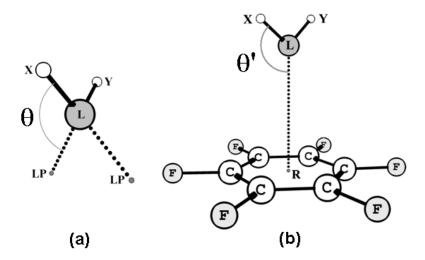
**Table 2.3** Interaction energies ( $E_{int}$ ) and distance parameters ( $R_{hfb}$  and  $R_c$ ) for the lone pair- $\pi$  complexes of HFB.

Table 2.3	continued	

$CH_3CO^{\bullet}$	-2.5	2.97 3.25	135.9	167.0	31.1
CH <sub>3</sub> NH <sup>●</sup>	-4.2	3.00 3.20	123.6	126.9	3.3
HOO●	-3.0	2.97 3.11	120.5	96.2	-24.3
$F^-$	-21.1	2.58 2.89	_ <sup>a</sup>	-	-
$CH_3CO_2^-$	-17.5	2.83 3.02	110.7	106.6	-4.1
$HCO_2^-$	-17.2	2.84 3.01	111.2	105.6	-5.6
$NO_3^-$	-14.3	2.80 3.04	107.1	86.4	-20.7
$\mathrm{Cl}^-$	-14.5	3.19 3.46	_ <sup>a</sup>	-	-
$\mathrm{Br}^-$	-13.0	3.37 3.58	_ <sup>a</sup>	-	-
$H_2PO_4^{-}$	-15.0	2.96 2.99	124.2	93.7	-30.5

<sup>a</sup> HCl, HF, F<sup>-</sup>, Br<sup>-</sup> and Cl<sup>-</sup> exhibit degenerate CPs and hence  $\theta$ ,  $\theta'$  and  $\Delta\theta$  could not be calculated.

The extent to which a lone pair is oriented towards the ring center can be quantified if we compare the orientation of the lone pair in the free molecule with the final geometry of the lone pair- $\pi$  complex. This is demonstrated in Scheme 2.1 where  $\theta$ indicates the angle that the lone pair makes with the atom bearing the lone pair and a nearby atom in the monomer. Similarly,  $\theta'$  indicates the angle that the centroid of the HFB makes with the lone pair bearing atom and the nearby atom. The difference between these two angles ( $\theta' - \theta$ ) designated as  $\Delta\theta$ , gives a good measure of the orientation of the lone pair in the complex. From  $\Delta\theta$  values, it is clear that in most of the complexes the lone pairs are oriented more or less towards the ring centroid. For instance, cases like PH<sub>3</sub>, N(CH<sub>3</sub>)<sub>3</sub>, pyridine, furan, N<sub>2</sub>, pyrimidine and CH<sub>3</sub>O<sup>•</sup> have  $\Delta\theta$  less than 1° indicating that the lone pair is almost perfectly aligned towards the center of the ring. Molecules such as H<sub>2</sub>CO, CH<sub>3</sub>CO<sup>•</sup>, HCO<sup>•</sup>, HOO<sup>•</sup>, NO<sub>3</sub><sup>-</sup> and H<sub>2</sub>PO<sub>4</sub><sup>-</sup> show  $\Delta\theta$  values in the range 20-30°. Since these molecules contain more than two lone pairs, an optimum configuration will maximize interactions from all the lone pairs with the HFB ring and hence the lone pairs may not necessarily point towards the centroid.

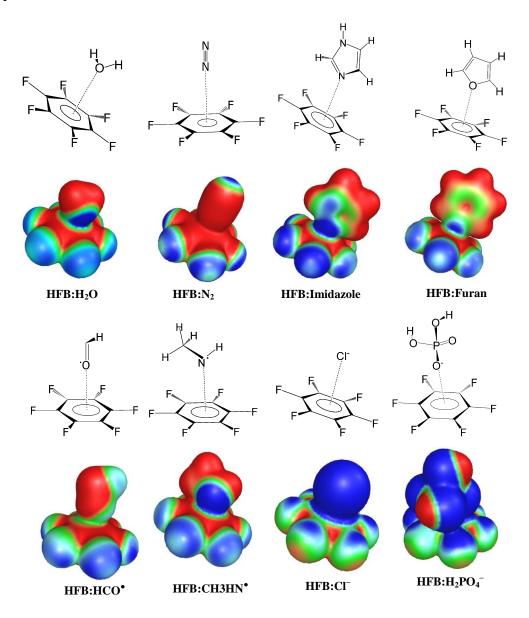


Scheme 2.1 Representation of (a) arrangement of lone pairs in a molecule and (b) orientation of the molecule in a lone pair- $\pi$  complex. L denotes the atom bearing the lone pair, X and Y are the atoms bonded to L. LP is the location of the lone pair, R is the ring centre,  $\theta$  is the angle which the lone pair makes with L and the nearest atom X and  $\theta'$  is the angle between L, X and R.

The above discussion confirms that MESP topography analysis allows the theoretical prediction of the strength and location of lone pairs and the directionality of lone pair- $\pi$  interactions. The interaction energies (E<sub>int</sub>) of lone pair- $\pi$  complexes range from very small in neutral molecules (N<sub>2</sub> and CO<sub>2</sub>) to very large in anions (F<sup>-</sup> and H<sub>2</sub>PO<sub>4</sub>). F<sup>-</sup> exhibits the most stable interaction (E<sub>int</sub> = -21.1 kcal/mol) while N<sub>2</sub> shows the weakest interaction (E<sub>int</sub> = -1.0 kcal/mol). All the heteroaromatics show significant lone pair- $\pi$  interaction with HFB and among them, imidazole exhibits the strongest interaction (-4.6 kcal/mol) and furan the weakest (-2.5 kcal/mol). The complex HFB:F<sup>-</sup> shows the shortest noncovalent bond distance (R<sub>hfb</sub> = 2.58 Å) and HFB:H<sub>2</sub>S shows the longest interaction distance (R<sub>hfb</sub> = 3.78 Å). E<sub>int</sub> values suggest that HFB can be effectively used

as a lone pair sensor for a wide range of lone pair species including neutral molecules, heteroaromatics, free radicals and anions.

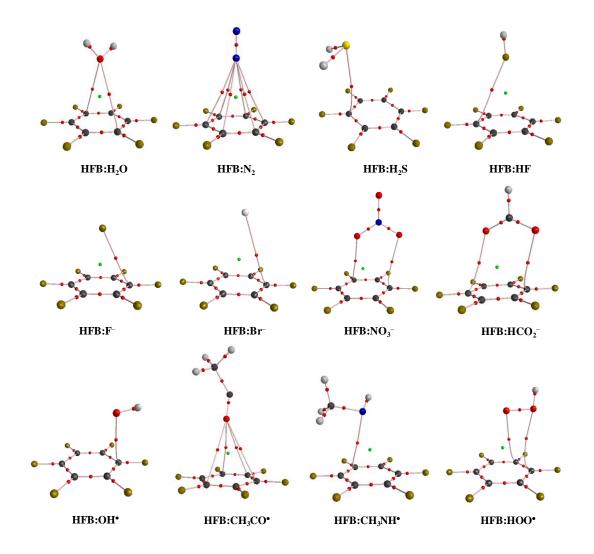
A quick glance at the electron density distribution of the complexes between HFB and the lone pair containing species may be obtained from Figure 2.5 which depicts MESP textured on to a 0.003 au electron density surface for some representative cases. This type of MESP plots are widely employed for identifying the electrophilic and nucleophilic regions in molecules. The MESP maps clearly indicate the interaction of the electron-deficient core of HFB (red) with the electron-rich lone pair/anion region (blue) giving rise to lone pair/anion- $\pi$  interaction. Moreover, the MESP pictures provide a qualitative measure of the lone pair/anion- $\pi$  interactions, analogous to the observations for cation- $\pi$  interactions [Mecozzi *et al.* 1996a; Mecozzi *et al.* 1996b]. However, unlike the MESP topographical analysis, such plots cannot provide quantitative information about lone pairs or lone pair- $\pi$  interactions.



**Figure 2.5** Molecular electrostatic potential textured on the 0.003 au electron density surface for HFB-lone pair complexes. Color coding **10.02**, blue -0.02 au to red 0.02 au for neutral and free radicals and blue -0.14 au to red -0.1 au for anionic species.

#### 2.4.3 Electron Density Analysis

Topographical properties of molecular electron density (MED) are often employed for studying the interactive behavior, particularly the bonding features of molecules. Though a lone pair indicates an electron-rich region, MED analysis will not yield a critical feature at that site and hence it will not provide the location of a lone pair in a molecule. In this respect, MESP topography is more advantageous than MED topography to locate non-bonded electrons in a molecule. However, MED analysis is useful for the study of bonded regions of a lone pair- $\pi$  complex. It has been demonstrated [Garau *et al.* 2003] for some systems that the electron density,  $\rho(\mathbf{r})$  and Laplacian of the electron density  $\nabla^2 \rho(\mathbf{r})$  at CPs are useful for characterizing bonding interactions. Figure 2.6 presents the AIM molecular graphs of HFB-lone pair complexes demonstrating bond paths, BCPs and CCPs.



**Figure 2.6** AIM molecular graphs of HFB-lone pair complexes showing the bond paths (lines) and bond critical points (red for BCPs and green for CCPs).

The presence of lone pair- $\pi$  interactions in all HFB complexes is confirmed by the presence of bond critical points (BCPs) of MED which connect the atom of the lone

pair bearing molecule to at least one, several or all the ring carbon atoms of HFB. Previous studies [Bauzá *et al.* 2012; Garau *et al.* 2003] have suggested that cage critical points (CCPs) located along the line connecting the center of the aromatic ring and the electron-donor atom can be used as a unique feature for lone pair- $\pi$ /anion- $\pi$  interactions. In the present study, CCPs have been located for all the HFB complexes except HFB:H<sub>2</sub>S, HFB:HO<sup>•</sup>, HFB:CH<sub>3</sub>O<sup>•</sup> and HFB:CH<sub>3</sub>OO<sup>•</sup>. In these four complexes, the guest species is slightly displaced towards the periphery of the HFB ring and the deviation from normal behavior could be attributed to an additional interaction of the hydrogen atoms of H<sub>2</sub>S, OH<sup>•</sup>, CH<sub>3</sub>O<sup>•</sup> and CH<sub>3</sub>OO<sup>•</sup> with the fluorine atoms in the HFB. Table 2.4 lists the AIM topological features of HFB:lone pair complexes.

Lone pair species	No. of RCPs	No. of CCPs	$\rho(\mathbf{r})$ at BCP (au)	$\nabla^2 \rho(\mathbf{r})$ at BCP (au)	$\rho(\mathbf{r})$ at CCP (au)	$\nabla^2 \rho(\mathbf{r})$ at CCP (au)
H <sub>2</sub> O	3	1	0.006	0.022	0.005	-0.006
$N_2$	7	1	0.006	0.023	0.005	-0.006
$CO_2$	2	1	0.005	0.019	0.003	-0.003
H <sub>2</sub> CO	3	1	0.005	0.021	0.004	-0.005
$H_2S$	1	0	0.007	0.019	_a	-
HCN	2	1	0.007	0.022	0.005	-0.006
NCCH <sub>3</sub>	2	1	0.007	0.024	0.005	-0.006
HF	2	1	0.004	0.016	0.003	-0.004
PH <sub>3</sub>	7	1	0.006	0.017	0.005	-0.005
OMe <sub>2</sub>	2	1	0.007	0.025	0.005	-0.006
NMe <sub>3</sub>	5	1	0.009	0.028	0.007	-0.008
NH <sub>2</sub> COH	2	1	0.008	0.030	0.005	-0.006
Pyrimidine	4	1	0.007	0.021	0.005	-0.006

**Table 2.4** AIM topological features of HFB:lone pair complexes

10010 211		. Ci				
Pyridine	4	1	0.007	0.022	0.005	-0.006
Furan	4	1	0.006	0.022	0.005	-0.006
$N_3H$	3	1	0.006	0.023	0.005	-0.006
OH	1	0	0.023	0.083	_ <sup>a</sup>	-
CH <sub>3</sub> O <sup>•</sup>	1	0	0.014	0.053	_ <sup>a</sup>	-
CH <sub>3</sub> OO <sup>•</sup>	3	0	0.008	0.030	_ <sup>a</sup>	-
HCO'	2	1	0.005	0.020	0.004	-0.005
CH <sub>3</sub> CO <sup>•</sup>	5	1	0.006	0.022	0.004	-0.005
CH <sub>3</sub> NH <sup>•</sup>	2	1	0.008	0.025	0.005	-0.006
HOO	3	1	0.008	0.029	0.005	-0.006
F	2	1	0.012	0.047	0.008	-0.011
CH <sub>3</sub> CO <sub>2</sub> <sup>-</sup>	3	1	0.014	0.047	0.006	-0.008
HCO <sub>2</sub> <sup>-</sup>	3	1	0.013	0.044	0.006	-0.007
NO <sub>3</sub> -	3	1	0.013	0.045	0.006	-0.008
Br	2	1	0.007	0.022	0.005	-0.005
$H_2PO_4^-$	4	1	0.011	0.040	0.005	-0.006

-- Table 2.4 continued --

<sup>a</sup> CCPs not located

### 2.4.4 Correlation between V<sub>min</sub> and E<sub>int</sub>

Since the strength of lone pair- $\pi$  interaction depends on the electron-rich nature of the interacting lone pair which is directly reflected in the MESP value at the minimum, it should be possible that the characterization of lone pair strength using MESP may provide a simple approach to quantify lone pair- $\pi$  interactions. Figure 2.7 depicts the relationship between E<sub>int</sub> and V<sub>min</sub> value for complexes between HFB and the lone pair bearing molecules. An excellent linear correlation is observed between the two quantities. Small deviation shown by the systems HFB:O(CH<sub>3</sub>)<sub>2</sub>, HFB:HO<sup>•</sup> and HFB:CH<sub>3</sub>O<sup>•</sup> could be due to the additional stabilization provided by the interaction of side-chain hydrogen atoms with the fluorine atoms of HFB ring. A more negative  $V_{min}$  corresponds to higher  $E_{int}$ . This suggests that the ability of a molecule to form a lone pair- $\pi$  interaction with HFB can be assessed in terms of the  $V_{min}$  value corresponding to the lone pair in the molecule.

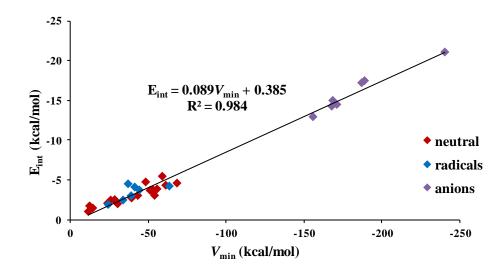
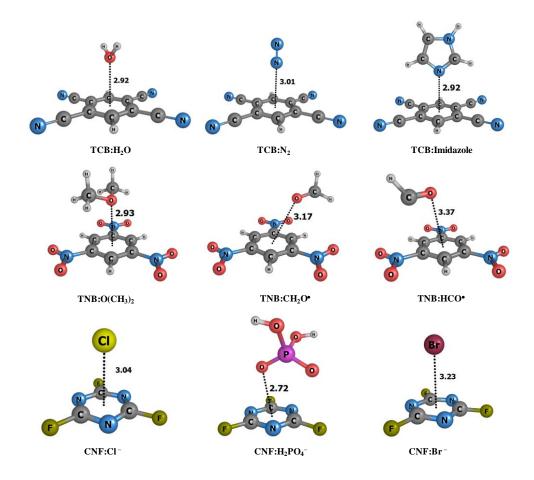


Figure 2.7 Correlation between MESP  $V_{min}$  at lone pair region and interaction energy of the complexes between HFB and the lone pair containing species.

#### 2.4.5 Validation of V<sub>min</sub> vs E<sub>int</sub> Relationship

The relationship between  $V_{\text{min}}$  and  $E_{\text{int}}$  is further validated by modeling lone pair-  $\pi$  complexes of 1,3,5-trinitrobenzene (TNB), 2,4,6-trifluoro-1,3,5-triazine or cyanuric fluoride (CNF) and 1,2,4,5-tetracyanobenzene (TCB) with a representative set of lone pair bearing molecules (H<sub>2</sub>O, N<sub>2</sub>, CO<sub>2</sub>, H<sub>2</sub>S, HCN, O(CH<sub>3</sub>)<sub>2</sub>, N(CH<sub>3</sub>)<sub>3</sub>, pyridine, furan, imidazole, HCO<sup>•</sup>, CH<sub>3</sub>O<sup>•</sup>, Cl<sup>-</sup>, H<sub>2</sub>PO<sub>4</sub><sup>-</sup>, Br<sup>-</sup>, NO<sub>3</sub><sup>-</sup> and HCO<sub>2</sub><sup>-</sup>). Representative set of lone pair- $\pi$  complexes of TNB, TCB and CNF are shown in Figure 2.8.



**Figure 2.8** Optimized geometries of lone pair- $\pi$  complexes of 1,2,4,5-tetracyanobenzene (TCB), 1,3,5-trinitrobenzene (TNB) and 2,4,6-trifluoro-1,3,5-triazine (CNF) with a representative set of lone pair bearing molecules. Distances in Å.

The correlation diagrams between  $E_{int}$  and  $V_{min}$  for TNB, CNF and TCB are depicted in Figure 2.9. The excellent linear correlation between the two quantities for all the three molecules confirms the ability of  $V_{min}$  to predict lone pair- $\pi$  interaction energy. Hence, the value of MESP at the minimum,  $V_{min}$  is proposed as a useful descriptor for studying the interactive behavior of a lone pair bearing molecule with electron-deficient  $\pi$ -systems. The values of  $E_{int}$ ,  $R_{hfb}$ ,  $R_c$ ,  $\theta$ ,  $\theta'$  and  $\Delta\theta$  for lone pair- $\pi$  complexes of TCB, CNF and TNB, are given in Table 2.5, Table 2.6 and Table 2.7, respectively.

#### Chapter 2

System	E <sub>int</sub>	R <sub>hfb</sub>	R <sub>c</sub>	θ	θ'	$\Delta \theta$
bystem	(kcal/mol)	(Å)	(Å)	(deg)	(deg)	(deg)
H <sub>2</sub> O	-5.0	2.92	3.24	119.8	128.1	8.3
$N_2$	-1.5	3.01	3.32	180	179.5	-0.5
$CO_2$	-2.2	3.12	3.42	180	178.9	-1.1
$H_2S$	-3.1	4.32	3.68	102.5	98.1	-4.4
N(CH <sub>3</sub> ) <sub>3</sub>	-7.6	3.00	3.28	107.9	133.5	25.6
O(CH <sub>3</sub> ) <sub>2</sub>	-6.3	2.92	3.19	121.3	110.5	-10.8
Imidazole	-7.1	2.92	3.21	127.8	128.3	0.5
Pyridine	-6.6	2.97	3.28	121.6	121.2	-0.4
Furan	-4.6	3.17	3.29	126.6	94.6	-32.0
HCO●	-2.8	3.83	3.11	141.3	141.5	0.2
$CH_3O^{\bullet}$	-3.7	3.75	3.04	124.2	109.5	-14.7
$H_2PO_4^{-}$	-16.7	2.84	3.00	124.2	96.4	-27.8
$NO_3^-$	-18.6	2.77	3.06	107.1	87.6	-19.5
Cl⁻	-16.8	3.36	2.88	_ <sup>a</sup>	-	-
$\mathrm{Br}^-$	-14.5	3.54	3.07	_ <sup>a</sup>	-	-
$\mathrm{HCO}_2^-$	-22.3	2.73	3.00	111.2	106.0	-5.2

**Table 2.5** Interaction energies ( $E_{int}$ ), distance parameters ( $R_{hfb}$  and  $R_c$ ) and  $\theta$ ,  $\theta$ ' and  $\Delta\theta$  values for lone pair- $\pi$  complexes of 1,2,4,5-tetracyanobenzene (TCB).

<sup>a</sup> Br<sup>-</sup> and Cl<sup>-</sup> exhibit degenerate CPs and hence  $\theta$ ,  $\theta$ ' and  $\Delta\theta$  could not be calculated.

**Table 2.6** Interaction energies ( $E_{int}$ ), distance parameters ( $R_{hfb}$  and  $R_c$ ) and  $\theta$ ,  $\theta$ ' and  $\Delta\theta$  values for lone pair- $\pi$  complexes of 2,4,6-trifluoro-1,3,5-triazine (CNF).

System	E <sub>int</sub> (kcal/mol)	R <sub>hfb</sub> (Å)	R <sub>c</sub> (Å)	θ (deg)	θ' (deg)	$\Delta \theta^{a}$ (deg)
H <sub>2</sub> O	-4.2	2.98	3.21	119.8	137.3	17.5
$N_2$	-1.2	3.12	3.41	180	178.5	-1.5
$CO_2$	-1.9	3.08	3.37	180	179.8	-0.2

Table 2.6 c	continued -	-				
$H_2S$	-3.4	4.20	3.59	102.5	97.1	-5.4
N(CH <sub>3</sub> ) <sub>3</sub>	-8.1	2.98	3.28	107.9	107.6	-0.3
O(CH <sub>3</sub> ) <sub>2</sub>	-6.1	2.93	3.22	121.3	108.9	-12.4
Imidazole	-8.7	3.21	3.48	127.8	91.5	-36.3
Pyridine	-7.3	3.18	3.43	121.6	92.2	-29.4
Furan	-6.9	3.25	3.26	126.6	94.6	-32.0
HCO <sup>●</sup>	-3.6	3.37	3.34	141.3	96.7	-44.6
$CH_3O^{\bullet}$	-5.0	3.17	2.67	124.2	135.9	11.7
$H_2PO_4^-$	-27.9	2.81	2.93	124.2	95.5	-28.7
$NO_3^-$	-27.9	3.14	2.50	107.1	103.4	-3.7
$Cl^-$	-31.5	3.21	2.51	_a	-	-
Br <sup>-</sup>	-29.4	3.41	2.72	_a	-	-
$HCO_2^-$	-34.7	2.75	3.04	111.2	98.7	-12.5

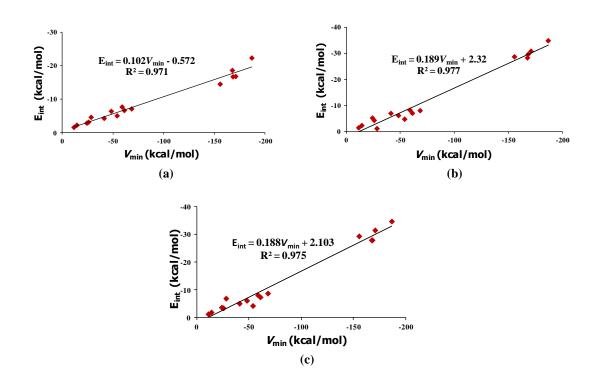
<sup>a</sup> Br<sup>-</sup> and Cl<sup>-</sup> exhibit degenerate CPs and hence  $\theta$ ,  $\theta$ ' and  $\Delta\theta$  could not be calculated.

**Table 2.7** Interaction energies ( $E_{int}$ ), distance parameters ( $R_{hfb}$  and  $R_c$ ) and  $\theta$ ,  $\theta$ ' and  $\Delta\theta$  values for lone pair- $\pi$  complexes of 1,3,5-trinitrobenzene (TNB).

System	E <sub>int</sub>	R <sub>hfb</sub>	R <sub>c</sub>	θ	θ'	$\Delta \theta^{a}$
System	(kcal/mol)	(Å)	(Å)	(deg)	(deg)	(deg)
$H_2O$	-4.7	2.92	3.24	119.8	128.1	8.3
$N_2$	-1.4	3.01	3.32	180	179.5	-0.5
$CO_2$	-2.2	3.12	3.42	180	178.9	-1.1
$H_2S$	-4.2	4.32	3.68	102.5	98.1	-4.4
N(CH <sub>3</sub> ) <sub>3</sub>	-8.1	3.00	3.28	107.9	133.5	25.6
O(CH <sub>3</sub> ) <sub>2</sub>	-6.1	2.92	3.19	121.3	110.5	-10.8
Imidazole	-7.9	2.92	3.21	127.8	128.3	0.5
Pyridine	-6.9	2.97	3.28	121.6	121.2	-0.4
Furan	-1.1	3.17	3.29	126.6	94.6	-32.0

Table 2.7	continued -					
HCO●	-5.1	3.83	3.11	141.3	141.5	0.2
$CH_3O^{\bullet}$	-6.9	3.75	3.04	124.2	109.5	-14.7
$H_2PO_4^{-}$	-29.5	2.84	3.00	124.2	96.4	-27.8
$NO_3^-$	-28.2	2.77	3.06	107.1	87.6	-19.5
$\mathrm{Cl}^-$	-30.7	3.36	2.88	_ <sup>a</sup>	-	
$\mathrm{Br}^-$	-28.6	3.54	3.07	_ <sup>a</sup>	-	-
$\mathrm{HCO}_2^-$	-34.7	2.73	3.00	111.2	106.0	-5.2

<sup>a</sup> Br<sup>-</sup> and Cl<sup>-</sup> exhibit degenerate CPs and hence  $\theta$ ,  $\theta'$  and  $\Delta\theta$  could not be calculated.



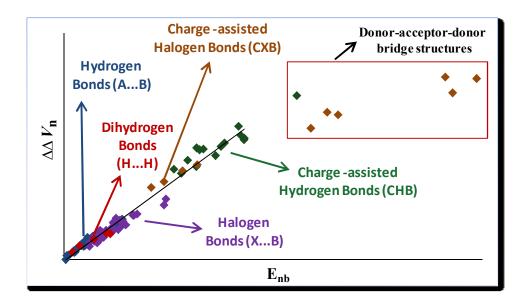
**Figure 2.9** Correlation between MESP  $V_{min}$  at lone pair region and interaction energy of the lone pair- $\pi$  complexes of (a) 2,4,6-trifluoro-1,3,5-triazine (CNF), (b) 1,2,4,5-tetracyanobenzene (TCB) and (c) 1,3,5-trinitrobenzene (TNB).

### **2.5 Conclusions**

Lone pairs play an important role in determining the reactivity, particularly the interactive behavior of molecules with electron-deficient systems. The present study has brought out that MESP topographical analysis provides a simple and effective way to characterize the electron-rich lone pair region of a molecule. The precise location of the MESP minimum can suggest the possible location of the lone pair region and enables a prediction on the orientation of the lone pair bearing molecule when it complexes with an electron-deficient  $\pi$ -system. MESP value of the minimum can be used as a good descriptor to measure the strength of the interaction between the lone pair bearing molecule and an electron-deficient  $\pi$ -system.  $V_{\min}$  provides an *a priori* prediction on the lone pair- $\pi$  interaction energy. The ability of electron-deficient aromatic rings to effectively sense a variety of lone pair bearing species is remarkable and hence highly fluorinated aromatic hydrocarbon moieties could be utilized as synthons in the design of sensors for lone pairs as well as volatile organic compounds in the atmosphere.

# Hydrogen Bonds, Halogen Bonds and Dihydrogen Bonds

Part A – Accurate Binding Energies and Cation Enhanced Binding Strengths & Part B – Molecular Electrostatic Potential Analysis of Hydrogen, Halogen, and Dihydrogen Bonds



## **3.1** ABSTRACT

In part A of this chapter, the interaction energies of 52 noncovalent complexes displaying hydrogen, halogen and dihydrogen bonds in the weak, medium and strong regimes have been computed at MP2, M06L and W1BD methods. Among these methods, the most accurate estimation of the noncovalent bond strength is obtained with WIBD method which shows the lowest mean absolute deviation (MAD) of the bond strength (0.19 kcal/mol) in comparison with the accurate CCSD(T) energy data reported in the literature. Compared to W1BD, MP2 underestimates interaction energies while M06L shows more accurate behavior than MP2 except for halogen and charge-assisted hydrogen bonds. Hybrid methods viz. MP4//MP2, MP4//M06L and CCSD(T)//MP2 yield interaction energies very close to those obtained from WIBD with MAD 0.14 kcal/mol, 0.16 kcal/mol and 0.27 kcal/mol, respectively. Cation complexation (Li<sup>+</sup>,  $NH_4^+$ ) on the electron acceptor site of noncovalent complexes studied using the *MP4//MP2* method shows that the polarization effect of the cation enhances more electron donation from the donor to the noncovalent bonding regions leading to substantial enhancement in the binding energy (~141 to 566 % for  $Li^+$  and ~105 to 539 % for  $NH_4^+$ ). Thus, in the presence of a cation, a noncovalent bond in the weak regime is promoted to the medium regime and that in the medium regime is promoted the strong regime.

In part B of this chapter, the nature of hydrogen bonds, halogen bonds and dihydrogen bonds in a variety of intermolecular donor-acceptor (D-A) complexes has been investigated at high level ab initio MP4//MP2 method coupled with

Atoms in Molecules (AIM) and Molecular Electrostatic Potential (MESP) approaches. Electron density  $\rho$  at bond critical point correlates well with interaction energy  $(E_{nb})$  for each homogeneous sample of complexes, but its applicability to the entire set of complexes is not satisfactory. Analysis of MESP minimum  $(V_{min})$  and MESP at the nuclei  $(V_n)$  shows that in all **D-A** complexes, MESP of A becomes more negative and that of **D** becomes less negative suggesting donation of electrons from **D** to A leading to electron donor-acceptor (eDA) interaction between A and D. MESP based parameter  $\Delta\Delta V_n$  measures donor-acceptor strength of the eDA interactions as it shows a good linear correlation with  $E_{nb}$  for all **D-A** complexes ( $R^2 = 0.976$ ) except the strongly-bound bridged structures. The bridged structures are classified as donor-acceptor-donor complexes. MESP provides a clear evidence for hydrogen-, halogen- and dihydrogen bond formation and defines them as eDA interactions in which hydrogen acts as electron acceptor in hydrogen- and dihydrogen bonds while halogen acts as electron acceptor in halogen bonds.

# Part A – Accurate Binding Energies and Cation Enhanced Binding Strengths

#### **3.2 Introduction**

Hydrogen bonds, halogen bonds and dihydrogen bonds play critical roles in chemical reactivity, molecular recognition, drug-receptor binding, crystal design, selfassembly and in determining biomolecular structure [Fersht 1987; Garrett and Grisham 1995; Jeffrey and Saenger 1994; Mingos and Braga 2004; Rebek et al. 1987; Yap et al. 1995]. These noncovalent interactions have numerous properties running in parallel in terms of strength and directionality [Bent 1968; Desiraju and Parthasarathy 1989; Grabowski 2013; Kovàcs and Varga 2006; Legon 1998; Legon 1999]. Since these interactions exhibit a continuum of strengths [Desiraju 2002; Parthasarathi et al. 2006], an accurate and quantitative account of the geometries and interaction energies is required for a thorough understanding of bonding. The strength of hydrogen bonds, halogen bonds and dihydrogen bonds arise from electrostatics, polarization, charge transfer, exchange-repulsion and dispersion effects and the relative contribution from each term vary depending on the nature of the donor and acceptor molecules involved [Morokuma 1977]. Electrostatic contribution dominates the classical type of hydrogen bonding interaction, while pronounced covalent character is found in strong hydrogen bonding and a dominance of dispersive interaction is observed in weak hydrogen bonds [Gilli and Gilli 2009; Gilli et al. 1994; Grabowski 2011; Grabowski and Sokalski 2005]. Hence, a balanced description of all the bonding components are required for obtaining accurate interaction energies of noncovalent complexes. Advanced quantum mechanical (QM) methods, teamed up with the developments in computer hardware have made it possible to determine noncovalent interaction energies with

accuracy close to experimental results [Müller-Dethlefs and Hobza 2000]. Among the QM methods, density functional theory (DFT) [Hohenberg and Kohn 1964; Kohn and Sham 1965; Parr and Yang 1989] methods provide a good balance between computational cost and accuracy. Performance of DFT methods for the study of noncovalent interactions has been widely discussed and benchmarked [Hobza 2004; Thanthiriwatte et al.; Zhao et al. 2005; Zhao and Truhlar 2005a]. Some improved DFT functionals have been recently developed [Zhao and Truhlar 2004; Zhao and Truhlar 2005b; Zhao and Truhlar 2006; Zhao and Truhlar 2008] to describe noncovalent complexes dominated by the dispersion interactions. In general, almost all the traditional local, non-local and even the highly parameterized exchange-correlation density functionals are unable to give accurate estimation of the energies of dispersion dominated complexes [Janowski and Pulay 2007; Kristyán and Pulay 1994; Perez-Jorda and Becke 1995]. Very recently, Remya and Suresh [Remya and Suresh 2013] have shown that the performance of the Minnesota functional M06L is superior to several other DFT methods implemented in Gaussian09 to obtain accurate geometry and interaction energies of noncovalent intermolecular complexes. High level *ab initio* methods accounting for electron correlation with large basis sets are recommended [Tsuzuki et al. 2000] for noncovalent complexes. Coupled cluster with singles and doubles including perturbative triples or CCSD(T) [Paldus et al. 1972; Pople et al. 1987] method is considered as one of the best methods to achieve chemical accuracy. However, applicability of this method is limited to the study of very small complexes owing to very high computational cost which scales to  $N^7$  where N is the number of basis functions used. Møller-Plesset perturbation theory [Moller and Plesset 1934] to the second order (MP2) is one of the least expensive *ab initio* methods which capture a large portion of the electron correlation energy and scales to the N<sup>5</sup> scale on computational complexity [Raghavachari

and Anderson 1996]. If N<sup>7</sup> complexity is affordable, the method of choice would be the MP4 method [Raghavachari and Pople 1978] which gives accuracy close to CISD.

The main aim of this work is to obtain accurate quantitative data on interaction energies of hydrogen bonds, halogen bonds and dihydrogen bonds in a large variety of intermolecular complexes. The accurate energy data would be useful for future benchmarking of computational methods and also aid in parameterizing molecular mechanics force fields for modeling and simulation studies. Further, the effect of cations on modulating the strength of noncovalent interaction will be assessed. Cations are omnipresent in the environment as well as in the human body and they play vital roles in the structure and function of proteins and nucleic acids as well as in the catalytic processes of enzymes. Rode and coworkers investigated the influence of metal ions on neighboring hydrogen bonds and showed that polarization effects of cations can alter the donor-acceptor interactions in hydrogen bonded systems, influence the binding energies and significantly alter the equilibrium geometry of hydrogen bonds [Limtrakul et al. 1987; Rode 1980; Rode and Sagarik 1982; Sagarik and Rode 1981]. Rode and Sagarik showed that binding of  $Mg^{2+}$  to the O(2) atom of thymine can cause considerable hydrogen bond stabilization of the AóT pair [Sagarik and Rode 1983a; Sagarik and Rode 1983b]. Cations also exhibit crucial influence on the dynamics of proton transfer processes and it has been demonstrated that electrically charged groups in the vicinity of a hydrogen bond can have profound effects on the energetics of proton transfer within that bond, even when the ion is fairly distant from the bond [Szczesniak and Scheiner 1985]. It is well known that coexistence of two interactions can either cause the strengthening of one interaction at the expense of the other or can cause either the strengthening or weakening of both interactions [Alkorta et al. 2010]. In other words, cooperativity effects are present in systems where two or more noncovalent interactions

coexist [Alkorta *et al.* 2010; Frontera *et al.* 2006; Garau *et al.* 2005; Liu and Xu 2011; Mahadevi and Sastry 2014; Vijay *et al.* 2008].

This chapter presents an investigation of the interaction energies of intermolecular complexes of the type **D**-**A** where the bond formation leads to some amount of electron donation from **D** to **A**. The methods selected for the study are W1BD, MP2, M06L and hybrid combinations MP4//MP2, MP4//M06L and CCSD(T)//MP2. The situation where **D**-**A** interaction is perturbed by second noncovalent interaction provided by a cation in the vicinity of **A** (Scheme 3.1) is also probed. A comprehensive investigation of the stabilization effect of monovalent cations *viz*. Li<sup>+</sup> and NH<sub>4</sub><sup>+</sup> in the vicinity of the electron acceptor molecule on the **D**-**A** type noncovalent complexes shows that the interaction of the cation with **A** will have a profound influence on **D** to donate more electrons for the **D**-**A** noncovalent bond formation.

**D**------
$$\mathbf{X}^+$$
   
  $\begin{array}{c} A = electron \ acceptor \\ D = electron \ donor \\ X^+ = Li^+, \ NH_4^+ \end{array}$ 

Scheme 3.1 Effect of cations on the strength of neighboring hydrogen bonds.

### **3.3 Computational Methods**

All noncovalent **D-A** complexes are optimized at W1BD [Barnes *et al.* 2009; Martin and De Oliveira 1999; Parthiban and Martin 2001], MP2 [Moller and Plesset 1934] and M06L [Zhao and Truhlar 2006] methods. W1BD method is a variation of Weizmann-1 theory, where coupled cluster is replaced with Brueckner doubles (BD) method. The algorithm for the calculation of energy in W1BD method includes several computational steps including geometry optimization and frequency calculation at B3LYP/cc-pVTZ+d method followed by an extrapolation scheme comprising of single point calculations at BD(T)/augh-cc-pVDZ+2df, BD(T)/augh-cc-pVTZ+2df, BD/aughcc-pVQZ+2df, BD(T)/MTSmall, BD(T,Full)/MTSmall for getting accurate energies. Strictly speaking W1BD is not an *ab initio* method since its empirical parameter is derived from W2 calculations and not from experiments. It is more expensive, accurate and a recommended method for obtaining very accurate energies [Barnes et al. 2009; Martin and De Oliveira 1999; Parthiban and Martin 2001]. The MP2 is a widely used ab *initio* choice for estimating the interaction energies of hydrogen bonded complexes which is size extensive and gives a good fraction of the correlation energy (80-90%) [Jensen 1999]. M06L is local meta-GGA exchange-correlation functional recommended for thermochemistry, thermochemical kinetics, and noncovalent interactions. Popleøs split-valence triple-zeta basis set, 6-311++G(d,p) [Hehre *et al.* 1986] with polarization and diffuse functions is used on all atoms for MP2 and M06L optimizations. The 6-311++G(d,p) basis set is chosen since it is recommended for obtaining satisfactory geometries at affordable computational cost over the large basis sets with more basis functions [Wiberg 2004]. The BSSE corrected interaction energies are calculated using supermolecule approach. The accuracy of the interaction energies calculated from WIBD, MP2 and M06L methods are assessed by comparing against the CCSD(T) energies available in the literature. Further, MP4 [Raghavachari and Pople 1978] single point energy calculations are performed on the MP2 and M06L optimized geometries. Since MP4 scales the same as CCSD(T) viz.  $N^7$ , CCSD(T) single point energy evaluations on MP2 optimized geometries is also performed. The basis set used for single point calculations is Dunnings augmented correlation-consistent polarized valence triple zeta basis set, aug-cc-pVTZ [Dunning 1989]. The Gaussian09 suite of programs [Frisch et al. 2010] is employed for all the computations. The effect of cations on the strength and nature of all the intermolecular complexes are evaluated by placing monovalent cations  $NH_4^+$  and  $Li^+$  in the vicinity of the electron acceptor molecule without imposing any symmetry constraints. The BSSE corrected interaction energies are calculated using supermolecular approach using the hybrid MP4//MP2 method.

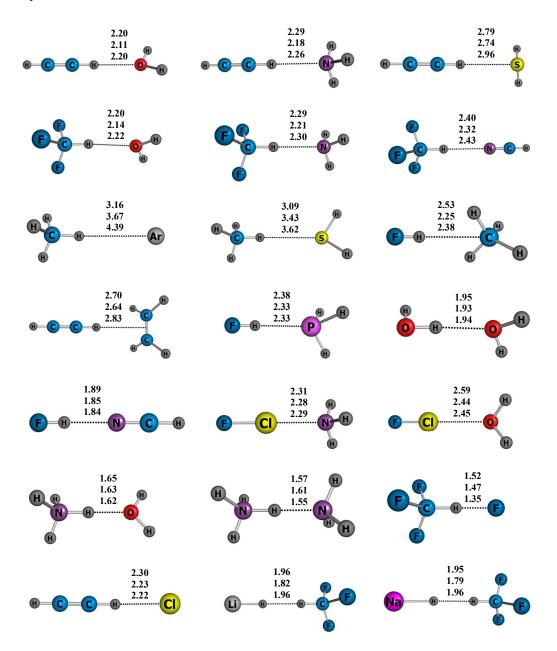
Vibrational frequency analysis is performed on all optimized structures to ensure that each minimum is true containing only positive frequencies.

#### **3.4 Results and Discussion**

#### **3.4.1 Modeling Accurate Interaction Energies**

The selected set of 52 intermolecular complexes includes conventional (possessing N, O, S, P or halogens as electron donors) and nonconventional hydrogen bonds (with C-H groups as electron acceptors and -electrons or carbon as electron donors), charge-assisted hydrogen bonds (CAHB), halogen bonds (XB) and dihydrogen bonds (HH). Charge-assisted hydrogen bonds, characterized by their partial covalent character [Desiraju 2002; Gilli et al. 1994; Madsen et al. 1998; Schiøtt et al. 1998] and very high stabilization energy, have either the donor or acceptor species charged. Dihydrogen bonds can also be considered as unconventional hydrogen bonds established between metal hydrides and proton donors where the metal-hydrogen  $\sigma$ -bond acts as an efficient electron donor. Figure 3.1 shows a representative set of intermolecular complexes selected for this work. The selected data set covers complexes featuring very weak, medium and strong interactions with energies ranging from less than 1 kcal/mol to over 25 kcal/mol. The notations E<sub>MP2</sub>, E<sub>M06L</sub> and E<sub>W1BD</sub> indicate the interaction energies at MP2, M06L and W1BD methods, respectively. The notation  $E_{MP4/MP2}$  represents the interaction energy calculated from MP4 single point calculation on the MP2 geometries,  $E_{MP4/M06L}$  represents the interaction energy calculated from MP4 single point calculation on the M06L geometries and E<sub>CCSD(T)//MP2</sub> represents the interaction energy calculated from CCSD(T) single point calculation on the MP2 geometries. The interactions energies are assessed based on the mean absolute deviation (MAD) of the W1BD energy values from the energies calculated using the tested methods.

Chapter 3



**Figure 3.1** Representative set of intermolecular **D-A** complexes studied. Bond distances at MP2, M06L and W1BD methods (in Å) are given in the order from top to bottom.

The reference CCSD(T) interaction energies collected from literature are represented as  $E_{ref}$ . The  $E_{ref}$ ,  $E_{MP2}$ ,  $E_{MP4//MP2}$ ,  $E_{M06L}$ ,  $E_{MP4//M06L}$ ,  $E_{CCSD(T)//MP2}$  and  $E_{W1BD}$  for hydrogen bond complexes are presented in Table 3.1 and those for halogen and dihydrogen bond complexes are given in Table 3.2. The  $E_{ref}$  values represent an assortment of interaction energies calculated at different optimization levels and different

extrapolation schemes. However,  $E_{ref}$  represent high quality energy data and hence  $E_{ref}$  values are used as reference to assess the accuracy of other methods.

A close analysis of interaction energies indicate that W1BD method performs extremely well for hydrogen, halogen and dihydrogen bonds which are evident from the very close agreement between  $E_{W1BD}$  and  $E_{ref}$  values. Exceptionally good performance is found for hydrogen bonds where  $E_{\rm W1BD}$  vary only ~0.1 kcal/mol from the  $E_{\rm ref}$  for all complexes except Ar...HCH<sub>3</sub> and HF...HCH<sub>3</sub>. In the case of Ar...HCH<sub>3</sub>, E<sub>W1BD</sub> is -0.07 kcal/mol which is significantly smaller than the reported CCSD(T)/CBS interaction energy of -0.40 kcal/mol [Patkowski 2013]. Since these complexes are dispersion dominated, the deviations in  $E_{W1BD}$  from  $E_{ref}$  could possibly indicate a weaker performance of W1BD to model dispersion energies. Deviation in the energy values may also be observed for halogen bonded complexes. However, in the whole data set,  $E_{WIBD}$ only vary < 0.5 kcal/mol from  $E_{ref}$  with two exceptions  $H_3N...ClF$  and  $H_2S...ClF$  where the interaction energy is slightly over estimated compared to the reported CCSD(T)/augcc-pVTZ energy values [Li et al. 2010]. MAD of E<sub>W1BD</sub> from E<sub>ref</sub> is only 0.19 kcal/mol and Figure 3.2 depicts a near perfect linear correlation between them which show that W1BD method is indeed a very good choice for studying the energetics of hydrogen, halogen and dihydrogen bond complexes. Nevertheless, the method becomes prohibitively expensive when the system contains more than 50 electrons. It may be noted that the MAD of  $E_{MP2}$  from  $E_{ref}$  is 0.41 kcal/mol whereas MAD of  $E_{M06L}$  from  $E_{ref}$ is 1.05 kcal/mol. This shows that the performance of MP2 method for modeling the strength of intermolecular noncovalent interactions is fairly good whereas M06L shows larger deviation with respect to the  $E_{ref}$  values. Since  $E_{W1BD}$  agrees very well with  $E_{ref}$  and  $E_{ref}$  values are available only for a limited number of systems, the former is used as a benchmark to compare the performance of MP2 and M06L, MP4//MP2 and MP4//M06L methods.

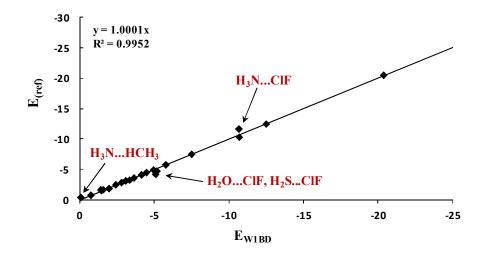
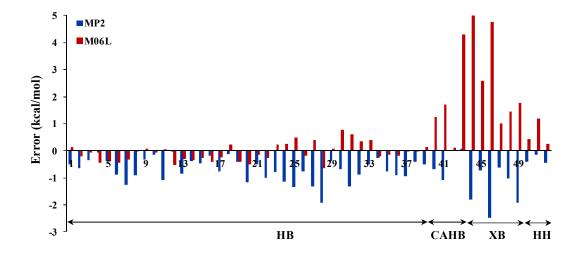


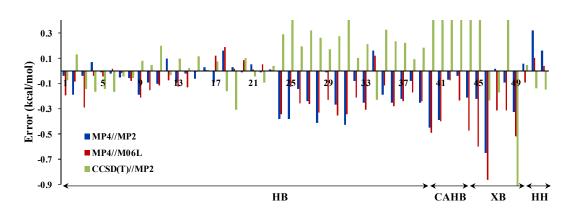
Figure 3.2 Correlation between  $E_{W1BD}$  and  $E_{ref}$  values. All values in kcal/mol.

The accuracy of MP2 energies greatly depend on the choice of basis set used in the calculation. For example, MP2 predicts repulsive interaction for  $H_2S...HCH_3$  and Ar...HCH<sub>3</sub> complexes with E<sub>MP2</sub> 0.04 and 0.05 kcal/mol, respectively using 6-311++G(d,p) basis set whereas it predicts attractive interaction for Ar...HCH<sub>3</sub> with higher basis sets [Parthasarathi et al. 2006]. This also suggest that 6-311++G(d,p) basis set is not quite adequate for studying these type of complexes dominated by dispersion. MAD of E<sub>MP2</sub> from E<sub>W1BD</sub> is 0.41 kcal/mol whereas MAD of E<sub>M06L</sub> from E<sub>W1BD</sub> is 0.81, almost twice that of MP2. The deviation of MP2 and M06L energies with respect to standard W1BD energies for all complexes can be understood from Figure 3.3. It is clear that MP2 underestimates the interaction energies for most of the complexes. The errors of MP2 energies with respect to W1BD energies *i.e.*,  $E_{W1BD}$ - $E_{MP2}$  values are < 1.5 kcal/mol for all neutral hydrogen bonds and dihydrogen bonds except H<sub>2</sub>CO...HF. Larger deviations from W1BD energies are observed for halogen bonds with highest error of -2.5 kcal/mol for  $H_2S...CIF$ . M06L method underestimates the interaction energies for most of the neutral hydrogen bonds with errors <1 kcal/mol, while the energies are overestimated for all charge-assisted hydrogen bonds, halogen bonds and dihydrogen bonds. Maximum deviation is observed for  $H_3N...CIF$ ,  $H_2S...CIF$  and  $F...HCF_3$ . For instance,  $E_{W1BD}$  and  $E_{M06L}$  for  $H_2S...CIF$  is -5.09 and -9.85 kcal/mol, respectively suggesting that the interaction energy is over estimated by 4.76 kcal/mol at M06L level. In general, MP2 underestimates interaction energies while M06L shows more accurate behavior than MP2 except for halogen and charge-assisted hydrogen bonds compared to W1BD.

The MP4 single point calculation on MP2 optimized geometry greatly improves the interaction energy values. For instance, the interaction is attractive in  $H_2S...HCH_3$  and Ar...HCH<sub>3</sub> with E<sub>MP4//MP2</sub> values -0.37 and -0.23 kcal/mol, respectively. MP4 single point calculation on M06L geometries also show remarkable improvement in the interaction energy values. MAD of  $E_{MP4/MP2}$  from  $E_{W1BD}$  is 0.14 kcal/mol and MAD of  $E_{MP4/M06L}$ from  $E_{W1BD}$  is 0.16, respectively. MP4//M06L calculation yields more accurate energies for halogen and charge-assisted hydrogen bonds than M06L. E<sub>M06L</sub> value -9.85 kcal/mol observed for H<sub>2</sub>S...ClF has become -4.23 kcal/mol at MP4//M06L level which is close to  $E_{W1BD}$  value -5.09 kcal/mol. Similarly in the case of H<sub>3</sub>N...ClF,  $E_{MP4/M06L}$  (-10.20 kcal/mol) and E<sub>W1BD</sub> (-10.67 kcal/mol) are in very good agreement compared to E<sub>M06L</sub> (-15.7 kcal/mol). Figure 3.4 presents the errors of E<sub>MP4/MP2</sub>. E<sub>MP4/M06L</sub> and E<sub>CCSD(T)/MP4</sub> with respect to  $E_{W1BD}$ . This figure clearly indicates that upon MP4 single point calculation the errors are scaled down significantly for both MP2 and M06L methods. The largest deviation is shown by FCl...SH<sub>2</sub> complex in both MP4//MP2 and MP4//M06L methods with error values -0.65 and -0.86 kcal/mol respectively. Thus MP4/aug-cc-pvtz single point calculations on MP2/6-311++G(d,p) and M06L/6-311++G(d,p) geometries significantly improve the description of the energetics of the hydrogen, halogen and dihydrogen bonds. CCSD(T) single point energy calculations on MP2 optimized geometries also yields more accurate interaction energy values for hydrogen bonds, halogen bonds and dihydrogen bonds with a MAD of 0.27 from E<sub>W1BD</sub> values. Among the three hybrid methods  $E_{MP4/MP2}$  method emerges the best for the estimation of interaction energies of intermolecular **D-A** complexes with the lowest MAD with respect to the benchmark W1BD energies. Hence geometry optimization at MP2/6-311++G(d,p) level followed by single point MP4 calculation using a higher basis set (aug-cc-pvtz) is suggested as good hybrid method for modeling accurate interaction energies of noncovalent complexes. It is also evident that with a judicious choice of basis set, MP2 is a good choice for the study of **D-A** complexes. BSSE correction must be incorporated in MP2 and MP4 calculations since the calculated BSSE values are substantially large for these methods which agree with the fact that failure in BSSE correction would lead to erroneous conclusions in the study of weak interactions [Zhu *et al.* 2000]. M06L optimizations though insufficient for halogen and charge-assisted hydrogen bonds can yield good interaction energies for noncovalent complexes when coupled with MP4 single point calculation. MP4//M06L method can be thus considered as a good *ab initio*-DFT hybrid method for studying the energetics of hydrogen bonds, halogen bonds and dihydrogen bonds.



**Figure 3.3** Comparison of energy errors of MP2 and M06L methods with respect to W1BD method.

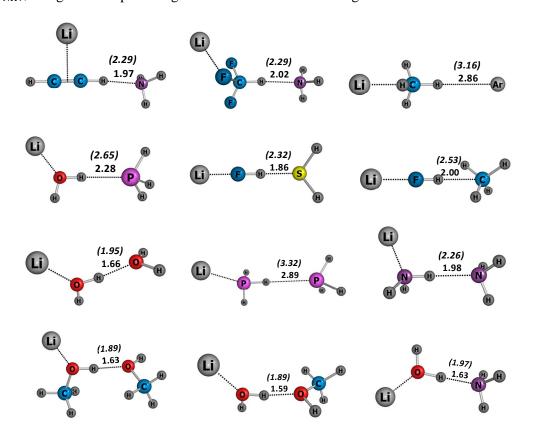


**Figure 3.4** Comparison of energy errors of MP4//MP2, MP4//M06L and CCSD(T)//MP2 methods with respect to W1BD method.

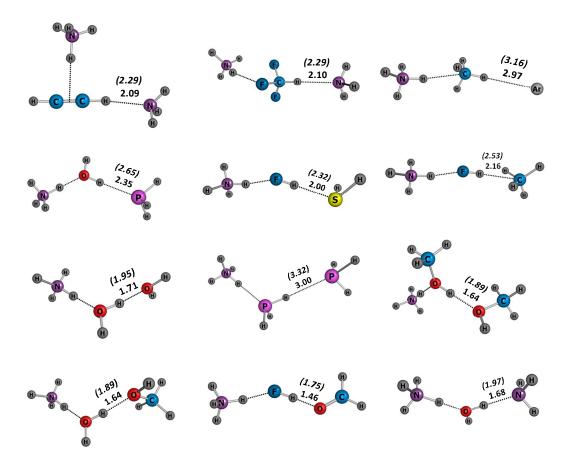
#### 3.4.2 Cation Enhanced Binding Strengths

The presence of cations viz. Li<sup>+</sup> and NH<sub>4</sub><sup>+</sup> in the vicinity of the electron acceptor molecule of hydrogen bonds, halogen bonds and dihydrogen can have two possible effects on the interaction between the electron donor and the acceptor; one in which interaction is strengthened and the other in which the cation disrupts the interaction either by interfering in the intermolecular interaction or by nucleophilic attack. In many hydrogen bonded complexes, the cation directly interacts with the electron acceptor leading to significant stabilization of the interactions. These complexes are characterized by higher interaction energies and shorter interaction distances. In certain cases, the minimal energy structures correspond to sandwich complexes of the type D...X...A, where the cation interacts with both the donor and acceptor. For instance the proximity of Li<sup>+</sup> and NH<sub>4</sub><sup>+</sup> with H<sub>2</sub>O...HCCH lead to H<sub>2</sub>O...Li<sup>+</sup>...HCCH and H<sub>2</sub>O...NH<sub>4</sub><sup>+</sup>...HCCH complexes, respectively. In a relatively fewer number of complexes particularly in halogen bonded complexes, the minimum energy structure correspond to the nucleophilic attack of the cation with one of the atoms of the electron acceptor. However, because the ultimate aim is to study cation enhanced bond strengths, the focus is on those geometries where the intermolecular interactions are not disturbed but strengthened by the presence

of the cation. The Li<sup>+</sup> and NH<sub>4</sub><sup>+</sup> adducts are designated as D...A...Li<sup>+</sup> and D...A...NH<sub>4</sub><sup>+</sup> respectively. The notations  $E_{Li^+}$  and  $E_{NH4^+}$  represent the Li<sup>+</sup> and NH<sub>4</sub><sup>+</sup> enhanced interaction energies and D<sub>Li^+</sub> and D<sub>NH4+</sub> represent the corresponding intermolecular hydrogen bond distances. Figure 3.5 and Figure 3.6 presents the geometries of a representative set of D...A...Li<sup>+</sup> and D...A...NH<sub>4</sub><sup>+</sup> complexes. The  $E_{Li^+}$ ,  $E_{NH4^+}$ ,  $D_{Li^+}$  and  $D_{NH4^+}$  along with the percentage increase in interaction energies are listed in Table 3.3.



**Figure 3.5** Optimized geometries of representative D...A...Li<sup>+</sup> complexes along with the hydrogen bond distances in . Hydrogen bond distances of the corresponding **D-A** complexes are given in parentheses.



**Figure 3.6** Optimized geometries of representative  $D...A...NH_4^+$  complexes along with the hydrogen bond distances in  $A...NH_4^+$ . Hydrogen bond distances of the corresponding **D-A** complexes are given in parentheses.

The cation enhanced interaction energies are measured in terms of net stabilization energy (NSE) which is the difference between interaction energies before and after complexing the cation;  $NSE_{Li+}$  and  $NSE_{NH4+}$  represent the net stabilization energies on complexation with Li<sup>+</sup> and  $NH_4^+$  respectively (Table 3.3).

 $E_{Li+,}$  and  $E_{NH4+}$  values are significantly higher than the corresponding energy values in all **D-A** complexes which indicate the stabilization effect of metal ions in their neighborhood. The stabilization effect of cations is also evident from the shortening of the intermolecular hydrogen bond distances observed in all the cases. The NSE values ranges from 0.32 to 19.44 kcal/mol in Dí Aí Li<sup>+</sup> complexes with an average shortening

of ~ 0.38 in the intermolecular hydrogen bond distances. The ternary complex, Ar...HCH<sub>3</sub>...Li<sup>+</sup> ( $E_{Li+} = -0.55$  kcal/mol) is about 2.4 times more stable than Ar...HCH<sub>3</sub> complex ( $E_{int} = -0.23$  kcal/mol). Here, the C-H...Ar distance is shortened by 0.31 . The cation induced enhancement in interaction energy is more pronounced in the weak homodimer H<sub>3</sub>P...H<sub>3</sub>P which show a 6.7 fold increase in interaction energy and a shortening in hydrogen bond distance by 0.31 on the proximity of Li<sup>+</sup>. The NSE is the highest for HCN...HF...Li<sup>+</sup> (NSE <sub>Li+</sub> = 19.77 kcal/mol) and lowest for, Ar...HCH<sub>3</sub>...Li<sup>+</sup> (NSE <sub>Li+</sub> = 0.32 kcal/mol).

The stabilization effect of  $NH_4^+$  on hydrogen bond strength is relatively less compared to Li<sup>+</sup>. The NSE of D...A...NH<sub>4</sub><sup>+</sup> complexes ranges from 0.24 kcal/mol to 12.26 kcal/mol and the average shortening of the hydrogen bonds distances is 0.28 . While the interaction of Li<sup>+</sup> with H<sub>3</sub>N...H<sub>3</sub>N has considerable stabilization effect on the strength of the hydrogen bond with a NSE of 10.24 kcal/mol, the interaction of NH<sub>4</sub><sup>+</sup> with H<sub>3</sub>N...H<sub>3</sub>N disrupts the hydrogen bonded NH<sub>3</sub> dimer and forms a much stronger H<sub>3</sub>Ní HNH<sub>3</sub><sup>+</sup>...NH<sub>3</sub> complex. The NSE values of ternary D...A...NH<sub>4</sub><sup>+</sup> complexes follow the same trend as in the D...A...Li<sup>+</sup> complexes with the highest NSE for HCN...HF...NH<sub>4</sub><sup>+</sup> (NSE<sub>Li+</sub> = 13.05 kcal/mol) and lowest for Ar...HCH<sub>3</sub>...NH<sub>4</sub><sup>+</sup> (NSE <sub>Li+</sub> = 0.24 kcal/mol). The stabilization effect of Li<sup>+</sup> and NH<sub>4</sub><sup>+</sup> on CH... interaction is also investigated by using the prototype C<sub>6</sub>H<sub>6</sub>...CH<sub>4</sub> dimer. The NSE for C<sub>6</sub>H<sub>6</sub>...CH<sub>4</sub>...Li<sup>+</sup> and C<sub>6</sub>H<sub>6</sub>...CH<sub>4</sub>...NH<sub>4</sub><sup>+</sup> are 5.72 and 3.61 kcal/mol, respectively which signify substantial strengthening of the interaction. Thus, the interaction energies, NSE values and the interaction distances indicate that polarization effects of the cations can lead to substantial increase in the strength of hydrogen bonds.

**Table 3.1** Interaction energies of hydrogen bond complexes calculated at M06L ( $E_{M06L}$ ), MP4//M06L ( $E_{MP4//M06L}$ ), MP2 ( $E_{MP2}$ ), MP4//MP2 ( $E_{CCSD(T)//MP2}$ ), W1BD ( $E_{W1BD}$ ), and reference CCSD(T) ( $E_{ref}$ ) methods in kcal/mol. Reference corresponding to  $E_{ref}$  values also provided.

SI.No.	Complex	E <sub>M06L</sub>	E <sub>MP4//M06L</sub>	$E_{MP2}$	E <sub>MP4//MP2</sub>	E <sub>CCSD(T)</sub> //MP2	$E_{W1BD} \\$	E <sub>ref</sub>
1	H <sub>3</sub> NHCCH	-3.77	-3.45	-3.15	-3.60	-3.71	-3.64	-3.60 [Liu and Xu 2011]
2	H <sub>2</sub> SHCCH	-1.37	-1.50	-0.95	-1.40	-1.46	-1.59	
3	H <sub>2</sub> OHCCH	-2.73	-2.51	-2.46	-2.76	-2.94	-2.80	-2.85 [ ezá et al. 2011]
4	HCNHCCH	-2.06	-2.46	-2.43	-2.57	-2.67	-2.50	
5	H <sub>3</sub> CCNHCCH	-2.71	-3.04	-2.71	-3.08	-3.23	-3.09	
6	H <sub>2</sub> COHCCH	-2.59	-3.06	-2.17	-3.02	-3.21	-3.04	
7	HFHCCH	-4.05	-4.37	-3.14	-4.34	-4.43	-4.39	
8	HClHCCH	-2.81	-2.75	-1.91	-2.78	-2.88	-2.83	
9	H <sub>3</sub> NHCF <sub>3</sub>	-4.38	-4.10	-3.99	-4.12	-4.23	-4.31	
10	H <sub>2</sub> OHCF <sub>3</sub>	-3.38	-3.29	-3.30	-3.35	-3.39	-3.44	
11	H <sub>2</sub> SHCF <sub>3</sub>	-2.22	-2.06	-1.09	-2.07	-1.97	-2.17	
12	HCNHCF <sub>3</sub>	-2.68	-3.12	-3.18	-3.30	-3.23	-3.20	
13	HClHCF <sub>3</sub>	-1.68	-1.83	-1.12	-1.87	-1.86	-1.96	

Tab	le 3.1 continued							
14	H <sub>3</sub> NHCH <sub>3</sub>	-0.40	-0.62	-0.36	-0.73	-0.73	-0.75	-0.77 [MacKie and DiLabio 2011]
15	$H_2SHCH_3$	-0.17	-0.42	0.04	-0.37	-0.31	-0.43	
16	H <sub>3</sub> CCNHCH <sub>3</sub>	-0.27	-0.67	-0.48	-0.70	-0.67	-0.67	
17	HFHCH <sub>3</sub>	-1.18	-1.53	-0.65	-1.32	-1.34	-1.41	-1.64 [MacKie and DiLabio 2011]
18	ArHCH <sub>3</sub>	-0.30	-0.26	0.05	-0.23	-0.23	-0.07	-0.40 [Patkowski 2013]
19	$C_2H_2C_2H_2$	-1.03	-1.47	-1.05	-1.48	-1.76	-1.45	-1.52 [ ezá et al. 2011]
20	HFC <sub>2</sub> H <sub>4</sub>	-3.98	-4.56	-3.30	-4.47	-4.38	-4.48	-4.50 [MacKie and DiLabio 2011]
21	$H_3P$ $H_2O$	-2.26	-2.43	-1.93	-2.47	-2.47	-2.42	-2.49 [Lane and Kjaergaard 2009]
22	H <sub>2</sub> COH <sub>2</sub> O	-4.85	-5.16	-4.13	-5.10	-5.20	-5.11	
23	H <sub>3</sub> PHF	-4.99	-4.76	-3.95	-4.76	-4.71	-4.75	
24	$H_2O$ $HF$	-8.94	-8.35	-7.55	-8.31	-8.40	-8.69	
25	$H_2SHF$	-5.53	-4.91	-3.71	-4.66	-4.56	-5.04	
26	HCNHF	-7.32	-7.24	-6.73	-7.36	-7.30	-7.50	-7.49 [MacKie and DiLabio 2011]
27	H <sub>3</sub> NHF	-12.90	-12.24	-11.18	-12.26	-12.18	-12.50	-12.45 [Botschwina and Oswald 2005]
28	H <sub>2</sub> COHF	-7.66	-7.99	-6.40	-7.91	-8.05	-8.32	
29	NCHHCl	-4.74	-4.42	-4.26	-4.64	-4.48	-4.65	
30	H <sub>2</sub> OHCl	-6.14	-5.00	-4.68	-5.08	-5.07	-5.35	

Tal	ble 3.1 continued							
31	H <sub>2</sub> SHCl	-3.94	-3.01	-2.04	-2.92	-2.82	-3.35	-3.26 [Pernal <i>et al</i> .]
32	PH <sub>3</sub> HCl	-3.43	-2.87	-2.20	-3.00	-2.98	-3.08	
33	$OH_2OH^E$	-6.04	-5.33	-5.13	-5.39	-5.43	-5.64	
34	PH <sub>3</sub> PH <sub>3</sub>	-0.25	-0.58	-0.18	-0.62	-0.69	-0.46	
35	$H_2SH_2S$	-1.43	-1.46	-0.80	-1.38	-1.24	-1.57	-1.68 [Mintz and Parks 2012]
36	CH <sub>3</sub> HOHOCH <sub>3</sub>	-5.59	-5.49	-4.85	-5.52	-5.54	-5.77	-5.76 [ ezá et al. 2011]
37	HClHCl	-1.94	-1.72	-1.03	-1.74	-1.74	-1.96	-1.85 [Tuma et al. 1999]
38	$H_3NH_3N$	-3.06	-2.92	-2.69	-3.01	-3.00	-3.09	-3.13 [ ezá and Hobza 2013]
39	$H_2O$ $H_2O$	-5.08	-4.71	-4.45	-4.70	-4.77	-4.95	-4.92 [ ezá et al. 2011]
40	$H_2ONH_4^+$	-21.62	-19.89	-19.72	-19.93	-20.61	-20.38	-20.45 [Boese et al. 2007]
41	$H_3NNH_4^+$	-27.87	-25.75	-25.07	-25.76	-26.32	-26.15	
42	CI HCCH	-10.81	-10.63	-10.70	-10.63	-10.26	-10.70	-10.29 [Botschwinaa and Oswald 2002
43	F HCF <sub>3</sub>	-30.13	-25.61	-25.93	-25.80	-26.84	-25.84	

**Table 3.2** Interaction energies of halogen and dihydrogen bond complexes calculated at M06L ( $E_{M06L}$ ), MP4//M06L ( $E_{MP4//M06L}$ ), MP2 ( $E_{MP2}$ ), MP4//MP2 ( $E_{MP4//MP2}$ ), CCSD(T)//MP2 ( $E_{CCSD(T)//MP2}$ ), W1BD ( $E_{W1BD}$ ), and reference CCSD(T) ( $E_{ref}$ ) methods in kcal/mol. Reference corresponding to  $E_{ref}$  values also provided.

SI.No.	Complex	$E_{M06L}$	EMP4//M06L	E <sub>MP2</sub>	E <sub>MP4//MP2</sub>	E <sub>CCSD(T)//MP2</sub>	$E_{W1BD} \\$	E <sub>ref</sub>
44	H <sub>3</sub> NClF	-15.71	-10.20	-8.86	-10.46	-9.09	-10.67	-11.64 [Hill and Hu 2013]
45	H <sub>2</sub> OClF	-7.76	-4.57	-4.43	-4.95	-4.53	-5.17	- 4.73 [Li et al. 2010]
46	H <sub>2</sub> SClF	-9.85	-4.23	-2.61	-4.44	-3.75	-5.09	- 4.20 [Li et al. 2010]
47	HCNCIF	-5.96	-4.64	-4.33	-4.97	-4.32	-4.95	
48	H <sub>3</sub> CCNClF	-7.57	-5.80	-5.09	-6.02	-5.30	-6.11	
49	H <sub>2</sub> COClF	-7.70	-5.43	-4.02	-5.62	-5.06	-5.94	
50	LiHHCF <sub>3</sub>	-6.45	-5.92	-5.59	-6.06	-5.96	-6.01	
51	NaHHCF <sub>3</sub>	-7.45	-6.36	-6.11	-6.57	-6.39	-6.26	
52	LiHHCCH	-4.38	-4.18	-3.7	-4.30	-4.29	-4.14	-4.12 [Cybulski et al. 2003]

**Table 3.3** Energetic and geometric features of D...A...Li<sup>+</sup> and D...A...NH<sub>4</sub><sup>+</sup> complexes.  $E_{int}$  and D are the interaction energies and interaction energies and interaction distances of D-A complexes.  $E_{Li^+}$ ,  $E_{NH4^+}$ ,  $D_{Li^+}$  and  $D_{NH4^+}$  are the interaction energies and interaction distances of D...A...Li<sup>+</sup> and D...A...NH<sub>4</sub><sup>+</sup> complexes and NSE<sub>Li^+</sub> and NSE<sub>NH4+</sub> represent the corresponding stabilization energies. Energy values in kcal/mol and distances in units.

Complex	E <sub>int</sub>	D	$E_{Li^+}$	NSE <sub>Li+</sub>	D <sub>Li+</sub>	E <sub>NH4+</sub>	NSE <sub>NH4+</sub>	D <sub>NH4+</sub>
Complex	(kcal/mol)	( )	(kcal/mol)	(kcal/mol)	( )	(kcal/mol)	(kcal/mol)	( )
ArHCH <sub>3</sub>	-0.23	3.164	-0.55	0.32	2.858	-0.47	0.24	2.971
H <sub>3</sub> NHCCH	-3.60	2.291	-12.81	9.21	1.974	-10.37	6.77	2.091
H <sub>3</sub> NHCF <sub>3</sub>	-4.12	2.291	-13.02	8.90	2.021	-10.29	6.17	2.097
C <sub>6</sub> H <sub>6</sub> CH <sub>4</sub>	-1.58	2.575	-7.30	5.72	2.276	-5.20	3.61	2.378
$H_3P$ $H_2O$	-2.47	2.649	-10.94	8.47	2.276	-8.62	6.15	2.345
$H_2SHF$	-4.66	2.321	-17.66	12.99	1.858	-12.91	8.25	2.003
H <sub>2</sub> COHF	-7.91	1.759	-26.26	18.36	1.327	-20.17	12.26	1.462
HClHCl	-1.74	2.666	-6.84	5.10	2.218	-5.16	3.42	2.380
$H_2SH_2S$	-1.38	2.837	-6.19	4.81	2.489	-5.19	3.81	2.592
$H_2O$ $H_2O$	-4.70	1.950	-16.52	11.82	1.660	-13.88	9.18	1.710
H <sub>3</sub> PH <sub>3</sub> P	-0.62	3.321	-4.13	3.51	2.890	-3.22	2.60	2.996

Table 3.3 continued								
$H_3NH_3N$	-3.01	2.263	-13.25	10.24	1.976	-19.25	16.24	1.750
NCHHCl	-4.64	2.106	-18.12	13.48	1.630	-14.12	9.48	1.793
H <sub>2</sub> OHF	-8.31	1.732	-26.29	17.98	1.349	-20.23	11.93	1.468
H <sub>2</sub> OHCl	-5.08	1.902	-17.95	12.87	1.450	-13.95	8.87	1.638
CH <sub>3</sub> HOHOCH <sub>3</sub>	-5.52	1.886	-17.54	12.02	1.628	-15.22	9.70	1.644
HFHCF <sub>3</sub>	-1.32	2.531	-6.40	5.08	2.000	-4.24	2.92	2.157
H <sub>2</sub> OHOCH <sub>3</sub>	-5.40	1.894	-18.83	13.43	1.593	-15.62	10.22	1.641
$H_3PH_2S$	-1.47	2.949	-6.89	5.43	2.534	-5.33	3.87	2.648
HCNHF	-7.36	1.889	-26.80	19.44	1.445	-20.40	13.05	1.572
$H_3N$ $H_2O$	-5.77	1.974	-21.37	15.60	1.627	-17.73	11.96	1.680
LiHHCF <sub>3</sub>	-6.06	1.956	-20.26	14.20	1.563	-18.88	12.82	1.682

# Part B Molecular Electrostatic Potential Analysis of Hydrogen, Halogen, and Dihydrogen Bonds

### **3.5 Introduction**

Hydrogen bonding is one of the most important, widely discussed and highly debated interactions in chemistry [Buckingham et al. 1988; Desiraju 2002; Gilli and Gilli 2000; Gilli and Gilli 2009; Gilli et al. 1994; Gotch and Zwier 1990; Grabowski 2001; Grabowski 2004; Grabowski 2011; Kollman et al. 1975; Morokuma 1977; Müller-Dethlefs and Hobza 2000]. Desiraju [Desiraju 2002] described it as an 'interaction without borders' to express the large variations in covalent, electrostatic, and van der Waals energy components of a hydrogen bond. Despite the extensive research over years, the perception of hydrogen bonds continues to evolve and a universally accepted definition of hydrogen bond remains elusive in the literature. A task group of IUPAC has reviewed this topic in depth based on theoretical and experimental knowledge acquired over the past century and proposed a short modern definition for it [Arunan et al. 2011; Desiraju et al. 2013]. Halogen bonds are highly directional noncovalent interactions that occur between an electron donor and a halogen atom in another molecule. Detailed report of IUPAC recommendations for defining hydrogen bonds and halogen bonds is provided in Chapter 1. Politzer et al. [Brinck et al. 1992; Brinck et al. 1993; Clark et al. 2007; Murray et al. 1994; Politzer et al. 2013] demonstrated that halogen bond is an electrostatically-driven interaction between positive  $\sigma$ -hole (a region of positive electrostatic potential on the outer side of the halogen) of the halogen and the negative potential of the base. Crabtree and coworkers [Crabtree et al. 1996] showed that hydrogen atom in metal hydrides and  $H_3NBH_3$  can form unusual hydrogen bonding interaction with a hydrogen atom in another molecule. The resulting H...H interactions are called dihydrogen bonds. In systems showing hydrogen bonds, halogen bonds and dihydrogen bonds, one atom in the bonded region accepts electron density from the other [Jonas *et al.* 1994; Mulliken and Person 1969; Ratajczak and Orville-Thomas 1980] and hence these interactions can be viewed as interaction between a Lewis base acting as electron donor (**D**) and a Lewis acid acting as electron acceptor (**A**).

Baderøs 'Atoms in Molecules' (AIM) [Bader 1985; Bader 1990; Bader 1991] and molecular electrostatic potential (MESP) [Murray et al. 1994; Politzer et al. 1985; Pullman 1990; Sen and Politzer 1989; Sjoberg and Politzer 1990] analyses are important theoretical tools for eliciting noncovalent interactions. Numerous studies [Knop et al. 2003; Koch and Popelier 1995; Parthasarathi et al. 2006; Popelier 1998; Popelier and Logothetis 1998; Suresh et al. 2009] have shown that AIM topological parameters viz. electron density ( $\rho$ ) at the bond critical point (bcp) and its Laplacian ( $\nabla^2 \rho$ ) are important quantities to characterize the strength and nature of hydrogen bonds, halogen bonds and dihydrogen bonds. There have been various reports [Grabowski 2001; Knop et al. 2003; Parthasarathi et al. 2006; Popelier 1998; Popelier and Logothetis 1998; Suresh et al. 2009] where  $\rho$  correlates with the interaction energy and length of the hydrogen bond. Sathyamurthy [Parthasarathi et al. 2006] et al. attempted to understand the concept of hydrogen bonding without borders using the topological properties of electron density and showed that the electron density at the hydrogen bond critical point increases approximately linearly with increasing stabilization energy in going from weak to moderate and strong hydrogen bonds. The most negative valued MESP point of a molecule, designated as  $V_{\min}$  symbolizes the sites of electron localization in a molecule [Mathew and Suresh 2010; Suresh and Gadre 2007] and has been used successfully in predicting the sites and directionality of hydrogen bonds in a variety of systems [Bobadova-Parvanova and Galabov 1998; Gadre and Bhadane 1997; Gadre and Pundlik 1997; Galabov and Bobadova-Parvanova 1999; Kollman *et al.* 1975; Leroy *et al.* 1976; Politzer and Murray 1991]. Kollman *et al.* [Kollman *et al.* 1975] showed the existence of good correlation between hydrogen bond energies and the magnitude of MESP at fixed distance from the proton acceptors in a series of complexes between HF and various acceptors. Recently, in a series of works [Bobadova-Parvanova and Galabov 1998; Dimitrova *et al.* 2002; Dimitrova *et al.* 2003; Galabov and Bobadova-Parvanova 1999; Galabov *et al.* 2003] Galabov *et al.* showed that MESP at the site of electron donor atom could be successfully used as reactivity descriptor for the study of hydrogen bonding. However, most of these works consider hydrogen bond complexes with either donor or acceptor molecules fixed and hence the applicability of these parameters for a heterogeneous sample of complexes with different proton donors and/or acceptors is limited.

In this chapter it is shown that for a large variety of intermolecular hydrogen bonds, halogen bonds and dihydrogen bonds, a simple definition suggesting them as electron donor-acceptor (eDA) interaction holds good. The results are based on high level *ab initio* interaction energy data and topographical features of  $\rho$  distribution and MESP. The value of  $\rho$  at bcp,  $V_{min}$  and  $V_n$  are used as electronic descriptors to quantify the strength and characteristics of eDA interactions of a large variety of complexes. Among  $\rho$ ,  $V_{min}$  and  $V_n$ , the last quantity is highly suited to measure the electron donating power of donor as well as electron accepting power of acceptor. A strong correlation between interaction energy and donor-acceptor strength is obtained for all the complexes which prove that they all belong to the same class, eDA complex.

#### **3.6 Computational Methods**

The interaction energies of all D-A complexes are calculated using the hybrid MP4//MP2 method recommended in Part A of this chapter. Gaussian 09 suite of programs [Frisch et al. 2010] is employed for all the computations. The topological properties of electron density at bond critical points (bcp) have been studied using AIM methodology with AIM2000 program [Biegler-König and Schönbohm 2002; Biegler-König et al. 2001]. MESP topographical analysis of the monomers and the intermolecular complexes are carried out at MP4/aug-cc-pvtz level. MESP,  $V(\mathbf{r})$  at any point with the position vector  $\mathbf{r}$  can be calculated using the equation 1.67 given in Chapter 1.  $V(\mathbf{r})$  is strongly dependent on the local charges around point  $\mathbf{r}$ , the positive charges on the neighboring nuclei, and the electron density in closer vicinity of point **r**.  $V_{\rm min}$  have been located for the donor and acceptor molecules in their isolated and bound state in the noncovalent complex. MESP at the nuclei  $(V_n)$  of the atoms participating in the nonbonded interactions is also evaluated using equation 1.68 (Chapter 1). The nuclei centered quantity,  $V_{\rm n}$  measures the electrostatic potential at the position of the atom 'n' due to all the electrons and rest of the nuclei. It is a local molecular property associated with the particular atom center. MESP at each atom of the donor and acceptor molecules is obtained from the standard output of the Gaussian09 program.

#### **3.7 Results and Discussion**

The set of intermolecular noncovalent complexes studied in Part A is of this chapter expanded to a total of 104 complexes that are classified into four categories, *viz.* (i) hydrogen bonds in neutral complexes (A...B), (ii) charge-assisted hydrogen bonds (CHB), (iii) halogen bonds (X...B), (iv) charge-assisted halogen bonds (CXB) and (v) dihydrogen bonds (H...H). The category A...B includes complexes where both donor and acceptor molecules are neutral; it has three subclasses: C-H...Y (hydrogen bonds

formed between C-H of  $C_2H_2$ ,  $CF_3H$  and  $CH_4$  and conventional electron donor molecules), X-H... (hydrogen bonds where the electron donor is a -system) and X-H...Y (hydrogen bonds with HCl, HF, H<sub>2</sub>O, PH<sub>3</sub>, H<sub>2</sub>S, CH<sub>3</sub>OH and HBr as electron donors/acceptors) complexes. The halogen bonded complexes of diatomic interhalogen compounds IF, ICl, IBr, CIF, BrF and BrCl with Lewis bases H<sub>2</sub>S, NH<sub>3</sub>, H<sub>2</sub>O, HCN, NCCH<sub>3</sub> an OCH<sub>2</sub> are studied. CHB and CXB includes noncovalent complexes connected through relatively strong hydrogen bonds and halogen bonds, respectively where either the donor or acceptor species is charged *i.e.*, hydrogen/halogen bonds in anionic systems and cationic systems. These bonds are characterized by their partial covalent character [Desiraju 2002; Gilli et al. 1994; Madsen et al. 1998; Schiøtt et al. 1998]. Dihydrogen bond complexes of BeH<sub>2</sub>, LiH, NaH and BH<sub>4</sub> as electron donors with different electron acceptors are also included. Enb represents the interaction energy calculated at MP4//MP2 method and the standard notations  $\rho$  and  $\nabla^2 \rho$  are used to indicate the electron density at the bond critical point (bcp) of the electron donoracceptor bond and the Laplacian of the electron density at the bcp. The accuracy of  $E_{nb}$ calculated with MP4//MP2 method is very close to the 'gold standard' CCSD(T)

**3.7.1 Electron Density Analysis** 

complexes along with  $\rho$  and  $\nabla^2 \rho$  at bcp.

The values of  $\rho$  and  $\nabla^2 \rho$  at bcp for H...H and most of the A...B complexes fall in the typical range [Koch and Popelier 1995] proposed for  $\rho$  (0.002 ó 0.035 au) and  $\nabla^2 \rho$ (0.024 ó 0.139 au). However, for most of XB, CHB and CXB complexes, higher values of  $\rho$  and  $\nabla^2 \rho$  are observed indicating the presence of remarkably stronger interactions.

benchmark values available in the literature with mean absolute deviation 0.25 kcal/mol.

The  $E_{nb}$  values range from < 1 kcal/mol to 59 kcal/mol and covers very weak, medium

and strong interactions. Table 3.4 presents the E<sub>nb</sub> values of a representative set of

Nonetheless, except H<sub>3</sub>O<sup>+</sup>...H<sub>2</sub>O, all other **D-A** systems exhibit typical closed-shell interactions by virtue of their positive  $\nabla^2 \rho$  values. H<sub>3</sub>O<sup>+</sup>...H<sub>2</sub>O represent a Zundel ion [Schuster *et al.* 1976] and have  $\nabla^2 \rho$  value of -0.564 au which is characteristic of a bond with covalent nature. Anionic CXB complexes *viz*. F ...IF, F ...BrF, Cl ...IF, Cl ...BrF, F ...IBr and Cl ...IBr are characterized by bridged structures and exceptionally high interaction energy values which fall in the range of 35 to 59 kcal/mol (Figure 3.7). For instance, in the case of F ...IF, the position of I is symmetric with respect to both the F atoms meaning that the complex is a resonance combination of F ...IF and F...IF . Similar bonding scenario is seen in F ...BrF, Cl ...IF, Cl ...BrF, F ...IBr and Cl ...IBr. The cationic complex H<sub>3</sub>O<sup>+</sup>...H<sub>2</sub>O also exhibits a bridged configuration (H<sub>2</sub>O...H<sup>+</sup>...OH<sub>2</sub>) with the H<sup>+</sup> placed at 1.19 and 1.20 from each of the two H<sub>2</sub>O molecules (Figure 3.7).

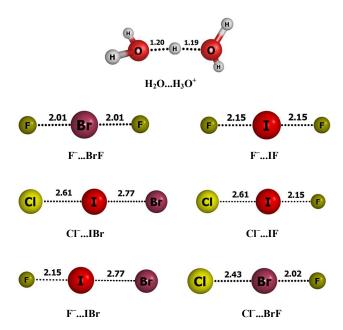
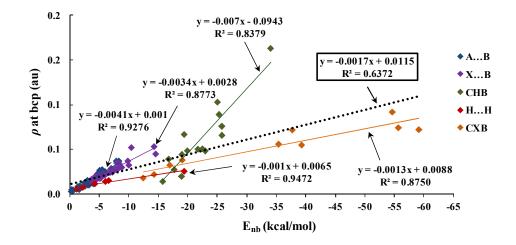
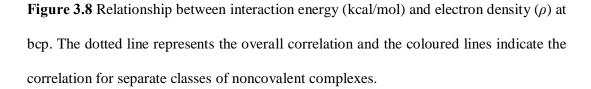


Figure 3.7 D-A complexes showing bridged configurations. Bond distances in Å.

It is well established that the topological parameters at bcp correlate with  $E_{nb}$  for a variety of noncovalent complexes. Sathyamurthi *et al.* [Parthasarathi *et al.* 2006] used a set of intermolecular complexes of varying strengths from van der Waals to covalent

limit and showed a linear relationship between  $\rho$  and  $E_{nb}$  as well as  $\nabla^2 \rho$  and  $E_{nb}$ . They also demonstrated a smooth change in the nature of the noncovalent interaction from van der Waals to classical hydrogen bonding and strong hydrogen bonding. Figure 3.8 depicts the relationship between interaction energy and electron density at bcp for all **D-A** complexes.





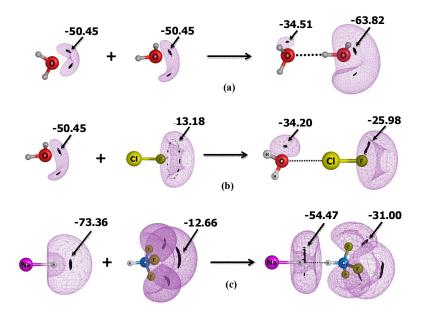
The correlation between  $\rho$  and  $E_{nb}$  is very good for each homogenous sample of complexes. However, for the heterogeneous sample of complexes comprising of neutral (Aí B), halogen bonded (X...B), dihydrogen bonded (Hí H) and charge-assisted hydrogen bonded (CHB) and charge-assisted halogen bonded (CXB) systems (Figure 3.7), the correlation is found to be poor ( $R^2 = 0.64$ ). For instance, in A...B complexes  $E_{nb}$  vs  $\rho$  correlation holds good with  $R^2$  value of 0.927. Likewise, satisfactory correlations exist for X...B, CHB, CXB and H...H bonds too with the  $R^2$  values 0.877, 0.837, 0.875 and 0.947, respectively. Thus, although  $\rho$  at bcp correlates reasonably well with  $E_{nb}$  for each homogenous sample of intermolecular complexes, its applicability for the whole set

is not satisfactory. These results clearly suggest that the applicability of AIM parameters is not quite adequate to describe a large variety of complexes on a uniform scale [Grabowski 2001].

#### **3.7.2 Molecular Electrostatic Potential Analysis**

The recent IUPAC recommendations gives emphasis on the key words 'attractive interaction' and 'evidence of bond formation' to define a hydrogen bonds or a halogen bond. Since bonding unequivocally means an attractive interaction, proving the bond formation with proper 'evidence' attains paramount importance. An attractive or repulsive interaction is bound to change the  $\rho$  distribution and hence a quantity directly related and very sensitive to  $\rho$  and amenable to experimental determination is highly useful to discover the bond formation. MESP is such a quantity and it connects  $\rho$  via eq. 1.67. Any change in  $\rho$  distribution due to bond formation between **D** and **A** molecules will be well reflected in their MESP features. The electronic changes that accompany the bond formation can be clearly understood by comparing  $V_{\min}$  values of isolated **D** and **A** molecules (designated as  $V_{\min-A}$  and  $V_{\min-D}$ , respectively) with  $V_{\min}$  values of **D** and **A** molecules in the complex (designated as  $V_{\min-A'}$  and  $V_{\min-D'}$ , respectively). Hence, the electronic reorganization during the bond formation can be quantified as  $\hat{e} V_{\min-D} = V_{\min-D'}$ ó  $V_{\min-D}$  for donor and ê  $V_{\min-A} = V_{\min-A'}$  ó  $V_{\min-A}$  for acceptor (Table 3.4). For all the complexes,  $\hat{e} V_{\min-D}$  is positive indicating the loss in electron density from **D** and  $\hat{e} V_{\min-A}$ is negative indicating gain in electron density by A. Thus, A becomes more electron rich at the expense of **D** meaning that the interaction between **D** and **A** can be best described as electron donor-acceptor (eDA) interaction. To illustrate this point, MESP plots of a representative set of complexes are given in Figure 3.9 along with their  $V_{\min}$  values. In the formation of  $H_2O$  dimer ( $H_2O...H_2O$ ), one of the  $H_2O$  molecules (A) gains electron density at the expense of the other (**D**) (Figure 3.9 a). In this case,  $V_{\min-D}$  and  $V_{\min-D'}$  are -

50.45 and -34.51 kcal/mol, respectively and  $V_{\min-A}$  and  $V_{\min-A'}$  are -50.45 and -63.82 kcal/mol, respectively.  $\hat{e} V_{min-A}$  and  $\hat{e} V_{min-D}$  are 15.95 and -13.37 kcal/mol, respectively which indicates that that a significant amount of electron density of **D** has been transferred to A during the formation of the noncovalent complex. Another interesting observation is that the magnitude of  $\hat{e} V_{\min-A}$  depends on the electron donating ability of the **D** in **D**-A. For instance, in the case of C-H...Y systems H<sub>3</sub>N...HCCH and H<sub>2</sub>S...HCCH, V<sub>min</sub> value -22.29 kcal/mol of the isolated HCCH is changed to -32.38 kcal/mol for the former and -26.73 kcal/mol for the latter which accounts for the stronger electron donating power NH<sub>3</sub> (ê  $V_{min-A}$  -10.09 kcal/mol) than H<sub>2</sub>S (ê  $V_{min-A}$  -4.44 kcal/mol). The  $\hat{e} V_{\min-A}$  of negatively charged systems are more negative than neutral ones which indicate a greater shift of electron density towards the acceptor side. This interpretation of  $\hat{e} V_{\min-D}$  and  $\hat{e} V_{\min-A}$  suggests that the quantity  $\hat{e} \hat{e} V_{\min} = \hat{e} V_{\min-D}$  of  $\hat{e} V_{\min-D}$ A could be used as a measure of the donor-acceptor strength of the noncovalent interaction. A reasonably good linear correlation between  $\hat{e} \hat{e} V_{\min}$  and  $E_{nb}$  is obtained (Figure 3.10) which suggests that the strength of the noncovalent bond is directly related with the donor-acceptor strength. Since  $V_{\min}$  measures the work done in bringing a unit test positive charge from infinity to the location of the  $V_{\min}$ , it is an energetic measure on the electrostatic influence.  $V_{\min}$  is also related with the charge transfer by virtue of its relation to the continuous electron distribution and hence reflects the charge transfer taking place in the system due to non-covalent binding.



**Figure 3.9** Change in  $V_{\min}$  upon bond formation for (a) H<sub>2</sub>O...H<sub>2</sub>O (b) H<sub>2</sub>O...ClF and (c) H<sub>3</sub>N...HCCH. The black dots represent the location of the most negative MESP-valued point and the corresponding  $V_{\min}$  values are also depicted.

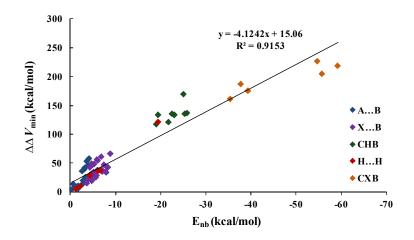
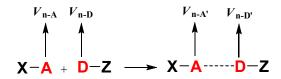


Figure 3.10 Linear relationship between  $\Delta\Delta V_{min}$  and noncovalent interaction energy (E<sub>nb</sub>).

The  $V_{\min}$  approach to measure the donor-acceptor strength is not possible in some cases because of the absence of a local  $V_{\min}$  in **D** or **A** of the **D**-**A** complex and such systems include Ar...HCH<sub>3</sub>, H<sub>3</sub>P...H<sub>2</sub>O, H<sub>3</sub>P...H<sub>2</sub>S, H<sub>3</sub>...HF, H<sub>3</sub>P...HCl, H<sub>3</sub>N...ClF and all cationic systems. Further, being a sensitive spatial property,  $V_{min}$  can be affected by secondary interactions from other parts of the molecule and this may be the reason for not finding a strong linear correlation between  $\Delta\Delta V_{min}$  and  $E_{nb}$  (R =0.910). On the other hand, the nucleus-centered quantity  $V_n$  is less sensitive to secondary interactions and all systems including cations show  $V_n$ .  $V_n$  at the donor ( $V_{n-D}$ ) and acceptor ( $V_{n-A}$ ) atoms in free molecules as well as  $V_n$  at the donor ( $V_{n-D}$ ) and acceptor atoms ( $V_{n-A}$ ) in complexes are computed and the quantities  $\Delta V_{n-A} = V_{n-A'}$  6  $V_{n-A}$  and  $\Delta V_{n-D} = V_{n-D'}$  6  $V_{n-D}$  are calculated (Scheme 3.2 and Table 3.4). The quantities  $\Delta V_{n-D}$  and  $\Delta V_{n-A}$  can be considered as electron donating ability and electron accepting ability of the acceptor and donor atoms, respectively. In all the A...B, X...B, CA and H...H type complexes,  $\Delta V_{n-D}$  is positive and  $\Delta V_{n-A}$  is negative indicating that **D** donates electron density to **A** during bond formation. This result is very similar to that obtained from  $V_{min}$  analysis and also means that  $\Delta\Delta V_n = \Delta V_{n-D}$  6  $\Delta V_{n-A}$  could be used as a good descriptor to measure the donor-acceptor power of the **D-A** complex.



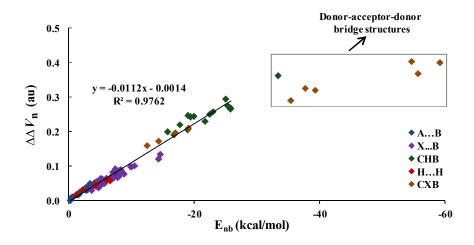
Scheme 3.2 X-A represents the electron acceptor and D-Z represents the electron donor. D and A are the atoms participating in the interaction. MESP at the nuclei are designated with symbols  $V_{n-A}$ ,  $V_{n-A'}$ ,  $V_{n-D}$  and  $V_{n-D'}$ .

A single linear correlation exists between  $\hat{e} \hat{V}_n$  and  $E_{nb}$  for all the **D**-A complexes except the bridged ones as shown in Figure 3.11. This correlation has R<sup>2</sup> value 0.976 suggesting that  $V_n$  can be effectively used for describing the bonding strength of all the **D**-A complexes irrespective of which category they belong to, *viz*. hydrogen bonds, halogen bonds, charge-assisted hydrogen bonds, charge-assisted

halogen bonds and dihydrogen bonds. The correlations of  $\hat{e} \hat{e} V_{\min}$  and  $\hat{e} \hat{e} V_n$  with  $E_{nb}$  also suggest the dominance of electrostatic contribution to the total interaction energy of noncovalent complexes. The exclusion of the bridged systems ( $H_3O^+$ ... $H_2O$ , F ... $I_{-}$ , F, F...Br...F, Cl...I...F, Cl...Br...F, F...I...Br and Cl...I...Br) from the linear correlation is justified because in such systems, the central atom show strong electron accepting interactions from two other atoms compared to only such interaction in nonbridged structures. The electronic reorganization during the bond formation in bridged anionic CXB complexes is demonstrated by means of MESP plots in Figure 3.12. In F...IF complex, I is placed symmetrically with respect to both the F atoms making it difficult to distinguish which F atom is the electron donor. This suggests the possibility of a resonance combination of F ... IF and F... IF and equal sharing of negative charge on both F atoms. Hence we may assume that central iodine accepts charge density from both the F atoms leading to a donor-acceptor-donor interaction in the bridged complex. This argument is further supported by the fact the both F atoms show the same  $V_{\min}$  value

in the complex (-158.20 kcal/mol) and a large enhancement in the negative MESP on the iodine atom (-110.63 kcal/mol). The MESP plot of F ...IBr too suggests the electron accepting interaction of iodine with partially negatively charged F and Br atoms. Energy decomposition analysis (EDA) by Wolters and Bickelhaupt [Wolters and Bickelhaupt 2012] has shown that halogen bonded trihalides of the type DX...A (D, X, A = F, Cl, Br, I) are generally associated with a weaker electrostatic attraction and a significantly strong covalent component arising from the stabilizing HOMOóLUMO interaction between the np-type lone pair on the halogen accepting fragment, A and the D-X antibonding \* LUMO on the halogen bond donating fragment DX.

Chapter 3



**Figure 3.11** Linear relationship between  $\Delta\Delta V_n$  and noncovalent interaction energy (E<sub>nb</sub>).

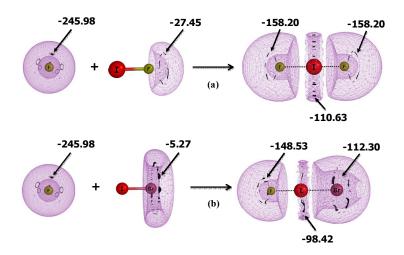


Figure 3.12 Change in  $V_{\min}$  upon bond formation in electron donor-acceptor-donor complexes (a) F ...IF and (b) F ...IBr. The black dots represent the location of the most negative MESP-valued point and the corresponding  $V_{\min}$  values are also depicted.

The significance of the correlation between  $\Delta\Delta V_n$  and  $E_{nb}$  is that MESP approach unifies all kinds of hydrogen bonds, halogen bonds and dihydrogen bonds as electron donor-acceptor (eDA) interactions. Hence a hydrogen bond could be considered as an eDA interaction in which a hydrogen atom acts as an electron acceptor. This interpretation is also applicable for dihydrogen bonds. Similarly a halogen bond may be defined as an eDA interaction in which a halogen atom acts as the electron acceptor.

**Table 3.4** Interaction energies (E<sub>nb</sub>), AIM properties ( $\rho$  and  $\nabla^2 \rho$ ) and MESP features ( $\hat{e} V_{min-A}$ ,  $\hat{e} V_{min-D}$ ,  $\hat{e} \hat{e} V_{n-A}$ ,  $\hat{e} V_{n-D}$  and  $\hat{e} \hat{e} V_n$ ) for representative set of intermolecular complexes.

Complex	E <sub>nb</sub>	ρ	$ abla^2  ho$	ê V <sub>min-A</sub>	ê V <sub>min-D</sub>	ê ê V <sub>min</sub>	$\hat{\rm e}V_{\rm n-A}$	$\hat{\rm e}V_{\rm n-D}$	ê ê V <sub>n</sub>
	(kcal/mol)	(au)	(au)	(kcal/mol)	(kcal/mol)	(kcal/mol)	(au)	(au)	(au)
ArHCH <sub>3</sub>	-0.23	0.003	0.011				-0.0005	0.0005	0.0009
$H_2SHCH_3$	-0.37	0.005	0.016	-4.15	0.56	4.72	-0.0088	0.0007	0.0096
$H_3PH_2S$	-1.47	0.008	0.020				-0.0097	0.0080	0.0177
$H_2SH_2S$	-1.38	0.008	0.024	-4.14	4.39	8.53	-0.0087	0.0091	0.0178
H3PH <sub>2</sub> O	-2.47	0.013	0.031				-0.0185	0.0134	0.0319
$H_4C_2HF$	-4.47	0.018	0.040	-10.10	14.33	24.43	-0.0253	0.0257	0.0510
$H_3P$ $H_3P$	-0.62	0.004	0.011	-3.66	9.89	13.55	-0.0075	0.0023	0.0098
$H_2OH_2O$	-4.70	0.023	0.085	-13.37	15.94	29.30	-0.0303	0.0260	0.0563
H <sub>3</sub> BH <sup>-</sup> HF	-19.38	0.025	0.057	-105.30	15.88	121.17	-0.2005	0.0423	0.2428
НВеННССН	-1.17	0.006	0.018	-2.81	2.49	5.30	-0.0079	0.0098	0.0176
LiHHCCH	-4.26	0.011	0.027	-18.37	10.29	28.66	-0.0413	0.0041	0.0454

#### -- Table 3.4 continued --

LiHí HCF3	-6.06	0.014	0.033	-15.89	20.71	36.60	-0.0473	0.0121	0.0594
CF <sub>3</sub> HHNa	-6.57	0.015	0.033	-18.34	18.89	37.22	-0.0537	0.0195	0.0732
$H_2O\ldots H_4N^+$	-19.93	0.048	0.127				-0.0434	0.2011	0.2445
$C_6H_6H_4N^+$	-18.93	0.020	0.054				-0.0519	0.1537	0.2055
$ClO^{-}H_2O$	-19.38	0.067	0.125	-113.14	20.33	133.47	-0.2028	0.0405	0.2433
ClO <sup>-</sup> HF	-22.46	0.051	0.155	-110.27	24.91	135.18	-0.2148	0.0355	0.2504
$ClO_2$ HF	-25.32	0.089	0.092	-117.53	-17.70	135.22	-0.2190	0.0559	0.2750
H <sub>3</sub> NClF	-10.46	0.052	0.139				-0.0398	0.0615	0.1013
H <sub>2</sub> OClF	-4.95	0.021	0.101	-12.80	16.25	29.05	-0.0242	0.0315	0.0557
H <sub>2</sub> SClF	-4.44	0.020	0.062	-10.92	10.98	21.90	-0.0172	0.0249	0.0420
HCNBrCl	-4.30	0.015	0.065	-10.08	32.47	42.55	-0.0210	0.0208	0.0418
H <sub>3</sub> CCNBrCl	-5.24	0.018	0.075	-13.23	35.02	48.25	-0.0273	0.0202	0.0474
H <sub>2</sub> COBrCl	-4.73	0.018	0.078	-8.73	10.48	19.21	-0.0159	0.0218	0.0377
FFI	-59.15	0.072	0.283	-130.75	87.79	218.54	-0.2183	0.1817	0.4000
CH <sub>2</sub> Cl <sup>-</sup> NH <sub>3</sub>	-16.96	0.032	0.104				-0.0319	0.1645	0.1964

#### **3.8 Conclusions**

In Part A of this chapter, the competence of M06L, MP2, MP4//M06L, MP4//MP2 and CCSD(T)//MP2 methods for modeling accurate binding energies of noncovalent complexes featuring hydrogen bonds, halogen bonds and dihydrogen bonds is assessed by comparing the energies calculated using these methods against highly accurate W1BD benchmark energies. Though M06L method is reliable for calculating the binding energies of neutral hydrogen bond complexes, it overestimates the energies of charge-assisted hydrogen bonds, halogen bonds and dihydrogen bonds. However, the MP4//M06L method yields noteworthy improvement on the energy data, making this hybrid method a good *ab initio*-DFT choice for estimating noncovalent interaction energies. The energy values of hydrogen bonds, halogen bonds and dihydrogen bonds are underestimated at MP2 level while MP4//MP2 and CCSD(T)//MP2 methods reproduces energies very close to W1BD accuracy. Hence MP4//MP2 and CCSD(T)//MP2 methods as are good hybrid *ab initio* choices for modeling the interaction energies of noncovalent complexes. The interaction energy data shows that geometry optimization at an *ab initio* or DFT method followed by single point energy calculation using MP4 or CCSD(T) level (viz. MP4//MP2, MP4//M06L and CCSD(T)//MP2 ) at a higher basis set can yield interaction energy values with accuracy close to computationally expensive CCSD(T) and W1BD methods. The enhancing effect of monovalent cations on the strength of hydrogen bonds is very high which promotes a noncovalent bond in the weak regime to the medium regime and that in the medium regime to the strong regime.

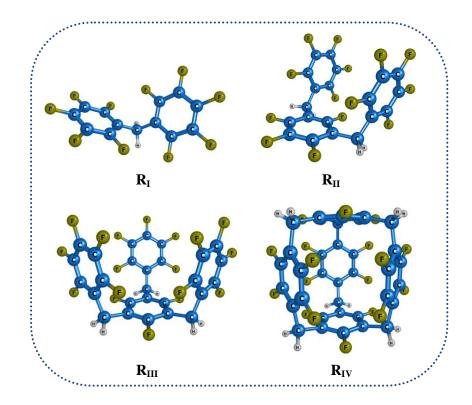
In Part B of this chapter, high level *ab initio* calculations coupled with atoms-inmolecules (AIM) and molecular electrostatic potential (MESP) approaches have been used for the study of a variety of intermolecular hydrogen bonds, halogen bonds and dihydrogen bonds to devise descriptor to quantify these noncovalent interactions. Although  $\rho$  values prove to be effective within a homogenous sample of **D**-A complexes where either the electron donor or acceptor is fixed, the applicability of these parameters for a heterogeneous sample of **D**-A complexes with different electron donors and/or acceptors is limited. An analysis of the  $V_{min}$  values of donor and acceptor molecules before and after complex formation shows that there is a considerable rearrangement of electron density within each monomer during the bond formation. A strong linear correlation is established between a parameter based on  $V_n viz$ .  $\Delta \Delta V_n$  and  $E_{nb}$  of all the complexes. The MESP at the nucleus emerges as an effective parameter to describe electron donor-acceptor interactions irrespective of the nature and strength of the interactions. To conclude, hydrogen bond can be considered as an eDA interaction in which a hydrogen atom acts as an electron acceptor whereas a halogen bond is as an eDA interaction in which a halogen atom acts as the electron acceptor. It is also shown that charge-assisted bridged complexes belong to a new category of donor-acceptor-donor complexes.

# Rational Design of Receptors Based on Noncovalent Interactions

Part A – Receptors for Neutral Molecules and Anions

&

Part B – Cage Receptors for Noble Gas Atoms and Molecular Hydrogen



### 4.1 ABSTRACT

In Part A of this chapter, mono, di, and tri pentafluorobenzyl substituted hexafluorobenzene (HFB) scaffolds  $R_{I}$ ,  $R_{II}$  and  $R_{III}$  are proposed as promising receptors for molecules of chemical, biological and environmental relevance, viz.  $N_2, O_3, H_2O, H_2O_2, F^-, Cl^-, BF_4^-, NO_3^-, ClO^-, ClO_2^-, ClO_3^-, ClO_4^- and SO_4^{2-}$ . The receptor-guest complexes modelled using M06L/6-311++G(d,p) DFT show remarkable increase in the complexation energy  $(E_{int})$  with increase in the number of fluorinated aromatic moieties in the receptor. Electron density analysis shows that fluorinated aromatic moieties facilitate the formation of large number of lone pair- $\pi$  interactions around the guest molecule. Lone pair strength of guest molecules quantified in terms of the absolute minimum  $(V_{min})$  of molecular electrostatic potential show that  $E_{int}$  strongly depends on the electron-deficient nature of the receptor as well as strength of lone pairs in the guest molecule. Compared to HFB,  $R_I$  exhibits 1.1 to 2.5-fold,  $R_{II}$  shows 1.6 to 3.6-fold and the bowl-shaped  $R_{III}$  gives 1.8 to 4.7-fold increase in the magnitude of  $E_{int}$ . For instance, in the cases of HFB...F<sup>-</sup>, **R**<sub>I</sub>...F<sup>-</sup>, **R**<sub>II</sub>...F<sup>-</sup> and **R**<sub>III</sub>...F<sup>-</sup> the E<sub>int</sub> values are -21.1, -33.7, -38.1 and -50.5 kcal/mol, respectively. The results strongly suggest that tuning lone pair- $\pi$  interaction provides a powerful strategy to design receptors for small molecules and anions.

Highly fluorinated aromatic cores are electron-deficient and provide stabilizing interactions with inert gases. In Part B of this chapter, a fluorinated cage receptor molecule ( $\mathbf{R}_{IV}$ ) capable of forming stable endohedral complexes with noble gas atoms and molecular hydrogen designed by pentafluorobenzyl  $(C_6F_5CH_2)$  substitution of hexafluorobenzene core is reported. The van der Waals complexes of rare gas atoms (He, Ne, Ar and Kr) with  $\mathbf{R}_{IV}$  studied at M06L/6-311++G(d,p) density functional theory show that ~5 to 8-fold increase in interaction energy can be achieved using  $\mathbf{R}_{IV}$  compared to the unsubstituted hexafluorobenzene. Hexafluorobenzene (HFB) stabilizes He, Ne, Ar, and Kr by -0.69, -0.93, -0.76, and -1.00 kcal/mol. The inert gas stabilization increases steadily with the cage receptor molecule with  $E_{int}$  values -4.07, -5.97, -6.00, and -6.11 kcal/mol for He, Ne, Ar and Kr respectively. The efficiency of  $\mathbf{R}_{IV}$  to trap and store molecular hydrogen is evident from the highly stable  $\mathbf{R}_{IV}$ ... $\mathbf{H}_2$  complex with an  $E_{int}$  value of -7.08 kcal/mol.

## Part A – Receptors for Neutral Molecules and Anions

#### **4.2 Introduction**

The design and synthesis of novel receptor systems for charged and neutral small molecules is a particularly relevant and challenging field that has spurred the interest of synthetic and theoretical chemists [Beer and Gale 2001; Dietrich 1993; Joyce et al. 2010; McKee et al. 2003]. Receptors capable of selective binding to small molecules find potential applications in varying fields including chemical and biological recognition, drug delivery, environmental chemistry, bio-sensing, catalysis, chemical separation and storage. Molecular recognition processes are mainly based on the combination of various attractive noncovalent interactions between receptor and substrate like electrostatic, dipole, dispersion,  $\pi$ -stacking, hydrogen bonding interactions and coordination to Lewis acids [Schmidtchen and Berger 1997]. Relatively few systems capable of molecular recognition of small gaseous substrates have been reported which include cyclodextrins, hemicarcerands, cryptophanes and porphyrins [Dietrich 1993; Graf and Lehn 1976]. Higher degree of design is required to make complementary receptors to anionic guests since they exhibit a multitude of geometries ranging from linear to spherical and even more complex structures as in the case of poly anions like DNA [Bianchi et al. 1997]. Larger size of anions leading to lower charge to mass ratio, sensitivity of anions to pH and protonation under acidic conditions also adds to the complexity involved in the design of anion hosts. The field of anion receptor chemistry emerged with a seminal communication by Simmons and Park [Park and Simmons 1968a; Park and Simmons 1968b] reporting the synthesis of a macrobicyclic ammonium based receptor for the binding of chloride ions. The highly specific transport of sulphate and phosphate across biological membranes regulated by neutral anion binding proteins motivated research efforts for the synthesis of neutral receptors. Crystal structures [Pflugrath and Quiocho 1988] have revealed that the sulfate binding protein binds the anion through precisely positioned hydrogen bonding interactions between the sulfate anion and the NH groups of the protein backbone, serine OH, or tryptophan NH groups [He and Quiocho 1991; Luecke and Quoicho 1990; Pflugrath and Quiocho 1985]. On the basis of these initial findings, a myriad of synthetic anion receptors have been designed utilizing hydrogen bonding [Amendola et al. 2010a; Amendola et al. 2010b; Begum et al. 2006; Bondy and Loeb 2003; Choi and Hamilton 2003; Lhoták 2005; Li et al. 2010; Llinares et al. 2003; al. 20061 recognition Yoon et for anion which include macrocyclic polyammonium/guanidinium, amides, urea, thiourea and functionalized calixarenes based receptors.

Compelling evidence for lone pair- $\pi$  and anion- $\pi$  interactions from theoretical [Alkorta *et al.* 1997; Alkorta *et al.* 2002; Mascal *et al.* 2002; Quiňonero *et al.* 2002b], experimental [De Hoog *et al.* 2004; Estarellas *et al.* 2011; Estarellas *et al.* 2009; Garcia-Raso *et al.* 2007; Kim *et al.* 2004; Schottel *et al.* 2008] and data base studies [Ahuja and Samuelson 2003; Casellas *et al.* 2006; Mooibroek *et al.* 2008; Quiňonero *et al.* 2002a; Quiňonero *et al.* 2002b] have opened an alternative route for the recognition of charged and neutral molecules bearing lone pairs by neutral hosts. Haloaromatics and electron-deficient aromatic rings like hexafluorobenzene, s-triazine, tetracyanobenzene, hexaazatriphenylene and tricyanobenzenes characterized by large negative quadruple moments are widely employed as anion binding units for the recognition of anions [Alkorta *et al.* 2002; Mascal *et al.* 2002; Mooibroek *et al.* 2008]. Receptors capable of multiple lone pair- $\pi$  interactions with the guest molecules in a cooperative fashion are required for efficient and selective recognition of lone pairs [Mascal et al. 2002]. Recently, Deva et al. demonstrated the additivity of an ion- $\pi$ interactions using *ab initio* calculations with the goal of designing neutral anion receptors [Garau et al. 2005]. Literature reports on highly selective anion receptors and channels [Dawson et al. 2010; Gorteau et al. 2006; Hay and Bryantsev 2008; Matile and Mareda 2009; Sakai *et al.* 2010] based on anion- $\pi$  interactions marks the rapid progress in the field. Mascal [Mascal 2006] theoretically predicted and experimentally synthesized several 1,3,5-cyclophane-based receptors incorporating triazine, cyanuric acid, or boroxine rings which show selective recognition towards fluoride ions by a combination of an interactions and ion-pair reinforced hydrogen bonding. Matile *et al.* [Matile and Mareda 2009] recently reported the synthesis and use of oligomer of NDIs for making an ion- $\pi$  slides that can be exploited to transfer an ions through membranes. The interaction of hexafluorobenzene (HFB) with electron-rich systems are well documented and is beneficially exploited as a key binding motif for the design of lone pair and anion sensors and receptors [Alkorta et al. 2002; Amicangelo et al. 2012; Danten 1999; Gallivan and Dougherty 1999; Kim et al. 2004; Mohan et al. 2013; Quiňonero et al. 2002b]. Very recently, Meyer et al. [Bretschneider et al. 2013] reported the synthesis of two neutral anion receptors viz. 1,3-bis(pentafluorophenyl-imino)isoindoline and 3,6-ditert-butyl-1,8-bis(pentafluorophenyl)-9H-carbazole that exploit anion- $\pi$  interactions to bind chloride and bromide ions.

Herein, neutral molecular receptors capable of binding lone pairs in molecules including anions through multiple lone pair- $\pi$  interactions are proposed using density functional theory (DFT) calculations. HFB is used as a scaffold and is substituted with pentafluorobenzyl groups (C<sub>6</sub>F<sub>5</sub>CH<sub>2</sub>-) to model bidentate receptor (**R**<sub>I</sub>), tridentate receptor (**R**<sub>II</sub>) and a tetradentate receptor (**R**<sub>III</sub>) (Scheme 4.1). The C<sub>6</sub>F<sub>5</sub>CH<sub>2</sub>- arms of the receptor molecules are expected to show orientation toward the electron-rich lone pair regions of the incoming molecule. Since the selective recognition of anions have

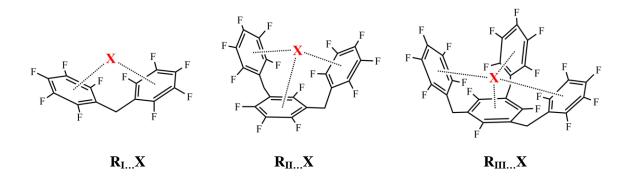
biological, chemical and environmental implications, the proposed receptor models could serve as excellent lead molecules towards the synthesis of anion receptors with potential medicinal and biological applications.

#### 4.3 Methods

#### 4.3.1 Molecular Design Strategy

Hexafluorobenzene (HFB), due to its electron-deficient nature, can bind effectively to lone pairs in neutral molecules, anions and free radicals [Alkorta et al. 1997; Alkorta et al. 2002; Mohan et al. 2013]. In order to improve the selectivity and binding affinity of HFB, pentafluorobenzyl (C<sub>6</sub>F<sub>5</sub>CH<sub>2</sub>-) substitution on HFB core is done. Substituting one F- with  $C_6F_5CH_2$ - leads to the receptor **R**<sub>I</sub>, a bis(perfluoroaryl)methane molecule with bidentate functionality. The synthetic approach of  $\mathbf{R}_{\mathbf{I}}$  by the desulfurization of sulfone-stabilized carbanions is reported in literature [Chambers and Todd 1985], however the utility of this molecule as a receptor for lone pair bearing molecules has not been investigated.  $\mathbf{R}_{II}$  is a fluorinated 1, 3-dibenzylbenzene molecule designed by substituting the HFB core with two  $C_6F_5CH_2$ - groups at 1 and 3 positions. The three electron-deficient rings in  $\mathbf{R}_{\mathbf{H}}$  make it a suitable receptor for the recognition of molecules with three lone pair bearing atoms like  $O_3$  and  $NO_3^-$ . The tetradentate receptor  $(\mathbf{R}_{III})$  is a fluorinated 1, 3, 5-tribenzylbenzene molecule designed by substituting HFB core with  $C_6F_5CH_2$ - groups at 1, 3 and 5 positions. **R**<sub>III</sub> is bowl-shaped and has four electron-deficient rings which can bind to anions with tetrahedral geometry like  $\mathrm{SO_4}^{2-}$ and  $ClO_4^-$ . The three receptor models  $R_I$ ,  $R_{II}$  and  $R_{III}$  and their possible lone pair- $\pi$ interactions with any lone pair bearing molecule is presented in Scheme 4.1.

The interactions of  $\mathbf{R}_{\mathbf{I}}$ ,  $\mathbf{R}_{\mathbf{II}}$  and  $\mathbf{R}_{\mathbf{III}}$  with different lone pair bearing neutral and anionic molecular systems of chemical, biological and environmental significance *viz*. N<sub>2</sub>, O<sub>3</sub>, H<sub>2</sub>O, H<sub>2</sub>O<sub>2</sub>, F<sup>-</sup>, Cl<sup>-</sup>, BF<sub>4</sub><sup>-</sup>, NO<sub>3</sub><sup>-</sup>, ClO<sup>-</sup>, ClO<sub>2</sub><sup>-</sup>, ClO<sub>3</sub><sup>-</sup>, ClO<sub>4</sub><sup>-</sup> and SO<sub>4</sub><sup>2-</sup> have been analyzed for their ability to form lone pair- $\pi/anion-\pi$  interactions. The chlorine oxyanion family *viz*. Cl<sup>-</sup>, ClO<sup>-</sup>, ClO<sup>-</sup>, ClO<sup>-</sup>, ClO<sup>-</sup>, and ClO<sup>-</sup><sub>4</sub> is chosen due to their environmental significance and also to understand the effect of sequential increase in the number of lone pair bearing atoms on the binding energy.



Scheme 4.1 Models proposed for anion recognition. X represents the lone pair bearing molecule and the possible lone pair- $\pi$  interactions are represented with dotted lines.

#### 4.3.2 Computational Methods

The geometries of all the receptor models and the complexes of the receptors with various lone pair bearing molecules are optimized at M06L level [Zhao and Truhlar 2006] using 6-311++G(d,p) basis set by means of Gaussian09 [Frisch *et al.* 2010] suite of programs. The binding energies are calculated using supermolecule approach with correction for basis set superposition error (BSSE) using counterpoise technique [Boys and Bernardi 1970a]. Solvation energies of a representative set of host-guest complexes are calculated using single point energy calculations at isodensity polarized continuum model (IPCM) [Foresman *et al.* 1996] at the same level of theory. IPCM model is more realistic and accurate since the solvation cavity is defined based on the isosurface of electron density. The topological properties of electron density at bond critical points (bcps) have been studied using 'atoms-in-molecules' (AIM) methodology with AIM2000 program [Biegler-König and Schönbohm 2002; Biegler-König *et al.* 2001]. Molecular

electrostatic potential analysis (MESP) is used to quantify the electron-rich character of the guest molecules. MESP topography of the receptor molecules are also analyzed at same level of theory.

#### **4.4 Results and Discussion**

The optimized geometries of  $\mathbf{R}_{I}$ ,  $\mathbf{R}_{II}$  and  $\mathbf{R}_{III}$  are presented in Figure 4.1. While HFB has all the ring C-C-C bond angles and C-C bond lengths equal *i.e*, 120° and 1.39 Å respectively, substitution with C<sub>6</sub>F<sub>5</sub>CH<sub>2</sub>- groups causes slight distortion of the C-C-C bond angles in  $\mathbf{R}_{I}$ ,  $\mathbf{R}_{II}$  and  $\mathbf{R}_{III}$ . In all the cases, C-C-C bond angle at the ipso carbon for the ring is decreased (by approximately 3 - 5°) while other C-C-C bond angles of the rings are increased (by approximately 2 - 5°). However, the C-C bond lengths remain more or less the same in all the receptors.

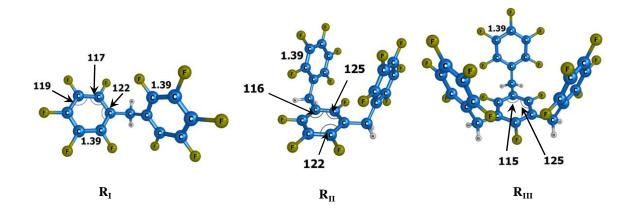
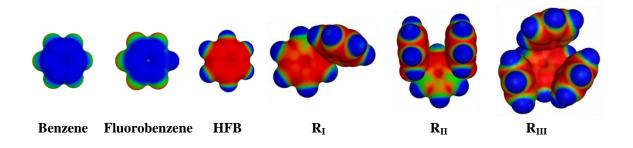


Figure 4.1 Optimized geometries of  $\mathbf{R}_{I}$ ,  $\mathbf{R}_{II}$  and  $\mathbf{R}_{III}$  at M06L/6-311++G(d,p) DFT method. C-C bond distances in Angstroms and C-C-C bond angles in degree are also depicted.

A qualitative picture of the electron-deficient nature of the fluorinated receptors can be understood from the MESP plots presented in Figure 4.2 where the regions of most negative potential appear blue and regions of most positive potential appear red. The  $\pi$ -region of benzene is evident from the large negative MESP on the ring. Monofluorobenzene also shows negative MESP over the aromatic ring. With hexafluoro substituion, MESP over the ring becomes positive indicating highly electron-deficient HFB. The reversal of electrostatics in HFB can be attributed to the combined electron withdrawing power of six fluorine atoms. The receptors  $\mathbf{R}_{I}$ ,  $\mathbf{R}_{II}$  and  $\mathbf{R}_{III}$  also show highly electron-deficient nature of aromatic rings. In the fluorinated aromatics, F atoms show blue-colored MESP which correspond to their lone pair regions. Since F atoms withdraw  $\pi$ -electron density from the aromatic rings, an increase in the negative character of  $V_{min}$  on F can indicate increased electron deficiency on the aromatic rings. The MESP isosurface of HFB and the three receptor molecules are shown in Figure 4.3 along with their  $V_{min}$  values. It shows that compared to HFB having  $V_{min}$  -6.6 kcal/mol on F atoms, the F atoms of  $\mathbf{R}_{I}$ ,  $\mathbf{R}_{II}$  and  $\mathbf{R}_{III}$  show progressively more negative  $V_{min}$ , *viz.* -9.2, -11.0 and -14.1 kcal/mol respectively, suggesting that more fluorine substitution increases the electron deficiency on the aromatic rings. The larger electron-deficient nature of the aromatic rings will enable the receptor molecules to establish stronger electrostatic influence on lone pair- $\pi$  interactions.



**Figure 4.2** MESP plots demonstrating the nature of aromatic rings in benzene, fluorobenzene, HFB,  $\mathbf{R}_{I}$ ,  $\mathbf{R}_{II}$  and  $\mathbf{R}_{III}$ . Color coding, **blue** -0.001 a.u. to red 0.03 a.u.

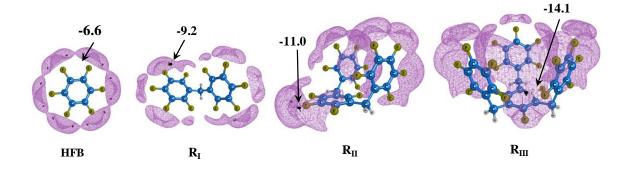


Figure 4.3 MESP isosurface of value -0.01 au for HFB,  $\mathbf{R}_{\mathbf{I}}$ ,  $\mathbf{R}_{\mathbf{II}}$  and  $\mathbf{R}_{\mathbf{III}}$  along with their  $V_{\min}$  values in kcal/mol.  $V_{\min}$  points are indicated by black dots.

MESP isosurfaces and MESP minima of some representative lone pair bearing molecules are presented in Figure 4.4. Table 4.1 reports the  $V_{min}$  values of all guest molecules. In Chapter 2 it has been shown that  $V_{min}$  quantifies the electron-rich character of a lone pair and provides good prediction on the lone pair- $\pi$  interaction energy (E<sub>int</sub>) with any electron-deficient  $\pi$ -system as  $V_{min}$  correlates linearly with E<sub>int</sub>. [Kumar *et al.* 2014; Mohan *et al.* 2013] The location of the lone pair region also enables a prediction on the orientation of the lone pair bearing molecule in the lone pair- $\pi$  complex [Mohan *et al.* 2013]. Among all the systems discussed here, sulfate anion (SO<sub>4</sub><sup>2-</sup>) exhibits the deepest  $V_{min}$  (-279.6 kcal/mol) while the least negative  $V_{min}$  (-3.6 kcal/mol) is observed for Cl<sub>2</sub>. The negative character of  $V_{min}$  follows the order, Cl<sub>2</sub> < N<sub>2</sub> < O<sub>3</sub> < H<sub>2</sub>O<sub>2</sub> < H<sub>2</sub>O < ClO<sub>4</sub><sup>-</sup> < BF<sub>4</sub><sup>-</sup> < ClO<sub>3</sub><sup>-</sup> < NO<sub>3</sub><sup>-</sup> < Cl<sup>-</sup> < ClO<sub>2</sub><sup>-</sup> < ClO<sup>-</sup> < F<sup>-</sup> < SO<sub>4</sub><sup>2-</sup>. In the chlorine oxyanion family, hypochlorite anion (ClO<sup>-</sup>) possesses the most negative  $V_{min}$  (-205.9 kcal/mol) while ClO<sub>4</sub><sup>-</sup> has the least electron-rich character with a  $V_{min}$  of -139.9 kcal/mol. The interaction energies of the receptor guest complexes are also expected to follow the same trend.

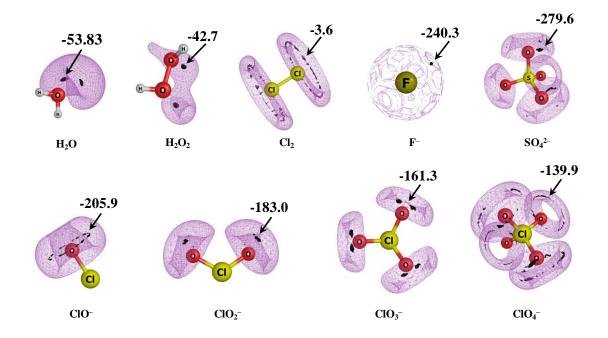


Figure 4.4 Representation of MESP isosurfaces for a representative set of lone pair bearing guest molecules. The MESP minima are marked as black dots and the corresponding  $V_{\min}$  values are given in kcal/mol.

The optimized geometries of  $\mathbf{R}_{I...}\mathbf{X}$ ,  $\mathbf{R}_{II...}\mathbf{X}$  and  $\mathbf{R}_{III...}\mathbf{X}$  complexes are given in Figure 4.5, 4.6 and 4.7 respectively. Table 4.1 reports the BSSE-corrected interaction energies ( $\mathbf{E}_{int}$ ) of **HFB**...**X**,  $\mathbf{R}_{I...}\mathbf{X}$ ,  $\mathbf{R}_{II...}\mathbf{X}$  and  $\mathbf{R}_{III...}\mathbf{X}$  complexes in kcal/mol.  $\mathbf{E}_{int}$  values of **HFB**...**X** allows a comparison of the enhancement in binding energies in  $\mathbf{R}_{I}$ ,  $\mathbf{R}_{II}$  and  $\mathbf{R}_{III}$  achieved by C<sub>6</sub>F<sub>5</sub>CH<sub>2</sub>- substitution on the HFB core. The optimum configuration of the guest molecules in all  $\mathbf{R}_{I...}\mathbf{X}$  complexes is such as to maximize the interactions from all the lone pairs with the electron-deficient arms of the receptor. For instance in  $\mathbf{R}_{I...}\mathbf{H}_2\mathbf{O}$ , the lone pairs of the O atom are oriented to each of the C<sub>6</sub>F<sub>5</sub>– arm of the receptor forming two lone pair- $\pi$  interactions with interaction distances of 3.38 and 3.34 Å respectively. In molecules like H<sub>2</sub>O<sub>2</sub>, H<sub>2</sub>O, F<sup>-</sup>, CI<sup>-</sup>, O<sub>3</sub>, CIO<sub>4</sub><sup>-</sup>, BF<sub>4</sub><sup>-</sup> and SO<sub>4</sub><sup>2-</sup> the interacting atoms are located almost equidistant from the two electron-deficient rings of the receptor molecule. F<sup>-</sup> forms two anion- $\pi$  interactions with  $\mathbf{R}_{I}$  at an interaction distance of 2.90 Å from both the perfluoroaryl rings in  $\mathbf{R}_{I...}\mathbf{F}^-$  complex.

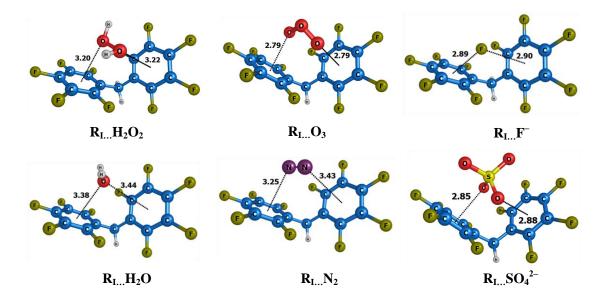


Figure 4.5 Optimized geometries of  $R_{I...}X$  complexes. Distances in Angstrom units.

The presence of multiple lone pair- $\pi$  interactions is amply justified by a drastic increase in the magnitude of  $E_{int}$ . The percentage increase in the magnitude of  $E_{int}$  values in  $\mathbf{R}_{1...}\mathbf{X}$  compared to  $\mathbf{HFB}_{...}\mathbf{X}$  is 11.2 - 174.8% which imply that molecules which can provide multiple interaction sites can indeed be used as effective recognition motifs for anions and lone pair bearing molecules.  $SO_4^{2-}$  exhibits the most stable interaction with  $\mathbf{R}_{\mathbf{I}}$  giving an  $E_{int}$  of -48.6 kcal/mol while the least stable interaction with  $\mathbf{R}_{\mathbf{I}}$  is shown by N<sub>2</sub> molecule ( $E_{int} = -2.6$  kcal/mol). The binding affinity of the guest molecules towards  $\mathbf{R}_{\mathbf{I}}$  follows the order, N<sub>2</sub> < H<sub>2</sub>O < Cl<sub>2</sub> < H<sub>2</sub>O<sub>2</sub> < O<sub>3</sub> < ClO<sub>3</sub><sup>-</sup> < ClO<sub>4</sub><sup>-</sup> < BF<sub>4</sub><sup>-</sup> < NO<sub>3</sub><sup>-</sup> < Cl<sup>-</sup> < ClO<sub>2</sub><sup>-</sup> < ClO<sub>2</sub><sup>-</sup> < ClO<sup>-</sup> < F<sup>-</sup> < SO<sub>4</sub><sup>2-</sup>. Among the chlorine oxyanion family, ClO<sup>-</sup> binds more strongly with  $\mathbf{R}_{\mathbf{I}}$  ( $E_{int} = -18.6$  kcal/mol) while ClO<sub>2</sub><sup>-</sup> exhibits the weakest binding ( $E_{int} = -13.8$  kcal/mol).

Optimized geometries of  $\mathbf{R}_{II...}\mathbf{X}$  complexes presented in Figure 4.6 clearly show the presence of at least three lone pair- $\pi$  interactions in all the complexes. A significant increase in the magnitude of  $E_{int}$  (13.5 – 45.2%) is observed for  $\mathbf{R}_{II...}\mathbf{X}$  compared to  $\mathbf{R}_{I...}\mathbf{X}$  (for X = O<sub>3</sub>,  $E_{int}$  is nearly unchanged) which presumably is the result of multiple interactions between the host and guest. The most significant enhancement in the magnitude of  $E_{int}$  is observed for  $R_{II...}N_2$  which is ~1.5 times higher than that of  $R_{I...}N_2$ . The  $E_{int}$  values of various molecules with  $R_{II}$  suggest the following trend in binding affinity:  $N_2 < O_3 < H_2O < Cl_2 < H_2O_2 < BF_4^- < ClO_4^- < ClO_3^- < NO_3^- < Cl^- < ClO_2^- <$  $ClO^- < F^- < SO_4^{2-}$ . In the case of chlorine oxyanion family,  $E_{int}$  and  $V_{min}$  follow the same trend where  $ClO_4^-$  with the least negative  $V_{min}$  forms the least stable complex ( $E_{int} = -$ 22.1 kcal/mol) while  $ClO^-$  with the most negative  $V_{min}$  forms the most stable complex ( $E_{int} = -30.7$  kcal/mol).

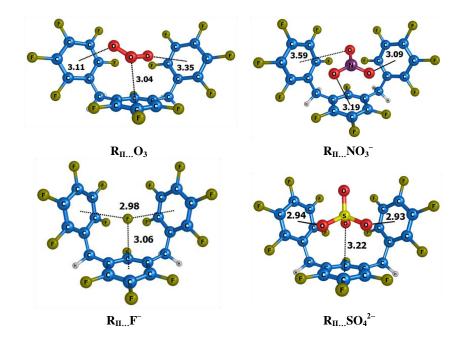


Figure 4.6 Optimized geometries of R<sub>II...</sub>X complexes. Distances in Angstrom units.

Tripodal receptors, hypothesized to be between cyclic and acyclic receptors are considered to bind more effectively to anionic ligands than the acyclic ones and are widely used as recognition components in various optical sensors and ion-selective membranes [Kuswandi *et al.* 2006]. In the tetradentate tripodal receptor  $\mathbf{R}_{III}$ , the guest molecules are locked into the cavity of the receptor by four or more lone pair/anion- $\pi$  interactions between the arms of  $\mathbf{R}_{III}$  and  $\mathbf{X}$  (Figure 4.7).

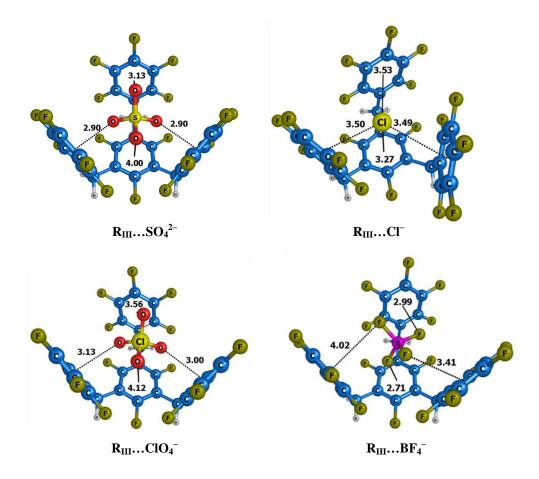


Figure 4.7 Optimized geometries of R<sub>III...</sub>X complexes. Distances in Angstrom units.

A significant enhancement ~9.4 to 37.8 % in  $E_{int}$  is observed for  $R_{III...X}$  complexes compared to  $R_{II...X}$  complexes. The trend for the interaction remains more or less the same with N<sub>2</sub> and SO<sub>4</sub><sup>2-</sup> being the least and most interacting species, respectively. The geometrical parameters as well as the interaction energy data suggests that  $R_{III}$  can be effectively used for binding tetrahedral anions with four electron-rich centers like SO<sub>4</sub><sup>2-</sup>, BF<sub>4</sub><sup>-</sup> and ClO<sub>4</sub><sup>-</sup>. The boost in  $E_{int}$  for  $R_{III}$  is more pronounced in less electron-rich neutral systems like Cl<sub>2</sub> and N<sub>2</sub>.  $R_{III...X}$  complexes of Cl<sub>2</sub> and N<sub>2</sub> show 293% and 371 % enhancement in  $E_{int}$  compared to the corresponding HFB...X complexes. In the chloride oxyanion family, the trend in  $V_{min}$  is reproduced in the interaction energy data of all the receptors with ClO<sup>-</sup> exhibiting the most and ClO<sub>4</sub><sup>-</sup> the least binding. This suggests that the interaction energy data has close association with the electron-rich nature of the guest molecules.

Х	V	E <sub>int</sub>					
	$V_{\min-X}$	HFBX	R <sub>I</sub> X	R <sub>II</sub> X	R <sub>III</sub> X		
$H_2O_2$	-42.7	-3.8	-6.0	-7.4	-9.2		
$H_2O$	-53.8	-3.1	-4.8	-6.4	-8.6		
$O_3$	-17.8	-3.8	-6.4	-6.2	-8.5		
$N_2$	-11.4	-1.0	-2.6	-3.7	-4.9		
$Cl_2$	-3.6	-1.9	-5.1	-6.6	-7.3		
Cl	-171.0	-14.5	-21.3	-26.9	-32.6		
$F^-$	-240.3	-21.1	-33.7	-38.1	-50.8		
$\mathrm{BF_4}^-$	-145.4	-8.9	-18.6	-21.5	-24.9		
$NO_3^-$	-167.4	-14.3	-20.8	-26.7	-31.2		
${\rm SO_4}^{2-}$	-279.6	_ <sup>a</sup>	-48.6	-62.6	-75.6		
C10 <sup>-</sup>	-205.9	-18.6	-27.0	-30.7	-36.2		
$\text{ClO}_2^-$	-183.0	-13.8	-24.0	-30.0	-35.4		
$\text{ClO}_3^-$	-161.3	-15.7	-17.5	-22.7	-27.9		
$\text{ClO}_4^-$	-139.9	-13.9	-18.5	-22.1	-26.8		

Table 4.1 Interaction energy (E<sub>int</sub>) of HFB...X, R<sub>I</sub>...X, R<sub>I</sub>...X and R<sub>III</sub>...X in kcal/mol.

 $^aSO_4{}^{2-}$  forms an anionic  $\sigma\text{-complex}$  with HFB

The free energy change ( $\Delta G$ ) for the formation of the receptor-guest complexes are summarized in Table 4.2. The complexes of the receptors with neutral molecules associated with lower binding energies (except  $\mathbf{R}_{III...}\mathbf{Cl}_2$  and  $\mathbf{R}_{III...}\mathbf{O}_3$ ) are characterized by positive  $\Delta G$  values signifying endergonic reactions which cannot occur spontaneously.  $\Delta G$  values for  $\mathbf{R}_{III...}\mathbf{Cl}_2$  and  $\mathbf{R}_{III...}\mathbf{O}_3$  are negative indicating the exergonic or spontaneous formation of host-guest complex in both cases. The complexes of  $\mathbf{R}_{I}$ ,  $\mathbf{R}_{II}$ and  $\mathbf{R}_{III}$  with all anionic guest molecules show large negative  $\Delta G$  values. Binding energies of a representative set of complexes computed at IPCM solvation model ( $\mathbf{E}_{int-}_{IPCM}$ ) are presented in Table 4.3. In comparison with the gas phase, the binding energy is reduced slightly in the solvent phase, but it is favorable, indicating that receptors based on the lone pair/anion- $\pi$  interaction are competitive in solvents too.

X	$\Delta G$ (kcal/mol)					
Λ	R <sub>I</sub> X	R <sub>II</sub> X	R <sub>III</sub> X			
$H_2O_2$	3.1	2.1	1.4			
$H_2O$	1.3	2.9	1.3			
O <sub>3</sub>	4.6	4.2	-0.3			
$N_2$	4.9	4.3	2.8			
$Cl_2$	2.3	0.7	-2.6			
Cl	-15.9	-18.7	-25.9			
$F^-$	-28.7	-29.6	-40.4			
$\mathrm{BF_4}^-$	-7.7	-9.1	-13.2			
$NO_3^-$	-9.7	-10.0	-20.8			
SO4 <sup>2-</sup>	-40.4	-53.4	-67.6			
ClO <sup>-</sup>	-19.9	-21.6	-28.4			
$\text{ClO}_2^-$	-15.7	-15.6	-28.9			
$\text{ClO}_3^-$	-9.1	-8.9	-21.3			
$\text{ClO}_4^-$	-9.6	-12.7	-18.7			

Table 4.2 Free energy change ( $\Delta G$ ) of  $R_I...X$ ,  $R_{II}...X$  and  $R_{III}...X$  complexes in kcal/mol.

**Table 4.3** Binding energy values of receptor-guest complexes in aqueous phase usingIPCM solvation model in kcal/mol.

System	E <sub>int-IPCM</sub>	System	E <sub>int-IPCM</sub>
$R_{I}H_2O_2$	-6.0	$R_{I\ldots}ClO_2^-$	-24.0
$R_{I}H_2O$	-4.6	$R_{I}ClO_4^-$	-18.4
$R_{I}O_3$	-6.4	$R_{II\ldots}H_2O_2$	-7.2
$R_{I}N_2$	-2.6	<b>R</b> <sub>II</sub> <b>O</b> <sub>3</sub>	-5.9
$R_{I}Cl_2$	-5.1	$R_{II\dots}N_2$	-3.5
$\mathbf{R}_{\mathbf{I}}\mathbf{C}\mathbf{I}^{-}$	-21.3	$R_{II}Cl_2$	-6.4
$\mathbf{R}_{\mathbf{I}}\mathbf{F}^{-}$	-33.7	R <sub>II</sub> Cl <sup>−</sup>	-26.6
$R_{I}BF_4^-$	-18.6	R <sub>II</sub> F <sup>−</sup>	-37.9
$\mathbf{R}_{\mathrm{I}}\mathbf{NO}_{3}^{-}$	-20.8	$\mathbf{R}_{\mathrm{III}}\mathbf{N}_{2}$	-5.1
R <sub>I</sub> ClO <sup>-</sup>	-27.0	$\mathbf{R}_{\mathbf{III}}\mathbf{BF_4}^-$	-27.5

The noncovalent anion- $\pi$ /lone pair- $\pi$  interaction in the receptor-guest complexes have been further explored using AIM analysis which reveals bcps and bond paths connecting the atoms of the guest molecules with the ring C atoms of the fluorinated arms of the receptors.

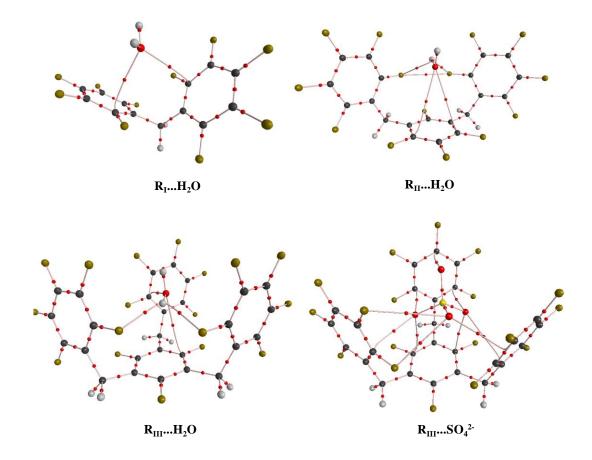


Figure 4.8 AIM Molecular graphs of  $R_{I...}H_2O$ ,  $R_{II...}H_2O$ ,  $R_{III...}H_2O$  and  $R_{III...}SO_4^{2-}$ . Small red spheres and lines represent bond critical points (BCPs) and bond paths, respectively.

Bcps and bond paths can be considered as signatures of lone pair/anion- $\pi$  interactions. In Figure 4.8, the AIM molecular graphs of  $\mathbf{R}_{I...}\mathbf{H}_2\mathbf{O}$ ,  $\mathbf{R}_{II...}\mathbf{H}_2\mathbf{O}$ ,  $\mathbf{R}_{III...}\mathbf{H}_2\mathbf{O}$  and  $\mathbf{R}_{III...}\mathbf{SO}_4^{2-}$  are shown as representative cases.  $\mathbf{R}_{I...}\mathbf{H}_2\mathbf{O}$  exhibits two bcps, each one connecting the O and a ring carbon atom suggesting the presence of two lone pair- $\pi$  interactions.  $\mathbf{R}_{II...}\mathbf{H}_2\mathbf{O}$  display two bcps linking the O atom with the ring C atoms of the

central HFB core. Additional stabilization by hydrogen bonding interaction of the H atoms of H<sub>2</sub>O and F atoms of C<sub>6</sub>F<sub>5</sub> rings of  $\mathbf{R}_{II}$  are also revealed in the molecular graphs.  $\mathbf{R}_{III...}\mathbf{SO_4}^{2-}$  complex displays multiple lone pair- $\pi$  interactions and halogen bonds (between O and F atoms). The value of  $\rho(\mathbf{r})$  at bcp varies between 0.002 to 0.028 au, while the corresponding  $\nabla^2 \rho(\mathbf{r})$  values are all positive in the range 0.011 to 0.091 au. Thus it is clear that lone pair- $\pi$ /anion- $\pi$  interactions coupled with hydrogen and halogen bonds bring about the efficient binding of the receptor molecules with neutral and anionic guest molecules.

## Part B – Cage Receptors for Noble Gas Atoms and Molecular Hydrogen

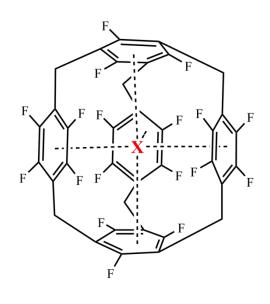
### **4.5 Introduction**

Non covalent complexes formed between rare gas atoms and aromatic molecules  $(RG-\pi)$ have been the subject of many theoretical and experimental investigations [Dessent and Müller-Dethlefs 2000; Felker et al. 1994; Hobza et al. 1994; Kim et al. 2000; Neusser and Krause 1994; van der Avoird et al. 1994]. The chemical inertness of noble gases was considered to be absolute for many years [Christe 2001] since their discovery until 1930 when Pauling [Pauling 1933] suggested that chemical bonding may be possible for heavier noble gas atoms like xenon where the outermost electronic shell is less stable. Later, Neil Bartlett [Bartlett 1962] demonstrated that the inertness of noble gases is not a basic tenet of chemistry by synthesizing the first noble gas compound,  $Xe^{+}[PtF_5]$  which triggered the search for interactions between rare gases and other elements. Noble gas atoms, due to their spherical electron density distribution, do not possess any permanent electric multipole moment and hence the electrostatic component of the interaction energy is absent in the case of the complexes of rare gas atoms with aromatic molecules [Chalasinski and Szczesniak 1994; Hobza et al. 1994]. Being chemically inert, rare gas atoms interact by van der Waals forces, which at large distances are governed by attractive dispersion forces. The van der Waals complexes of argon with a number of prototype benzene-related systems including benzene, fluorinated benzenes, aniline, furan and oxazoles have been probed [Bohn et al. 1989; Brupbacher and Bauder 1990; Hobza et al. 1996; Hobza et al. 1992; Hobza et al. 1991; Hobza et al. 1993; Kraka et al. 1995; Kukolich 1983; Tarakeshwar et al. 2001]. These studies have shown that exchange repulsion forces preferentially dictate the equilibrium geometry whereas, the dispersion forces determine the stability of RG– $\pi$  complexes. Structure adapted perturbation theory (SAPT) studies by Kim et al. [Tarakeshwar *et al.* 2001] on the complexes of argon with benzene and fluoro-substituted benzenes *viz.* fluorobenzene and p-difluorobenzene showed that fluorine substitution does not affect the stability of the complexes strongly since it causes a reduction in both the stabilizing induction and dispersion forces as well as the destabilizing exchange-repulsion and exchange-induction forces.

Encapsulation of charged or neutral molecules in the inner cavities of organic host molecules is a fascinating area of research and various theoretical and experimental efforts exploring the viability of cage like molecules having endohedrally trapped noble gas atoms have been reported [Cerpa et al. 2009; Jiménez-Vázquez et al. 2001; Krapp and Frenking 2007; Pan et al. 2013; Saunders et al. 1993]. Clathrates and hydrates are the earlier noble gas compounds known where the noble gas atoms are caged in cavities in the crystal lattice of the host compound formed by a network of hydrogen bonds between covalently bound molecules. The superior Xe binding characteristics of cryptophane molecules through van der Waals forces has also been demonstrated [Bartik et al. 1998; Brotin and Dutasta 2009; Jacobson et al. 2011]. Noble gas atoms encapsulated in cage-molecules functionalized to target biological receptors are employed in magnetic resonance imaging techniques for various medical applications [Berthault et al. 2008; Spence et al. 2001]. In view of the importance of cage like molecules for the encapsulation of noble gas atoms, theoretical approaches are employed to design a substituted hexafluorobenzene based caged structure that can effectively bind noble gas atoms. The binding affinity of the cage receptor for molecular hydrogen is also probed due to the increasing interest of receptors in hydrogen storage. The theoretical predictions presented in this chapter would be of interest to synthetic chemists for the synthesizing highly efficient novel receptors for noble gas atoms.

# 4.6 Design Strategy and Computational Methods

The cage receptor is modelled in a stepwise manner by substituting the electrondeficient core of hexafluorobenzene at 1, 3, and 5 positions with pentafluorobenzyl ( $C_6F_5CH_2$ -) groups. The tripodal platform of **R**<sub>III</sub> reported in Part A of this chapter is used for the construction of the cage receptor by moving it from an open to closed cavity *i.e.*, to a cage (**R**<sub>IV</sub>). The receptor model, **R**<sub>IV</sub> and its possible noncovalent interactions with any incoming guest molecule is presented in Scheme 4.2.



**R**<sub>IV</sub>

Scheme 4.2 The cage receptor model,  $\mathbf{R}_{IV}$ .  $\mathbf{X}$  = He, Ne, Ar, Kr and H<sub>2</sub>. Dotted lines represent the possible interactions of the guest molecule with the electron-deficient rings of the receptor.

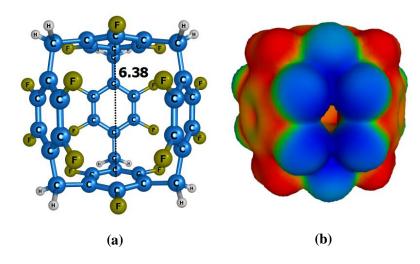
Geometry optimization of  $\mathbf{R}_{IV}$  as well as the complexes of the  $\mathbf{R}_{I}$ ,  $\mathbf{R}_{II}$ ,  $\mathbf{R}_{II}$  (reported in Part A of this chapter) and  $\mathbf{R}_{IV}$  with noble gas atoms and H<sub>2</sub> are carried out at M06L/6-311++G(d,p) level [Zhao and Truhlar 2006] using Gaussian09 [Frisch *et al.* 2010] suite of programs. BSSE corrected interaction or stabilization energies (E<sub>int</sub>) of the complexes are calculated using the supermolecule approach. The comparison of E<sub>int</sub> values for the  $\mathbf{R}_{IV}...\mathbf{X}$  with E<sub>int</sub> for HFB...X,  $\mathbf{R}_{I}...\mathbf{X}$ ,  $\mathbf{R}_{II}...\mathbf{X}$  and  $\mathbf{R}_{III}...\mathbf{X}$  complexes

demonstrates the systematic improvement in the interaction energy on moving from HFB with single electron-deficient ring to the cage receptor with five electron-deficient rings. Topological properties of molecular electron density at the bond critical points (BCP) are obtained by AIM methodology [Bader 1985] as implemented in AIM2000 program [Biegler-König and Schönbohm 2002; Biegler-König *et al.* 2001]. Molecular electrostatic potential (MESP) topography of the receptor molecule is analyzed at the same level of theory.

To test the suitability of M06L/6-311++G(d,p) level for the binding energy calculations, the  $E_{int}$  of benzene-argon complex computed at M06L/6-311++G(d,p) level is compared with experimental binding energy value.  $E_{int}$  of benzene-argon complex is 0.962 kcal/mol which is indeed very close to the experimental binding energy obtained by Krause and Neusser [Krause and Neusser 1993] (0.972 kcal/mol) suggesting the adequacy of this level for the calculations.

## **4.7 Results and Discussion**

Figure 4.9 presents the optimized geometry of  $\mathbf{R_{IV}}$  and the MESP textured on the 0.003 au electron density surface to demonstrate the most negative potential (blue) and most positive potential (red) regions of the receptor. All the five aromatic rings of  $\mathbf{R_{IV}}$  are electron-deficient and form noncovalent interactions with guest molecules in the internal cavity. The inner cavity of  $\mathbf{R_{IV}}$  is 6.38 Å in length and 5.47 Å in width. The interaction distances for the complexes of He, Ne, Ar, Kr and Xe with HFB are 3.06 Å, 3.24 Å, 3.60 Å, 3.55 Å and 3.81 Å respectively. This shows that the cavity of the  $\mathbf{R_{IV}}$  is large enough to encapsulate He, Ne, Ar and Kr whereas Xe is too large to be contained in the  $\mathbf{R_{IV}}$  cavity.



**Figure 4.9** (a) Optimized geometry of the cage receptor and (b) MESP textured on the 0.003 au electron density surface.

Figure 4.10 presents the endohedral complexes of  $\mathbf{R}_{IV}$  with noble gas atoms He, Ne, Ar and Kr. It is clear that the noble gas atom is placed symmetrically relative to the center of the cage in all the endohedral complexes. The interaction energies of the noncovalent complexes of noble gas atoms (He, Ne, Ar and Kr) and H<sub>2</sub> with R<sub>I</sub>, R<sub>II</sub>, R<sub>III</sub> and  $\mathbf{R}_{IV}$  are presented in Table 4.4. The stabilization energy for the van der Waals complexes of He, Ne, Ar and Kr with the cage receptor is -4.07, -5.97, -6.00 and -6.11 kcal/mol, respectively. As the number of fluorinated aromatic units is increased from one to five, the binding energies of the noble gas complexes have increased steadily. Compared to HFB...He complex, magnitude of E<sub>int</sub> is increased by 5.9-fold for R<sub>IV</sub>...He complex. Similarly 6.4-fold, 7.9-fold and 6.1-fold increase in the magnitude of Eint is observed in the complexes of Ne, Ar and Kr with  $\mathbf{R}_{IV}$  in comparison with HFB. The DFT-SAPT interaction energies of endohedral complexes of the C<sub>60</sub> fullerene with He, Ne, Ar and Kr atoms reported by Hesselmann and Korona [Hesselmann and Korona 2011] are -1.58, -2.86, -7.88 and -8.26 kcal/mol, respectively. Slanina et al. [Slanina et al. 2006] reported the stabilization energy of Ne@C<sub>60</sub> at MP2/6-311G(2d, 2p) and MPWB1K/6-311G(2d, 2p) as -5.39 and -7.20 kcal/mol, respectively. These results indicate that compared to fullerene, the newly proposed cage receptor  $\mathbf{R}_{IV}$  binds more effectively with He and Ne while the interaction of the  $\mathbf{R}_{IV}$  is slightly as good or slightly weaker with Ar and Kr.

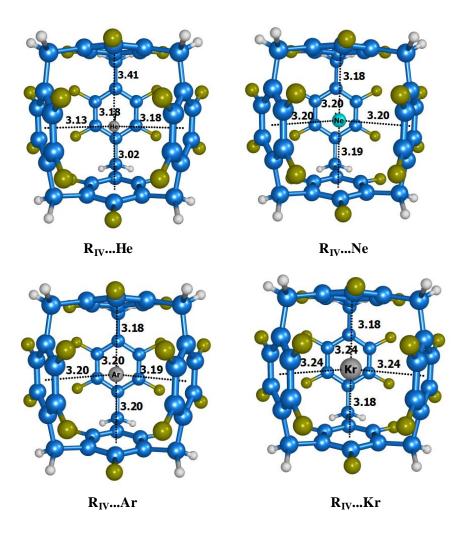


Figure 4.10 Optimized geometries of  $R_{IV}$ ...He,  $R_{IV}$ ...Ne,  $R_{IV}$ ...Ar and  $R_{IV}$ ...Kr complexes. Interaction distances in Å.

 $\mathbf{R_{IV}}$ ... $\mathbf{H_2}$  complex (Figure 4.11) is highly stable with an  $\mathbf{E}_{int}$  value of -7.08 kcal/mol which is considerably higher than the reported values for  $\mathbf{H_2@C_{60}}$  and  $\mathbf{H_2@C_{70}}$ . The stabilization energy of  $\mathbf{H_2@C_{70}}$  calculated from diffusion Monte Carlo (DMC) [Sebastianelli *et al.* 2010] calculations is -3.83 kcal/mol while the energy calculated from DFT-SAPT [Korona *et al.* 2009] is -3.46 kcal/mol, SCS-MP2 [Kruse and Grimme 2009] method is -6.50 kcal/mol and MPWBK [Murata *et al.* 2008] method is -

6.90 kcal/mol. The reported stabilization energies for  $H_2@C_{60}$  from DMC [Sebastianelli *et al.* 2010] calculations is -4.29 kcal/mol, DFT-SAPT [Korona *et al.* 2009] is -4.63 kcal/mol and MP 2.5/CBS' (2,3) [Kruse and Grimme 2009] method is -7.30 kcal/mol. It is also evident that there almost 10-fold increase in  $E_{int}$  for  $R_{IV}...H_2$  complex compared to HFB...H<sub>2</sub> complex. These results clearly show the efficiency of  $R_{IV}$  to trap and store molecular hydrogen.

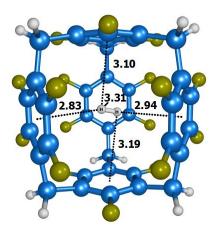


Figure 4.11 Optimized geometry of  $\mathbf{R}_{IV}$ ... $\mathbf{H}_2$  complex. Interaction distances in Å.

Table 4.4 Interaction energy values (Eint) of HFB...X, RI...X, RII...X, RIII...X andRIV...X in kcal/mol.

X	E <sub>int</sub>								
28	HFBX	R <sub>I</sub> X	R <sub>II</sub> X	R <sub>III</sub> X	R <sub>IV</sub> X				
He	-0.69	-1.04	-1.53	-2.54	-4.07				
Ne	-0.93	-1.40	-2.29	-3.23	-5.97				
Ar	-0.76	-2.10	-2.95	-4.16	-6.00				
Kr	-1.00	-2.54	-3.60	-4.33	-6.11				
$H_2$	-0.72	-1.34	-2.52	-3.85	-7.08				

The presence of nonbonding interactions between the noble gas atoms and H<sub>2</sub> with the cage receptor is confirmed by AIM topological features *viz*. the existence of bcps and bond paths linking the atoms of the guest molecule and one or more ring carbon atoms of  $\mathbf{R}_{IV}$ . Electron density,  $\rho(\mathbf{r})$  and Laplacian of electron density,  $\nabla^2 \rho(\mathbf{r})$  at bcps for  $\mathbf{R}_{IV}$ ...X complexes are summarized in Table 4.5. The bond paths and bcps between the ring carbon atoms of  $\mathbf{R}_{IV}$  and the atoms of the guest species are depicted in the molecular graphs of the  $\mathbf{R}_{IV}$ ...He,  $\mathbf{R}_{IV}$ ...Ne,  $\mathbf{R}_{IV}$ ...Ar and  $\mathbf{R}_{IV}$ ...Kr shown in Figure 4.12 and molecular graph of  $\mathbf{R}_{IV}$ ...H<sub>2</sub> shown in Figure 4.13.

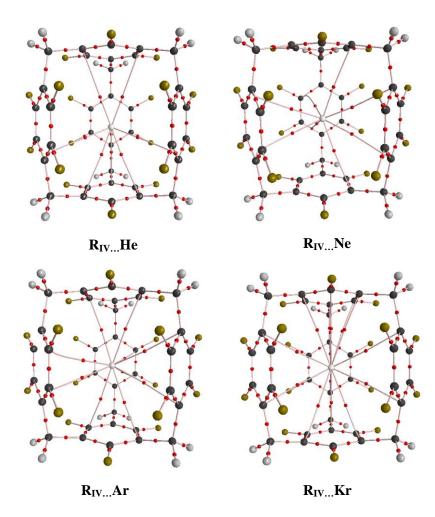


Figure 4.12 AIM molecular graph of the endohedral complexes of  $\mathbf{R}_{IV}$  with He, Ne, Ar and Kr. Small red spheres represent bond critical points (bcps) and red lines represent bond paths.

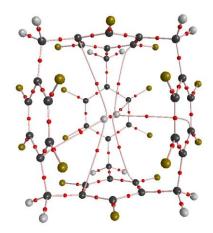


Figure 4.13 AIM molecular graph of the  $R_{IV}$ ... $H_2$  complex. Small red spheres represent bond critical points (bcps) and red lines represent bond paths.

**Table 4.5** Electron density ( $\rho(\mathbf{r})$ ) and Laplacian of electron density ( $\nabla^2 \rho(\mathbf{r})$ ) at bcps for  $\mathbf{R}_{IV...}\mathbf{X}$  complexes. I, II, III, IV and V represent the five aromatic rings in the cage receptor. Values in au.

Х	Ι		II		III		IV		V	
			$\rho(\mathbf{r})$	$\nabla^2 \rho(\mathbf{r})$						
He	0.002	0.009	0.002	0.011	0.002	0.009	0.001	0.005	0.002	0.010
Ne	0.003	0.014	0.003	0.014	0.003	0.014	0.003	0.014	0.003	0.014
Ar	0.006	0.022	0.006	0.024	0.006	0.023	0.006	0.022	0.006	0.023
Kr	0.008	0.027	0.008	0.026	0.007	0.024	0.007	0.024	0.007	0.024
$H_2$	0.003	0.010	0.004	0.012	0.003	0.010	0.004	0.011	0.003	0.009

It is found that the number of bcps and bond paths linking the noble gas atom with the ring carbon atoms of  $\mathbf{R}_{IV}$  increases with the strength of the interaction. For instance weaker complexes,  $\mathbf{R}_{IV}$ ...He and  $\mathbf{R}_{IV}$ ...Ne are characterized by 8 bcps and 8 bond paths whereas stronger  $\mathbf{R}_{IV}$ ...Ar and  $\mathbf{R}_{IV}$ ...Kr complexes exhibits 10 and 12 bcps respectively. The values of  $\rho(\mathbf{r})$  and  $\nabla^2 \rho(\mathbf{r})$  also increase with the strength of the interaction.

## **4.8 Conclusions**

In Part A of this chapter, neutral molecular receptors capable of binding lone pair bearing molecules including anions through multiple lone pair- $\pi$  interactions have been proposed through density functional theory calculations. The bidentate  $(\mathbf{R}_{I})$ , tridentate  $(\mathbf{R}_{II})$  and tetradentate  $(\mathbf{R}_{III})$  receptor models bind to electron-rich guest molecules (viz.  $N_2$ ,  $O_3$ ,  $H_2O$ ,  $H_2O_2$ ,  $F^-$ ,  $Cl^-$ ,  $BF_4^-$ ,  $NO_3^-$ ,  $ClO^-$ ,  $ClO_2^-$ ,  $ClO_3^-$ ,  $ClO_4^-$  and  $SO_4^{2-}$ ) through two, three and four or more lone pair- $\pi$  interactions. **R**<sub>III</sub>, due to its flexible tripodal structure and the most electron-deficient character of the aromatic rings provide the maximum number of interaction sites and hence complexes more effectively to the electron-rich guest molecules. The favorable interactions between the receptor models and guest molecules in both gas phase and solution phase suggest that these molecules which exploit lone pair- $\pi$ /anion- $\pi$  interactions can indeed serve as excellent lead molecules towards the synthesis of neutral receptors for small molecules and anions with potential applications in chemistry and biology. The present study also underlines our previous observation that  $V_{\min}$  is a good descriptor to measure the strength of the interaction between the lone pair bearing molecule and an electron-deficient  $\pi$ -system since the E<sub>int</sub> data of the host-guest complexes follow more or less the same trend as the lone pair strength of the molecules revealed from their  $V_{\min}$  values. By systematically increasing the number of electron-deficient aromatic rings, substantial increase in anion- $\pi$  interaction can be achieved, and this strategy is useful for developing molecular motifs for the recognition of weakly binding organic anions and neutral molecules with lone pairs.

Part B reports fluorinated cage receptor ( $\mathbf{R}_{IV}$ ) molecule for the encapsulation of noble gas atoms and molecular hydrogen using density functional theory calculations. The cages are constructed by pentafluorobenzyl ( $C_6F_5CH_2$ -) substitution of HFB core to form a cage cavity. Stable van der Waals complexes of  $\mathbf{R}_{IV}$  with noble gas atoms and  $H_2$  predicted from DFT calculations suggest that this molecule could find potential applications as molecular receptors for rare gases and for hydrogen storage.

## List of publications

### A) Articles in Journals

- Comparison of Aromatic NH...π, OH...π and CH...π Interactions of Alanine Using MP2, CCSD, and DFT Methods. Mohan, N.; Vijayalakshmi, K. P.; Koga, N.; Suresh, C. H. J. Comp. Chem. 2010, 31, 2874.
- Mechanism of Epoxide Hydrolysis in Microsolvated Nucleotide Bases Adenine, Guanine and Cytosine: A DFT Study. Vijayalakshmi, K. P.; Mohan, N.; Ajitha, M. J.; Suresh, C. H. Org. Biomol. Chem. 2011, 9, 5115.
- Molecular Electrostatics for Probing Lone Pair-π Interactions. Mohan, N.; Suresh, C. H.; Kumar, A.; Gadre, S. R. *Phys. Chem. Chem. Phys.*, 2013, 15, 18401.
- Lone Pairs: An Electrostatic Viewpoint. Kumar, A.; Gadre, S. R.; Mohan, N.; Suresh, C. H. J. Phys. Chem. A, 2014, 118, 526.
- A Molecular Electrostatic Potential Analysis of Hydrogen, Halogen, and Dihydrogen Bonds. Mohan, N.; Suresh, C. H. J. Phys. Chem. A, 2014, DOI: 10.1021/jp4115699.
- Energies of Hydrogen Bonds, Halogen Bonds and Dihydrogen Bonds: A Comparison of MP2, MP4, M06L and W1BD methods. Mohan, N.; Suresh, C. H. (submitted).
- Anion Receptors Based on Highly Fluorinated Aromatic Scaffolds. Mohan, N.; Suresh, C. H. (*submitted*).

#### **B)** Published contributions to academic conferences

- 1. Presented a poster entitled "Quantifying Lone Pair Strength and Lone Pair- $\pi$ Interactions Using Molecular Electrostatic Potential" in the 3<sup>rd</sup> Indo-German Conference on "Modeling Chemical and Biological (Re)Activity (MCBR 2013)" held at NIIPER and IISER, Mohali, during 26<sup>th</sup> February to 1<sup>st</sup> March 2013.
- 2. Presented a poster entitled "Design of novel receptors for lone pairs and anions based on lone pair- $\pi$  interactions" in the "Symposium on Theoretical and Computational Chemistry-Frontiers and Challenges" held at Bharathidasan University, Tiruchirappalli, during June 14-15, 2013.

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